

Study of CO₂ desublimation during cryogenic carbon capture using the lattice Boltzmann method

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Cryogenic carbon capture (CCC) can preferentially desublimate CO_2 out of the flue gas. A widespread application of CCC requires a comprehensive understanding of CO_2 desublimation properties. This is, however, highly challenging due to the multiphysics behind it. This study proposes a lattice Boltzmann (LB) model to study CO₂ desublimation on a cooled cylinder surface during CCC. In two-dimensional (2-D) simulations, various CO₂ desublimation and capture behaviours are produced in response to different operation conditions, namely, gas velocity (Péclet number Pe) and cylinder temperature (subcooling degree ΔT_{sub}). As *Pe* increases or ΔT_{sub} decreases, the desublimation rate gradually becomes insufficient compared with the CO₂ supply via convection/diffusion. Correspondingly, the desublimated solid CO₂ layer (SCL) transforms from a loose (i.e. cluster-like, dendritic or incomplete) structure to a dense one. Four desublimation regimes are thus classified as diffusion-controlled, joint-controlled, convection-controlled and desublimation-controlled regimes. The joint-controlled regime shows quantitatively a desirable CO₂ capture performance: fast desublimation rate, high capture capacity, and full cylinder utilization. Regime distributions are summarized on a $Pe-\Delta T_{sub}$ space to determine operation parameters for the joint-controlled regime. Moreover, three-dimensional simulations demonstrate four similar desublimation regimes, verifying the reliability of 2-D results. Under regimes with loose SCLs, however, the desublimation process shows an improved CO_2 capture performance in three dimensions. This is attributed to the enhanced availability of gas-solid interface and flow paths. This work develops a reliable LB model to study CO₂ desublimation, which can facilitate applications of CCC for mitigating climate change.

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1. Introduction

Global climate change is taking place at an unprecedented pace and is expected to have dramatic consequences on humankind from both health and economic perspectives (Babar et al. 2021; Zhao et al. 2022). There is a consensus among researchers that the growing anthropogenic CO₂ emissions are mainly to blame (Farcas & Woods 2009; Mac Dowell et al. 2017; Hepburn et al. 2019; Gilmore et al. 2022). To mitigate CO₂ emissions, it is necessary to introduce carbon capture technologies to separate CO_2 from the flue gas of power plants. Several CO_2 capture technologies are under development, such as chemical absorption, physical adsorption, membrane separation and cryogenic capture (Song et al. 2019; Nocito & Dibenedetto 2020; Gomez-Rueda et al. 2022; Naquash et al. 2022). One of the cryogenic carbon capture (CCC) technologies is to desublimate CO_2 on the cooled surface of heat exchangers, achieving the separation of CO_2 in pure from the flue gas (bin Ab Halim 2013; Maqsood et al. 2014; Shen et al. 2022). This desublimation-based CCC technology offers attractive advantages, such as easy operation, high efficiency, no chemical reaction, and pure separation. With these advantages, CCC is considered to hold significant application perspectives and research interests (Babar et al. 2018, 2021; Font-Palma, Cann & Udemu 2021). Nevertheless, compared with the other mature technologies, the development of desublimation-based CCC is still in a nascent stage due to some operational concerns (Pan, Clodic & Toubassy 2013; Gallucci & van Sint Annaland 2015). For example, a proper cooling temperature is required to guarantee the efficient desublimation rate and avoid the high cooling duty and cost. Meanwhile, the flue gas should be fed at a suitable rate so that the heat transfer surface can be fully utilized before the flue gas breakthrough. Furthermore, the desublimated solid CO_2 layer (SCL) needs to be controlled in a suitable pattern, otherwise it may adversely affect heat and mass transfer and even plug flow paths. These concerns demand a deep investigation of CO_2 desublimation in the CCC process.

During the desublimation-based CCC process, the flue gas containing multiple components flows unsteadily in void channels (or flow paths). Meanwhile, the component CO_2 desublimates on the cooled surface of solid heat exchangers, which introduces two important physical processes: the evolution of channel structures, and the conjugate heat transfer between the solid and the gas phases. These two processes, in turn, can significantly affect the flue gas flow and the CO₂ desublimation rate (Debnath et al. 2019). Therefore, CO_2 desublimation in the CCC process is a complex problem with fully coupled multiphysics. To study such a problem, some experiments were designed and conducted. Tuinier et al. (2010) proposed a post-combustion CCC system based on packed beds. This novel system used packing materials to act as the heat transfer surface for CO_2 desublimation, which operated in three consecutive steps: cooling, capture and recovery. In order to obtain a pseudo-continuous capture of CO₂, Tuinier, Hamers & van Sint Annaland (2011a) and Tuinier & van Sint Annaland (2012) operated three packed beds in parallel, following three different cycles of capture, recovery and cooling. They also changed the system design to use the evaporation of liquid natural gas for cooling, which would be a preferred option if the liquid natural gas was available at low cost (Tuinier et al. 2011a). By using such dynamically operated beds at atmospheric pressure, CO_2 was effectively separated from the flue gas or biogas. But this CCC system was not tested for gas mixtures with high CO_2 content and high pressure. To fill this gap, cryogenic

packed beds with different flow configurations were exploited to purify the natural gas with high CO_2 content (Ali *et al.* 2014, 2016). Through experimental observations, the countercurrent flow configuration was found to provide optimal separation and energy efficiencies, which was superior to the cocurrent flow bed.

Later, another CCC system was developed to introduce Stirling coolers as the heat transfer surface (Song, Kitamura & Li 2012a; Song et al. 2012b, 2013). Similar to the above CCC systems with packed beds, this one included three Stirling coolers for gas cooling, CO_2 desublimation, and CO_2 capture. From experiments, CO_2 and H_2O were separated at different Stirling coolers, without introducing large pressure drops and plugging problems. In addition, by adjusting operation parameters (i.e. the gas flow rate and the Stirling cooler temperature), the optimal performance with high CO_2 recovery and low energy consumption was obtained. More recently, in order to avoid the use of multiple packed beds or Stirling coolers, a new CCC system based on a packed bed of moving packing materials was built (Willson et al. 2019; Cann, Font-Palma & Willson 2021). Experimental results showed that this system had a modest life cost for large-scale applications, but a substantially low cost for small-scale applications. Besides, no excessive accumulation of desublimated CO_2 was observed in the capture step, suggesting the ability to capture CO_2 continuously. Subsequently, Wang et al. (2020) carried out experiments to visualize the growth of the SCL on a cooled surface. They demonstrated that under the low-temperature condition, CO₂ desublimated quickly to generate a loose SCL, which sublimated easily in the recovery step.

The above experiments were conducted to implement various cryogenic capture concepts and investigate the CO_2 capture performance. Due to the operational complexity and the experimental cost, however, limited system designs and operation conditions could be tested by experiments. For such reasons, the numerical simulation was applied as a powerful and economic approach to investigate the desublimation-based CCC technology. Tuinier et al. (2010) proposed a one-dimensional (1-D) pseudo-homogeneous model to describe evolutions of axial temperature, desublimated CO_2 , and concentration profiles during the CCC process within packed beds. This 1-D model was validated by their experiments, and the CO_2 capture performance was evaluated for different parameters. The lower inlet CO_2 content and the higher bed temperature were found to cause the larger cooling duty per mass of CO2 captured (Tuinier, van Sint Annaland & Kuipers 2011b). Moreover, compared with other competing CO_2 capture technologies (i.e. chemical absorption and membrane separation), the packed-bed-based CCC was shown to be favourable in cases with the decreased pressure drop and the incorporated impurity removal (Tuinier et al. 2011a). By introducing a multiple equilibrium temperature scheme, this 1-D model was extended to investigate the CO_2 capture performance of a desublimation-based cryogenic pipeline network consisting of three packed beds (Ali et al. 2016). The modelled CO_2 content at the outlet showed a promising agreement with experimental measurements. This 1-D pseudo-homogeneous model was modified further to consider the desublimation of CO_2 both on the gas-solid interface and in the gas area (Debnath et al. 2019). The spatio-temporal evolution of an SCL in a cryogenic packed bed was simulated under different operation conditions. The results suggested that the desublimation rate increased with the decreasing bed temperature, the increasing pressure, and the ascending CO_2 content. In order to enhance the understanding of CCC using Stirling coolers, Song et al. (2013, 2014, 2017a,b) developed a two-dimensional (2-D) model to simulate the formation of an SCL during the CCC process. By synthesizing the heat integration and the membrane capture units, their simulations demonstrated that the energy requirement of the improved CCC system was reduced. Besides, with the growth of

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the SCL on Stirling coolers, the temperature of the SCL increased and the desublimation rate of CO_2 decreased. This indicated that an advanced knowledge base of the SCL could hep to improve the CO_2 capture performance. By comparing with experiments, Wang *et al.* (2018*a*) also demonstrated that numerical models considering heat transfer in the SCL could produce more accurate results.

The existing numerical studies have improved the understanding of CO_2 desublimation during the CCC process. However, they applied volumetric models to describe the desublimation of CO_2 on the cooled heat transfer surface, which simplified the intricate pore structure of the SCL as homogeneous. Consequently, these models focused on averaged desublimation properties at macroscopic scales and ignored pore-scale details. Furthermore, these numerical studies adopted empirical correlations to determine the effective transport and desublimation properties. But the formulation of empirical correlations requires a prior understanding of pore-scale desublimation properties (Xu *et al.* 2018*a,b*, 2022). As can be seen, models that can investigate CO_2 desublimation in the CCC process at the pore scale are essential.

As a powerful pore-scale solver, the lattice Boltzmann (LB) method has been applied widely to study complex fluid flows in porous structures over the past three decades (Li et al. 2016; Lei, Luo & Wu 2019; Lei & Luo 2021a; Chen et al. 2022). Accordingly, LB simulations were reported to investigate separately the physical processes that are encountered in CO_2 desublimation, including the unsteady fluid flow, the heat and mass transfer, and the active gas-solid interface for desublimation. On the one hand, for simulating the incompressible fluid flow and component transport in porous structures, LB models with a single relaxation time or multiple relaxation times were developed (Dorschner et al. 2016; Wang et al. 2018b; Lei & Luo 2020). Compared with traditional solvers, these LB models offered attractive advantages, such as simple implementation, high parallelism, easy treatment of complex porous structures, and the ability to extend from two to three dimensions. On the other hand, CO_2 desublimation on the active gas-solid interface can be modelled by tracking the porous structure evolution and solving the boundary conditions for mass conservation and conjugate heat transfer. To model the mass conservation condition at the active fluid-solid boundary, Zhang et al. (2012) developed a general bounce-back LB boundary scheme. This scheme was easy to implement and suitable for boundaries with or without curvature and velocity, but the update of porous structures was not considered. In the meantime, Kang, Lichtner & Zhang (2006) and Chen et al. (2014) proposed an LB boundary scheme to solve the active fluid-solid interface, with both the dissolution of solid matrix and the precipitation of solid products being considered. Under effects of these two interfacial reactions, porous structures evolved with time and were tracked by the volume of pixel (VOP) method. Their model was applied extensively to investigate the active fluid-solid boundary in applications such as geological CO_2 sequestration and fuel cells (Chen *et al.* 2018*a,b*; Chen, Kang & Tao 2019; Lei & Luo 2021b). To solve the conjugate heat transfer boundary conditions, several efforts were made in the LB community without involving conventional extrapolations or iterations (He et al. 2019). A half-lattice division scheme was proposed to model the conjugate heat transfer between the solid and fluid phases. The reliability of this scheme was limited to cases with steady-state solutions or unified heat capacities between the two phases (Wang, Wang & Li 2007; Wang & Pan 2008). Later, by recasting the energy conservation equation, a new source term was introduced into LB equations to guarantee the conjugate heat transfer (Karani & Huber 2015). Due to the easy implementation, this treatment was applied to consider the conjugate heat transfer during coke combustion and methane hydrate dissolution (Zhang et al. 2019; Lei, Wang & Luo 2021).

From the above literature review, it is concluded that the LB method can be applied to model separately various aspects of the multiphysics behind CO_2 desublimation in the CCC process. However, modelling the interaction of all these complex and coupled physics at the pore scale remains challenging and has not been achieved by a single LB model. To advance the predictive capability of the LB method and improve the current understanding of the CCC process, this work aims to develop an LB model for studying CO_2 desublimation during the CCC process at the pore scale. The main goal of the pore-scale simulations is to elucidate the CO_2 desublimation properties and evaluate the CO_2 capture performance under various operation conditions.

2. Mathematical and physical models

This study focuses on the multiphysical processes behind CO_2 desublimation during the CCC process within a packed bed. The simplified schematic of a sample cryogenic packed bed is depicted in figure 1, where the bed is jacked by stainless steel and packed with solid materials (Ali *et al.* 2014). Before constructing governing equations for describing the desublimation of CO_2 at the pore scale, some simplifications and assumptions are made as follows.

- (i) This work investigates the capture of CO₂ without detailing the cooling of packing materials and the recovery of desublimated CO₂.
- (ii) The temperature of packing materials is fixed as T_w .
- (iii) The incompressible flue gas is neutrally buoyant and obeys the ideal gas law.
- (iv) The flue gas is represented as a mixture of CO_2 and N_2 .
- (v) Fick's law is applied to describe the mass diffusion of gas components.
- (vi) The desublimation rate of the gaseous component CO₂ is proportional to the local deviation from the gas–solid equilibrium.
- (vii) Physical properties of the gas and the solid phases are set as constants in relation to the initial condition.
- (viii) To allow for a wide-range parametric study, the computational domain is reduced to a small-size one that can both decrease the computational cost and hold the CO₂ desublimation characteristics.
 - (ix) To compare 2-D and three-dimensional (3-D) simulations, the shape of packing materials is considered cylindrical.

Under these premises, a small computational domain encompassing a single solid packing cylinder is selected from the cryogenic packed bed as depicted in figure 1. The computational domain is $0 \le x \le l_x$, $0 \le y \le l_y$ and $0 \le z \le l_z$. From the inlet of the selected domain, the incompressible flue gas at temperature T_0 , pressure p_0 and velocity u_0 is injected in. Such a flue gas initially consists of CO₂ and N₂ with mass fractions Y_0 and $(1 - Y_0)$, respectively. The temperature of the packing cylinder (T_w) is above the freezing point of N₂ but below that of CO₂. Thus once the flue gas is sufficiently cooled by the cylinder, N₂ continues passing the cylinder and leaving the domain without phase change, while the gaseous CO₂ starts to deposit as solid on the cylinder surface:

$$\operatorname{CO}_2(\mathbf{g}) \to \operatorname{CO}_2(\mathbf{s}) + Q.$$
 (2.1)

Here, Q is the released heat from CO₂ desublimation, and the gaseous and solid phases of CO₂ are denoted by g and s, respectively. During such a desublimation process, the mass transfer rate from the gaseous CO₂ to the solid CO₂ is estimated as (Tuinier *et al.* 2010;

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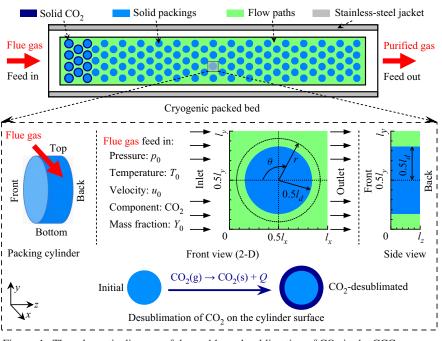


Figure 1. The schematic diagram of the problem: desublimation of CO_2 in the CCC process.

Debnath et al. 2019)

$$m_r = k_r (y_i p - p_e). \tag{2.2}$$

In the above calculation, k_r is the mass desublimation rate constant, p is the flue gas pressure, and y_i is the mole fraction of CO₂. The value of y_i is calculated based on the mass fraction Y of CO₂:

$$y_i = \frac{M}{M_{\rm CO_2}} Y$$
, with $\frac{1}{M} = \frac{Y}{M_{\rm CO_2}} + \frac{1 - Y}{M_{\rm N_2}}$, (2.3)

where M, M_{CO_2} and M_{N_2} are the molecular weights of the flue gas, CO₂ and N₂, respectively. The equilibrium pressure between the gas and the solid phases corresponding to the local temperature T is determined by an empirical correlation as (Tuinier *et al.* 2010)

$$p_e = \exp\left(10.257 - \frac{3082.7}{T} + 4.08\ln T - 2.2658 \times 10^{-2}T\right).$$
 (2.4)

The units of p_e and T are pascal (Pa) and kelvin (K), respectively. Note that CO₂ desublimates continuously on the cylinder surface until the equilibrium pressure is reached. That is, (2.2) is valid when the partial pressure of CO₂ is larger than the equilibrium pressure (i.e. $y_i p > p_e$), otherwise the mass transfer rate becomes zero under conditions with $y_i p \leq p_e$. From the desublimation process, the released heat Q is calculated as

$$Q = m_r a_r h_r, \tag{2.5}$$

with h_r being the enthalpy change of CO₂ desublimation, and a_r being the specific surface area per unit volume. During the CO₂ desublimation process, the pore structure of the SCL

changes with the deposition of solid CO_2 on the cylinder surface. This structure evolution is tracked by the mass conservation equation for the solid CO_2 as (Kang *et al.* 2014)

$$\rho_s \frac{\partial V_s}{\partial t} = m_r a_r V_r, \qquad (2.6)$$

where V_s and ρ_s represent the volume and density of solid CO₂, respectively, and V_r is the active volume for desublimation.

To model CO₂ desublimation at the pore scale, a set of governing equations is built, including the continuity equation (2.7) and the incompressible Navier–Stokes equation (2.8) for the flue gas flow, the species conservation equation (2.9) for the transport of CO₂ in flow paths, and the energy conservation equation (2.10) for heat transfer in both flow paths and solid phases (i.e. solid cylinder and solid CO₂):

•

$$\nabla \cdot \boldsymbol{u} = \boldsymbol{0}, \tag{2.7}$$

$$\rho_g \frac{\partial \boldsymbol{u}}{\partial t} + \rho_g \nabla \boldsymbol{\cdot} (\boldsymbol{u}\boldsymbol{u}) = -\nabla p + \rho_g \nabla \boldsymbol{\cdot} (\boldsymbol{\nu} \nabla \boldsymbol{u}), \qquad (2.8)$$

$$\frac{\partial Y}{\partial t} + \nabla \cdot (Y \boldsymbol{u}) = \nabla \cdot (D \,\nabla Y), \qquad (2.9)$$

$$\frac{\partial}{\partial t}(\rho c_p T) + \nabla \cdot (\rho c_p T \boldsymbol{u}) = \nabla \cdot (\rho c_p \alpha \, \nabla T) + Q.$$
(2.10)

Here, u = (u, v, w), ρ_g and v are the gas velocity, density and kinematic viscosity, respectively; *t* is the time, and *D* is the diffusion coefficient of the gaseous component CO₂; ρ , c_p and α are the local density, specific heat at constant pressure, and thermal diffusivity, respectively.

Such governing equations must satisfy boundary conditions at both internal and external boundaries of the computational domain. At the internal interface between the flue gas and the solid cylinder or solid CO_2 , two types of boundary conditions are considered.

On the one hand, at the gas–solid interface I satisfying the criterion $y_i p > p_e$, the gaseous CO₂ desublimates to generate the solid CO₂ and release heat. Such a desublimation process at the internal interface I is described by boundary conditions as

$$\boldsymbol{u}^{l} = (0,0), \qquad (2.11)$$

$$\boldsymbol{n} \cdot D\rho_g \,\nabla Y^I = m_r,\tag{2.12}$$

$$T^{I,+} = T^{I,-}, \quad \boldsymbol{n} \cdot (k \,\nabla T + \rho c_p \boldsymbol{u} T)^{I,+} = \boldsymbol{n} \cdot (k \,\nabla T + \rho c_p \boldsymbol{u} T)^{I,-} + q.$$
(2.13*a*,*b*)

These equations describe the no-slip velocity (2.11), the mass conservation (2.12), and the conjugate heat transfer (2.13*a*,*b*) boundary conditions. In these equations, *n* is the interface normal pointing to the gas phase, + and - denote parameters on either side of *I*, $k = \alpha \rho c_p$ is the thermal conductivity, and *q* is the heat flux caused by CO₂ desublimation.

On the other hand, at the gas-solid interface I_n satisfying $y_i p \leq p_e$, there is no CO₂ desublimation, and the no-flux boundary condition is adopted for mass conservation. Thus the boundary conditions at the internal interface I_n reduce to

$$\boldsymbol{u}^{l_n} = (0,0)\,, \tag{2.14}$$

$$\boldsymbol{\nabla}Y^{I_n} = \mathbf{0},\tag{2.15}$$

$$T^{I_n,+} = T^{I_n,-}, \quad \boldsymbol{n} \cdot (k \,\nabla T + \rho c_p \boldsymbol{u} T)^{I_n,+} = \boldsymbol{n} \cdot (k \,\nabla T + \rho c_p \boldsymbol{u} T)^{I_n,-}.$$
(2.16*a*,*b*)

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At the external boundaries of the computational domain, boundary conditions are set as follows. First, at the inlet (x = 0), the component mass fraction, temperature and velocity are specified. This is because the flue gas is injected into the domain at a specific operation condition. Then, at the outlet $(x = l_x)$, the zero-gradient velocity and the no-flux conditions for temperature and mass fraction are applied. A fully developed flow is thus considered there, and the flue gas can flow out freely. Finally, at the bottom (y = 0) and top (y = 0) l_{y}), the periodic conditions are imposed. Note that the additional front (z = 0) and back $(z = l_z)$ boundaries in 3-D simulations are also treated as periodic ones. These boundary conditions are described by

$$u = u_0, \quad v = 0, \quad w = 0, \quad Y = Y_0, \quad T = T_0 \quad \text{on } x = 0,$$
 (2.17)

$$\nabla u = \nabla v = \nabla w = \mathbf{0}, \quad \nabla Y = \mathbf{0}, \quad \nabla T = \mathbf{0} \quad \text{on } x = l_x,$$
 (2.18)

$$\zeta(y=0) = \zeta(y=l_y), \quad \zeta(z=0) = \zeta(z=l_z) \text{ for } \zeta = u, Y, T.$$
 (2.19)

In order to model CO_2 desublimation using the LB method, the above physical parameters should be converted to those in the lattice units. For this purpose, dimensionless parameters are derived to act as the conversion criteria between the two systems of units. By introducing the characteristic length L, velocity U, temperature T_{ch} and density ρ_g , dimensionless parameters marked by asterisks are derived as

$$x^{*} = \frac{u}{L}, \quad t^{*} = \frac{tU}{L}, \quad u^{*} = \frac{u}{U}, \quad \rho^{*} = \frac{\rho}{\rho_{g}}, \quad p^{*} = \frac{p}{\rho_{g}U^{2}}, \quad T^{*} = \frac{T}{T_{ch}},$$
$$m_{r}^{*} = \frac{m_{r}}{\rho_{l}U}, \quad h_{r}^{*} = \frac{h_{r}}{c_{p,g}T_{ch}}, \quad k_{r}^{*} = k_{r}U, \quad Re = \frac{LU}{\nu}, \quad Pe = \frac{LU}{D}, \quad Pr = \frac{\nu}{\alpha_{g}}.$$
(2.20)

The subscript g refers to physical properties of the flue gas. From such dimensionless derivations, key characteristic numbers are obtained, such as the Reynolds number Re, the Péclet number Pe, and the Prandtl number Pr. In the following LB simulations, a match of these dimensionless variables ensures the same desublimation properties between the lattice space and the real physical coordinate.

3. Numerical method

Considering different thermophysical properties between the gas and solid phases, (2.10)is recast as

$$\frac{\partial T}{\partial t} + \nabla \cdot (T\boldsymbol{u}) = \nabla \cdot (\alpha \nabla T) + F_T, \qquad (3.1)$$

with the source term F_T being

$$F_T = F_{T1} + F_{T2}, \quad F_{T1} = \frac{Q}{\rho c_p}, \quad F_{T2} = \frac{\nabla(\rho c_p)}{\rho c_p} \cdot (\alpha \,\nabla T - T \boldsymbol{u}) - \frac{T}{\rho c_p} \frac{\partial(\rho c_p)}{\partial t}.$$
(3.2*a*-*c*)

The derivation details can be found in our earlier work (Lei *et al.* 2021).

To solve the governing equations (2.7)–(2.9) and (3.1) in two and three dimensions, the 2-D nine-velocity (D2Q9) and 3-D fifteen-velocity (D3Q15) multiple-relaxation-time (MRT) LB models are developed, respectively (Pan, Luo & Miller 2006; Guo & Shu 2013; Lei & Luo 2019). The corresponding discrete velocities e_i and weight coefficients w_i are provided in Appendix A.

In the proposed LB models, a set of evolution equations is built as (Guo & Shu 2013; Lei & Luo 2019; Lei *et al.* 2021)

$$f_i\left(\mathbf{x} + \mathbf{e}_i\delta_t, t + \delta_t\right) - f_i\left(\mathbf{x}, t\right) = -\left(\mathbf{M}^{-1}\mathbf{S}\mathbf{M}\right)_{ij} \left[f_j\left(\mathbf{x}, t\right) - f_j^{eq}\left(\mathbf{x}, t\right)\right],\tag{3.3}$$

$$g_i\left(\boldsymbol{x} + \boldsymbol{e}_i\delta_t, t + \delta_t\right) - g_i\left(\boldsymbol{x}, t\right) = -\left(\boldsymbol{M}^{-1}\boldsymbol{S}_{\boldsymbol{y}}\boldsymbol{M}\right)_{ij} \left[g_j\left(\boldsymbol{x}, t\right) - g_j^{eq}\left(\boldsymbol{x}, t\right)\right], \quad (3.4)$$

$$h_{i}\left(\boldsymbol{x}+\boldsymbol{e}_{i}\delta_{t},t+\delta_{t}\right)-h_{i}\left(\boldsymbol{x},t\right)=-\left(\boldsymbol{M}^{-1}\boldsymbol{S}_{t}\boldsymbol{M}\right)_{ij}\left[h_{j}\left(\boldsymbol{x},t\right)-h_{j}^{eq}\left(\boldsymbol{x},t\right)\right]$$
$$+\delta_{t}\bar{F}_{T,i}+\frac{\delta_{t}^{2}}{2}\frac{\partial\bar{F}_{T,i}}{\partial t},$$
(3.5)

where *i* and *j* are discrete directions, and $f_i(x, t)$, $g_i(x, t)$ and $h_i(x, t)$ are distribution functions for the density, the CO₂ mass fraction and the temperature fields, respectively. The corresponding equilibrium distribution functions f_i^{eq} , g_i^{eq} and h_i^{eq} are given as

$$f_i^{eq} = w_i \left[\rho_g + \rho_p \left(\frac{\boldsymbol{e}_i \cdot \boldsymbol{u}}{c_s^2} + \frac{(\boldsymbol{e}_i \cdot \boldsymbol{u})^2}{2c_s^4} - \frac{\boldsymbol{u}^2}{2c_s^2} \right) \right],$$
(3.6)

$$g_i^{eq} = w_i Y \left[1 + \frac{e_i \cdot u}{c_s^2} + \frac{(e_i \cdot u)^2}{2c_s^4} - \frac{u^2}{2c_s^2} \right],$$
(3.7)

$$h_i^{eq} = w_i T \left[1 + \frac{e_i \cdot u}{c_s^2} + \frac{(e_i \cdot u)^2}{2c_s^4} - \frac{u^2}{2c_s^2} \right].$$
(3.8)

Here, ρ_p is a variable related to the gas pressure as $\rho_p = p/c_s^2$, where $c_s = e/\sqrt{3}$ is the lattice sound velocity; $e = \delta_x/\delta_t$ is the lattice speed and is set as e = 1 in the following simulations, with δ_x and δ_t denoting the lattice spacing and time step, respectively. This LB model for incompressible fluid flows can reduce compressible errors (Guo & Shu 2013).

To avoid discrete lattice effects, the distribution function for the thermal source term (F_T) is defined as (Guo & Zhao 2002; Shi & Guo 2009)

$$\bar{F}_{T,i} = w_i F_T \left(1 + \frac{\boldsymbol{e}_i \cdot \boldsymbol{u}}{c_s^2} \frac{\tau_t - 0.5}{\tau_t} \right), \tag{3.9}$$

with τ_t being the relaxation time. The time derivatives in (3.2c) $(\partial \rho c_p / \partial t)$ and (3.5) $(\partial \bar{F}_{T,i} / \partial t)$ are treated by the backward scheme. In the evolution equations (3.3)–(3.5), **S**, **S**_y and **S**_t are the diagonal relaxation matrices, while **M** is the transformation matrix to map distribution functions from the physical space to the moment space. More details about the transformation are provided in Appendix A. Based on the distribution functions, the macroscopic variables can be calculated finally as

$$\rho_p = \sum_i f_i, \quad \rho_g \boldsymbol{u} = \sum_i \boldsymbol{e}_i f_i, \quad Y = \sum_i g_i, \quad T = \sum_i h_i. \tag{3.10a-d}$$

In order to obtain the accurate solution of (2.7)–(2.9) and (3.1) by the above LB models, boundary conditions for macroscopic variables in (2.11)–(2.19) should be satisfied. Note, however, that the fundamental variables in LB equations are discrete distribution functions

(i.e. $f_i(x, t)$, $g_i(x, t)$ and $h_i(x, t)$). It is thus necessary to build LB boundary schemes to transform the boundary conditions for macroscopic variables to those for discrete distribution functions.

On the one hand, treatments of the external boundary conditions are introduced. For the specified inlet in (2.17) and the fully developed outlet in (2.18), the non-equilibrium extrapolation boundary scheme is applied to reconstruct the unknown distribution functions (Guo & Shu 2013). For the periodic top and bottom boundaries in (2.19), the outgoing distribution functions from the top re-enter the domain from the bottom, and vice versa (Guo & Shu 2013). This scheme is also applied for the periodic front and back boundaries in (2.19).

On the other hand, LB schemes are built for modelling boundary conditions at the internal boundaries I and I_n . For the gas–solid interface I with the desublimation of CO₂, three boundary treatments are required. First, the conjugate heat transfer in (2.13*a*,*b*) is satisfied automatically by solving the energy conservation equation (3.1). Then the no-slip velocity condition in (2.11) is addressed by the halfway bounce-back scheme, with the unknown distribution functions at the gas grid x_g adjacent to I being (Zhang *et al.* 2012)

$$f_{\bar{t}}(x_g, t + \delta_t) = f'_i(x_g, t).$$
(3.11)

Here, the superscript ' denotes the post-collision distribution function, *i* is the direction opposite to \bar{i} (i.e. $e_i = -e_{\bar{i}}$), and e_i points to the solid phase. Finally, to solve the mass conservation condition in (2.12), the CO₂ mass fraction gradient at interface I (∇Y^I) is calculated based on the finite-difference scheme as (Zhang *et al.* 2012)

$$\boldsymbol{n} \cdot \boldsymbol{\nabla} \boldsymbol{Y}^{I} = \frac{\boldsymbol{Y}^{g} - \boldsymbol{Y}^{I}}{0.5\boldsymbol{n} \cdot \boldsymbol{e}_{i}\delta_{x}},\tag{3.12}$$

where Y^g is the CO₂ mass fraction at the gas grid neighbouring the interface *I*. By inserting (3.12) into (2.12) and using the ideal gas law, the value of Y^I is calculated as

$$Y^{I} = \frac{D\rho_{g}Y^{l} + 0.5\boldsymbol{n} \cdot \boldsymbol{e}_{i}\delta_{x}k_{r}p_{e}}{D\rho_{g} + 0.5\boldsymbol{n} \cdot \boldsymbol{e}_{i}\delta_{x}k_{r}p_{0}T/T_{0}}.$$
(3.13)

Hence the mass conservation condition reduces to a given CO_2 mass fraction value Y^I . The halfway bounce-back scheme is used to solve this boundary condition, and the unknown distribution functions at the gas grid are computed as (Zhang *et al.* 2012)

$$g_{\bar{i}}(x_g, t+\delta_t) = -g'_i(x_g, t) + 2w_i Y^I.$$
(3.14)

In addition, for the interface I_n without CO₂ desublimation, the conjugate heat transfer in (2.16*a*,*b*) and the no-slip velocity in (2.14) are addressed as conducted at interface *I*. In other words, the halfway bounce-back scheme applied to solve the no-flux condition for mass fraction in (2.15) becomes,

$$g_{\bar{t}}(x_g, t+\delta_t) = g'_i(x_g, t).$$
 (3.15)

With the desublimation process, solid CO_2 is generated to form an SCL on the cooled cylinder surface, and the movement of solid CO_2 with the fluid flow is not considered. The pore structure of the SCL is updated based on the mass conservation equation (2.6) for the solid CO_2 . In LB simulations, this structure evolution is realized by the commonly used VOP method (Kang *et al.* 2006; Zhou *et al.* 2020). Explicitly, a grid mesh is selected that

is fine enough to cover the computational domain. Thus each grid node of the domain can be assumed to represent only one material: the solid cylinder, the solid CO₂ or the flue gas. In the VOP method, each grid node (or pixel) holds a control volume of size $1 \times 1 \times 1$ in lattice units, with the grid node being located at the centre of the volume. At each grid node, the volume of solid CO₂ is noted as V_s . Initially, values of V_s are set as $V_s = 1$ at solid CO₂ grids, $V_s = 0$ at gas grids, and $V_s = 0$ at cylinder grids, respectively. As the desublimation process continues, V_s changes according to (2.6), and it is updated at each time step as

$$V_s(t+\delta_t) = V_s(t) + m_r a_r V_r / \rho_s.$$
(3.16)

Considering that each grid node can be occupied by one material, the desublimated volume is not included in the grid node until V_s exceeds the threshold value. That is, as the value of V_s doubles at a solid CO₂ grid (i.e. $V_s = 2$) or increases to $V_s = 1$ at a cylinder grid, one of its neighbouring gas grid nodes is chosen to be converted into a solid CO₂ grid. The ratios of the desublimation probability between the nearest and diagonal grid nodes are set as $R_{dp} = 1 : 0.125$ in three dimensions and $R_{dp} = 1 : 0.25$ in two dimensions, respectively. These selected R_{dp} values are consistent with the ratios of weight coefficients w_i between the nearest and diagonal directions. The sensitivity of CO₂ desublimation properties to the value of R_{dp} has been evaluated in Appendix B, thus verifying the reliability of the selected R_{dp} above.

4. Results and discussion

The developed MRT LB models are programmed in the C language, with the Message Passing Interface library being applied for parallel computing. The LB code is verified by two cases: one is the desublimation of CO_2 on the surface of a single cylinder immersed in the quiescent flue gas; the other is the desublimation of CO_2 inside a packed bed fed with flue gas. As demonstrated in Appendix C, the present numerical results agree well with existing simulations and experiments, validating the proposed LB models and verifying their implementation. In addition, for a comprehensive model validation, key sub-models of the proposed MRT LB method have been tested in the supplementary material available at https://doi.org/10.1017/jfm.2023.227. Subsequently, pore-scale simulations are conducted to investigate CO_2 desublimation on the packing cylinder as shown in figure 1. Considering that the computational domain is selected from the cryogenic bed, the volume fraction of void space is set as the bed porosity Ali et al. (2014). Thus key geometrical parameters of the computational domain are set as length $l_x = 14.7$ mm, width $l_y = 14.7$ mm, depth $l_z = 0.69$ mm, cylinder diameter $l_d = 10.0$ mm, and the void volume fraction $\phi = 0.637$. From such a 3-D structure, an x - y cross-section at a random location z_r is selected for 2-D simulations (see the front view in figure 1).

In the computational domain, a cooled cylinder at temperature T_w is placed in the centre area for CO₂ desublimation, and the remaining void space (or flow paths) is initially filled with pure N₂ at temperature T_w . The incompressible flue gas at the initial condition (T_0, Y_0, u_0, p_0) is injected from the inlet, and the component CO₂ desublimates on the surface of the cooled cylinder. The desublimation parameters are set as $k_r = 10^{-6}$ s m⁻¹ and $h_r = 5.682 \times 10^5$ J kg⁻¹ (Tuinier *et al.* 2010). The initial conditions of the flue gas are $T_0 = 293$ K, $Y_0 = 1$ and $p_0 = 0.1$ MPa. Based on the equilibrium pressure in (2.4), the freezing point of CO₂ corresponding to $p_0 = 0.1$ MPa can be calculated as $T_f = 194.6$ K. The inlet velocity of the flue gas u_0 and the cylinder temperature T_w are left for changing the desublimation conditions. Thermophysical properties of the flue gas, the solid CO₂

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and the solid cylinder are fixed as $\rho_g = 1.46$ kg m⁻³, $c_{p,g} = 0.846$ kJ kg⁻¹ K⁻¹, $\alpha_g = 5.02 \times 10^{-6}$ m²s⁻¹, $\rho_s = 1.56 \times 10^3$ kg m⁻³, $c_{p,s} = 0.967$ kJ kg⁻¹ K⁻¹, $\alpha_s = 4.64 \times 10^{-7}$ m² s⁻¹, $\rho_c = 2.55 \times 10^3$ kg m⁻³, $c_{p,c} = 0.841$ kJ kg⁻¹ K⁻¹, and $\alpha_c = 3.74 \times 10^{-7}$ m² s⁻¹. Here, the subscripts *g*, *s* and *c* represent properties of the flue gas, the solid CO₂ and the solid cylinder, respectively. The gas viscosity and the CO₂ diffusion coefficient are $\nu = 7.12 \times 10^{-6}$ m² s⁻¹ and $D = 1.63 \times 10^{-5}$ m² s⁻¹, respectively. In the subsequent simulations, the conversion between the physical and lattice units is based on a match of the dimensionless parameters in (2.20), with characteristic parameters being selected as

$$L = l_{y}, \quad U = u_{0}, \quad \rho_{ch} = \rho_{g}, \quad T_{ch} = T_{0}.$$
 (4.1*a*-*d*)

Before proceeding further, grid convergence tests have been carried out. A mesh of size $640 \times 640 \times 30$ with lattice resolution 0.0219 mm is selected to describe the computational domain in figure 1. In 2-D simulations, an x - y cross-section is selected randomly from the 3-D domain, thus the mesh size is 640×640 . More details about the grid convergence tests are provided in Appendix D and the supplementary material.

Given the periodic front and back boundaries of the computational domain, the desublimation of CO₂ is first simulated in two dimensions. A comparison with 3-D simulations is then provided to verify the reliability of 2-D results. In the subsequent simulations, the range of u_0 from 1.22×10^{-3} m s⁻¹ to 6.1×10^{-2} m s⁻¹, and the range of T_w from 100 K to 180 K, are covered. These two parameters (i.e. u_0 and T_w) are characterized by the Péclet number *Pe* and the dimensionless subcooling degree $\Delta T_{sub} = (T_f - T_w)/T_{ch}$, respectively. The corresponding *Pe* and ΔT_{sub} locate in the ranges [1.1, 55] and [0.05, 0.32], respectively. Each simulation test is continued until the maximum thickness of the SCL (δ_{fm}) reaches the termination condition $\delta_{fm} = 0.048l_x$. The termination time instant in each test is denoted as t_e . For the quantitative analysis, the coordinates ranges are set as $0 \le x \le l_x$, $0 \le y \le l_y$ and $0 \le z \le l_z$ for (x, y, z), and $l_d/2 < r \le l_x/2$, $0 \le \theta < 2\pi$ and $0 \le z \le l_z$ for (r, θ, z) . Here, the coordinate *r* starts from $l_d/2$ because we focus on the space with the flue gas and the solid CO₂. Both of these coordinate systems are used to describe the CO₂ desublimation properties.

4.1. CO₂ desublimation characteristics

To discuss the general properties of CO₂ desublimation on the cooled cylinder surface, a case with the subcooling degree $\Delta T_{sub} = 0.17$ and Péclet number Pe = 11 is first simulated in two dimensions. This case is referred to as case Base. The simulated CO₂ desublimation properties are illustrated in figure 2, including contours of solid CO₂, temperature (*T*) and CO₂ mass fraction (*Y*) at two time instants t = 8.9, 55.8 s. As the desublimation process goes on, CO₂ deposits on the cylinder surface to generate the SCL, which is observed to be thicker in the front surface area (facing the inlet) and thinner in the back surface area (facing the outlet). This uneven desublimation is driven by the continuous gas injection from the inlet. Also, distributions of *Y* show that the outgoing CO₂ mass fraction is obviously smaller than the injected value. This indicates that a large portion of the injected CO₂ is captured by the cooled cylinder. These CO₂ desublimation properties are consistent with our expectations. Moreover, by providing the enlarged solid CO₂ distributions, the intricate pore structure of the desublimated SCL is depicted at each of the selected time instants. Both *T* and *Y* are found to decrease within the SCL, implying

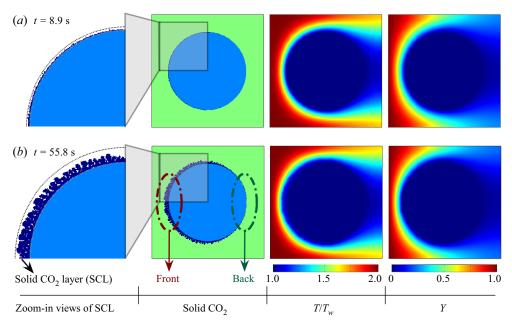


Figure 2. CO₂ desublimation properties in case Base with subcooling degree $\Delta T_{sub} = 0.17$ and Péclet number Pe = 11. Contours of solid CO₂, temperature (*T*) and CO₂ mass fraction (*Y*) at time instants (*a*) t = 8.9 s and (*b*) 55.8 s. Zoom-in views of solid CO₂ are provided to clarify pore structures of SCLs.

the suppressed heat and mass transfer there. The present 2-D simulations provide detailed temperature and CO_2 mass fraction distributions and pore structures of the SCL, which are difficult to observe from existing experiments and 1-D studies.

In order to quantify these observed CO_2 desublimation characteristics, we calculate the angularly averaged scalars as

$$\bar{\psi}_r = \frac{1}{2\pi} \int_0^{2\pi} \psi(r,\theta) \,\mathrm{d}\theta.$$
 (4.2)

Here, $\bar{\psi}_r$ represents the angularly averaged volume fraction of solid CO₂ (ϕ_r), temperature (\bar{T}_r) and CO₂ mass fraction (\bar{Y}_r) . Figure 3 plots the computed profiles of $\bar{\psi}_r$ at two time instants t = 8.9, 55.8 s. As shown in figure 3(*a*), the calculate ϕ_r increases with time and grows outwards, suggesting the growth of the SCL on the cylinder surface. The maximum ϕ_r stays on the cylinder surface and remains less than 1 (i.e. $\phi_{rm} < 1$), which stems from the weak desublimation in the back surface area. Further, profiles of ϕ_r can be used to define the surface of the SCL as the position $r = r_m$ with $\phi_r = 0.01$. The maximum thickness of the SCL (δ_{fm}) is then calculated as the distance between the surfaces of the solid cylinder ($r = l_d/2$) and the SCL ($r = r_m$). On the other hand, profiles of both \bar{T}_r and \bar{Y}_r are illustrated in figures 3(*b*) and 3(*c*). At a certain radius *r*, the value of \bar{T}_r (or \bar{Y}_r) is found to decrease with the growth of the SCL. In addition, \bar{T}_r (or \bar{Y}_r) increases at a smaller rate inside the SCL ($l_d/2 < r \leq r_m$), and at a larger rate in the gas region ($r_m < r \leq l_x/2$). This tendency results from two factors: one is the resistance of the SCL on heat and mass transfer; the other is that heat and mass are transferred mainly by the faster convection in the gas area, and the slower conduction and diffusion in the SCL.

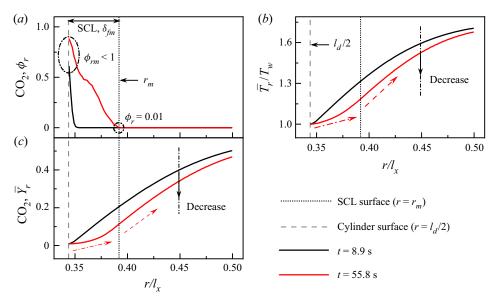


Figure 3. CO₂ desublimation properties in case Base with subcooling degree $\Delta T_{sub} = 0.17$ and Péclet number Pe = 11. Angularly averaged profiles of (*a*) volume fraction of solid CO₂ (ϕ_r), (*b*) temperature (\bar{T}_r) and (*c*) CO₂ mass fraction (\bar{Y}_r) at two time instants t = 8.9, 55.8 s.

Considering the important role of the SCL, we calculate three metrics for quantitative analyses. The first is ϕ_x , the transversally averaged volume fraction of solid CO₂:

$$\phi_x = \frac{1}{l_y} \int_0^{l_y} V_s(x, y) \, \mathrm{d}y.$$
(4.3)

The next metric is the local thickness of the SCL (δ_f) determined along the angular direction. Finally, from $l_d/2$ to $(l_d/2 + \delta_f)$, the radially averaged volume fraction of solid CO₂ (ϕ_θ) is calculated as

$$\phi_{\theta} = \frac{1}{\delta_f} \int_{l_d/2}^{l_d/2+\delta_f} V_s(r,\theta) \,\mathrm{d}r. \tag{4.4}$$

Here, $V_s(x, y)$ and $V_s(r, \theta)$ are local volumes of solid CO₂ in two different coordinates.

Profiles of ϕ_x are first depicted in figure 4(*a*). The value of ϕ_x is found to be larger in the front surface area but smaller in the back surface area, corresponding to the uneven CO₂ accumulation on the cylinder surface in figure 2. Then results for δ_f are plotted in figure 4(*b*), from which the maximum thickness of the SCL (δ_{fm}) is captured at each time instant. Here, δ_{fm} grows with time and keeps locating in the front surface area with strong CO₂ desublimation. Based on the calculated δ_f , the parameter ϕ_{θ} is finally determined along the angular direction. As shown in figure 4(*c*), the value of ϕ_{θ} remains smaller than 1, suggesting that the SCL consists of both solid CO₂ and flue gas. For illustration, figure 4(*d*) provides the zoom-in view of the SCL at the time instant *t* = 55.8 s. The observed dendritic pore structures of the SCL verify the coexistence of both solid CO₂ and flue gas. Furthermore, ignoring the small fluctuations introduced by the random selections of neighbouring gas grids for the SCL growth, profiles of δ_f and ϕ_{θ} in figures 4(*b*) and 4(*c*) are fairly symmetric about the middle of the domain ($\theta = 0$). This symmetry is attributed to the central position of the cylinder and the periodic top and bottom.

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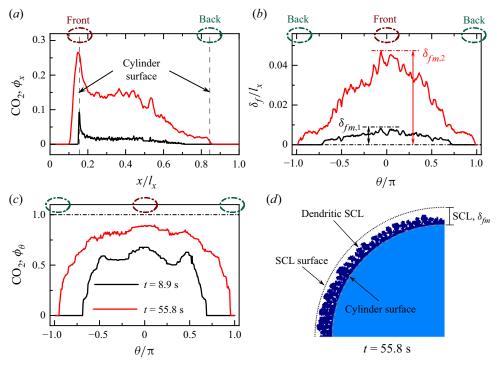


Figure 4. Analysis of the SCL in case Base with subcooling degree $\Delta T_{sub} = 0.17$ and Péclet number Pe = 11. (*a*) Transversally averaged volume fraction of solid CO₂ (ϕ_x). (*b*) Local thickness of the SCL along the angular direction (δ_f). (*c*) Radially averaged volume fraction of solid CO₂ (ϕ_θ) at two time instants t = 8.9, 55.8 s. (*d*) Zoom-in view of the SCL in the highlighted grey rectangle of figure 2(*b*) at t = 55.8 s.

By modelling this case, the general CO₂ desublimation properties have been discussed both qualitatively and quantitatively. Also, the pore structure of the SCL is visualized and analysed by different metrics. In order to further investigate effects of operation conditions on the CO₂ desublimation process, simulations with different values of ΔT_{sub} and *Pe* (i.e. T_w and u_0) are conducted. The CO₂ desublimation properties and the CO₂ capture performance are compared for different operation parameters. Based on this comparison, four distinct regimes are identified, with each one representing a unique CO₂ desublimation pattern. Results of two sets of simulations are provided as representatives of the four desublimation regimes: cases A1 and A2 with *Pe* = 11 and ΔT_{sub} = 0.32, 0.05, and cases B1 and B2 with ΔT_{sub} = 0.17 and *Pe* = 1.1, 55. The parameters for case Base, cases A1-A2 and cases B1-B2 are summarized in table 1.

4.2. Four desublimation regimes

We first consider cases A1-A2 with different ΔT_{sub} values. Based on (2.2)–(2.4), the larger subcooling degree ΔT_{sub} (or the lower temperature *T*) yields the smaller equilibrium pressure p_e and then the faster mass transfer rate m_r . Hence, compared with case Base ($\Delta T_{sub} = 0.17$), cases A1-A2 are selected to represent the faster ($\Delta T_{sub} = 0.32$) and the slower ($\Delta T_{sub} = 0.05$) CO₂ desublimation conditions, respectively. For each case, figures 5(*a*) and 5(*b*) depict spatial distributions of solid CO₂, temperature (*T*) and CO₂ mass fraction (*Y*) at the termination time instant t_e , with $\delta_{fm} = 0.048l_x$. Cases A1-A2 generally show CO₂ desublimation properties similar to case Base: the SCL grows on the

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Parameters	Case no.				
	Base	A1	A2	B1	B2
T_{w} (K)	145	100	165	145	145
$u_0 (10^{-2} \text{ m s}^{-1})$	1.22	1.22	1.22	0.122	6.10
ΔT_{sub}	0.17	0.05	0.32	0.17	0.17
Pe	11	11	11	1.1	55

Table 1. Values of the cylinder temperature T_w , the gas injection velocity u_0 , the dimensionless subcooling degree ΔT_{sub} , and the Péclet number *Pe* in case Base, cases A1-A2 and cases B1-B2.

cylinder surface, the strong CO₂ desublimation occurs in the front surface area, and heat and mass transfer is suppressed within the SCL. In addition to these similarities, cases A1-A2 show pore structures different to those of the SCL from case Base: the smaller ΔT_{sub} brings in the more compact SCL. As visualized in figure 5(*c*), the decrease of ΔT_{sub} makes the pore structure of SCL transform from a cluster-like type (A1), via a dendritic type (Base), to a dense type (A2).

The difference in pore structures of the SCL is further quantified by the angularly averaged volume fraction of solid CO₂ (ϕ_r) in figure 6(*a*). At a smaller ΔT_{sub} , ϕ_r is larger and thus the SCL is denser. This change tendency is attributed to the relative intensity of the CO_2 desublimation rate and the CO_2 supply on the gas-solid interface. Based on (2.12), CO₂ diffuses to desublimate on the gas-solid interface, thus the supplied CO₂ there is determined by diffusion. In case A1 with $\Delta T_{sub} = 0.32$, the desublimation rate is sufficiently large and the diffused CO_2 is exhausted once it reaches the surface of the SCL (or tips of solid CO_2). This fast desublimation leaves limited CO_2 to desublimate inside the SCL. The favoured CO_2 desublimation on the SCL surface combined with the restrained CO_2 desublimation inside the SCL lead to the fast growth of the SCL in a radial and cluster-like fashion. Note that, compared with the fast CO_2 desublimation, the supplied CO_2 via diffusion is insufficient, and case A1 is defined as the diffusion-controlled regime. Then in case Base, ΔT_{sub} decreases to 0.17 and the desublimation rate slows down. As a result, a part of the diffused CO_2 passes the SCL surface without phase change and desublimates inside the SCL. The comparable desublimation and diffusion of CO_2 yield the dendritic-like SCL, which is more compact than the cluster-like SCL in case A1. Case Base is thus defined as the joint-controlled regime. Finally, as ΔT_{sub} decreases continuously to 0.05 in case A2, the CO_2 desublimation rate becomes relatively slow. Instead of completely condensing on the SCL surface, the injected CO₂ diffuses to make most gas-solid interface rich in CO_2 . Therefore, the slow desublimation process occurs on most gas-solid interface, and the SCL grows in a compact and dense pattern. Considering the sufficient CO_2 supply and the slow CO_2 desublimation rate, case A2 is marked as the desublimation-controlled regime.

Upon the growth of the SCL, differences in heat and mass transfer arise among cases A1-A2 and Base. On the one hand, seen from distributions of Y in figures 2(a), 5(a) and 5(b), the injected CO₂ is captured efficiently by the cylinder in both cases A1 and Base, while a large portion of the injected CO₂ passes the cylinder and leaves the domain in case A2. Quantitatively, the angularly averaged CO₂ mass fraction (\bar{Y}_r) is calculated and plotted in figure 6(b) for case Base and cases A1-A2. As illustrated, the profile of \bar{Y}_r in case A2 is above those in the other two cases. These results indicate that the decreasing ΔT_{sub} (or the increasing T_w) gives rise to the degraded CO₂ capture performance. As

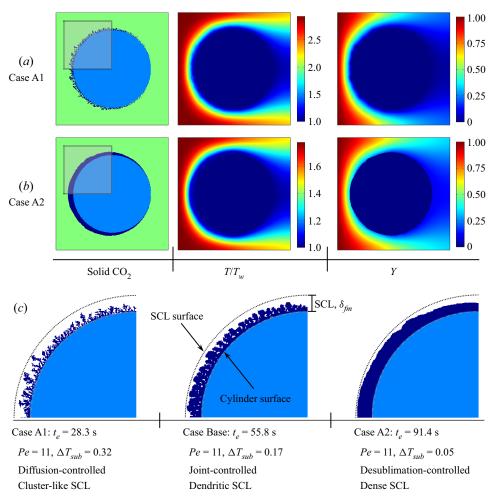


Figure 5. CO₂ desublimation properties in cases A1-A2 with Péclet number Pe = 11 and different subcooling degrees ΔT_{sub} . Contours of solid CO₂, temperature (*T*) and CO₂ mass fraction (*Y*) in (*a*) case A1 with $\Delta T_{sub} = 0.32$, and (*b*) case A2 with $\Delta T_{sub} = 0.05$, at the termination time instant t_e . (*c*) Zoom-in views of the SCL in highlighted grey rectangles for case Base and cases A1-A2.

explained above, this is due to the fact that the smaller ΔT_{sub} represents the slower CO₂ desublimation rate and the smaller capture ratio of CO₂. On the other hand, profiles of the angularly averaged temperature (\bar{T}_r) are calculate for case Base and cases A1-A2. As shown in figure 6(c), \bar{T}_r increases along the *r* direction and the increase rate in the SCL slows down as ΔT_{sub} decreases. This reflects the fact that in a low- ΔT_{sub} case, the pore structure of the SCL is compact and dense, thus its thermal resistance becomes strong.

By modelling cases A1-A2, our results show a consistent trend with previous experiments (Wang *et al.* 2020) that the SCL becomes more compact corresponding to the decreasing ΔT_{sub} . This verifies the reliability of the present LB simulations. However, previous experiments failed to describe intricate pore structures of the SCL, effects of the SCL on heat and mass transfer, and interactions between desublimation and diffusion/convection (or causes for different pore structures of the SCL). Therefore, this study helps to advance the understanding of CO₂ desublimation.

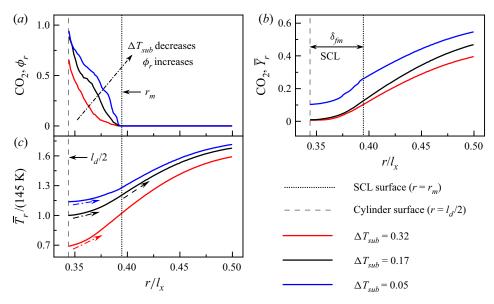


Figure 6. CO₂ desublimation properties in cases A1-A2 with Péclet number Pe = 11 and different subcooling degrees ΔT_{sub} . Angularly averaged profiles of (*a*) volume fraction of solid CO₂ (ϕ_r), (*b*) CO₂ mass fraction (\bar{Y}_r) and (*c*) temperature (\bar{T}_r), at the termination time instant t_e in case Base and cases A1-A2.

We then consider cases B1-B2 that have the smaller (B1) and the larger (B2) Péclet number Pe than case Base. The larger Pe represents the faster gas injection velocity u_0 . Again, seen from scalar distributions in figures 7(a) and 7(b), cases B1-B2 hold CO₂ desublimation properties similar to case Base. Zoom-in views of SCL structures and angularly averaged scalars are then provided in figures 7(c) and 8 to demonstrate differences between cases B1-B2 and case Base. Compared with case Base, the pore structure of the SCL becomes incompletely covered on the cylinder surface in case B1, but compact in case B2 (figure 7c). Correspondingly, there is a gradual rise in ϕ_r from case B1 via Base to B2 (figure 8a). As explained for cases A1-A2, the formation of these SCL structures is associated with the relative strength of the CO₂ desublimation rate and the CO_2 supply on the gas-solid interface. In other words, the gas convection intensity in cases B1-B2 varies obviously with the Péclet number Pe, which subsequently affects both the CO_2 desublimation rate and the CO_2 supply for desublimation. To be specific, in case B1 (Pe = 1.1), the gas convection is weak, thus the transport of CO₂ to the gas-solid interface is severely limited (figure 7*a*). As a consequence, the CO_2 desublimation rate declines sharply, the growth of the SCL is retarded strongly, and almost half of the cylinder surface is not coated by solid CO_2 (figure 7c). Due to effects of the weak convection, this case is defined as the convection-controlled regime. By contrast, the gas convection is accelerated in case B2 (Pe = 55), and CO₂ is transported easily to the gas-solid interface for desublimation. As illustrated by distributions of Y and profiles of \overline{Y}_r (figures 7(b) and $\mathcal{B}(b)$, the supply of CO₂ via convection is relatively abundant (figure 7b). Similar to case A2, the sufficient CO₂ supply compared with desublimation finally contributes to the dense and compact structure of the SCL (figure 7c). Case B2 is thus classified as the desublimation-controlled regime. Furthermore, with the increase of Pe, both T_r and \bar{Y}_r increase significantly in the flue gas region (figures 8b,c). This is because the strong convection accelerates both heat and mass transfer in the flue gas area.

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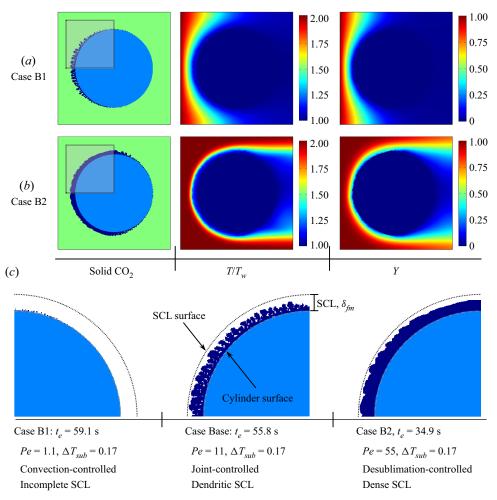


Figure 7. CO₂ desublimation properties in cases B1-B2 with subcooling degree $\Delta T_{sub} = 0.17$ and different Péclet numbers *Pe*. Contours of solid CO₂, temperature (*T*) and CO₂ mass fraction (*Y*) in (*a*) case B1 with *Pe* = 1.1 and (*b*) case B2 with *Pe* = 55, at the termination time instant *t_e*. (*c*) Zoom-in views of the SCL in highlighted grey rectangles for case Base and cases B1-B2.

After that, pore structures of the SCL in cases A-B are analysed quantitatively and compared with case Base. Figure 9 depicts the transversally averaged volume fraction of solid CO₂ (ϕ_x), the local thickness of the SCL along the angular direction (δ_f), and the radially averaged volume fraction of solid CO₂ (ϕ_θ). Profiles of these three metrics verify the strong desublimation in the front surface area and the symmetrical SCL structure about the middle of the domain. In addition, maximum values of both ϕ_x and ϕ_θ decrease as ΔT_{sub} increases or *Pe* declines, which quantify the less compact SCL (figures 9*a*,*c*). The maximum value of ϕ_θ reaches 1 in cases A2 and B2 (desublimation-controlled regime) but drops to 0.56 in case A1 (diffusion-controlled regime). Again, this verifies qualitatively the dense SCL structure under the desublimation-controlled regime, and the cluster-like SCL structure under the diffusion-controlled regime. Meanwhile, values of δ_f and ϕ_θ remain 0 in the back surface area in case B1 (convection-controlled regime) due to the incompletely coated cylinder surface by the SCL (figures 9*a*,*b*).

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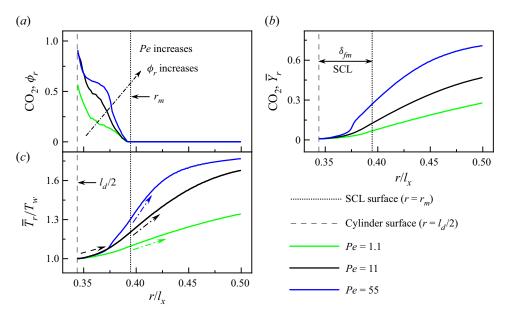


Figure 8. CO₂ desublimation properties in cases B1-B2 with subcooling degree $\Delta T_{sub} = 0.17$ and different Péclet numbers *Pe*. Angularly averaged profiles of (*a*) volume fraction of solid CO₂ (ϕ_r), (*b*) CO₂ mass fraction (\bar{T}_r), and (*c*) temperature (\bar{T}_r), at the termination time instant t_e in case Base and cases B1-B2.

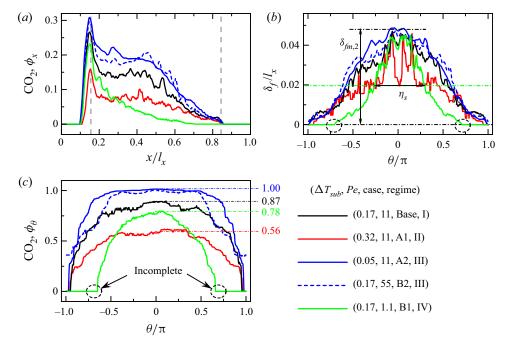


Figure 9. Analysis of the SCL in cases Base, A1-A2 and B1-B2 with subcooling degrees $\Delta T_{sub} = 0.05, 0.17, 0.32$ and Péclet numbers Pe = 1.1, 11, 55 at the termination state. (a) Transversally averaged volume fraction of solid CO₂ (ϕ_x). (b) Local thickness of the SCL along the angular direction (δ_f). (c) Radially averaged volume fraction of solid CO₂ (ϕ_θ). The four desublimation regimes are joint-controlled (II), diffusion-controlled (II), desublimation-controlled (III) and convection-controlled (IV).

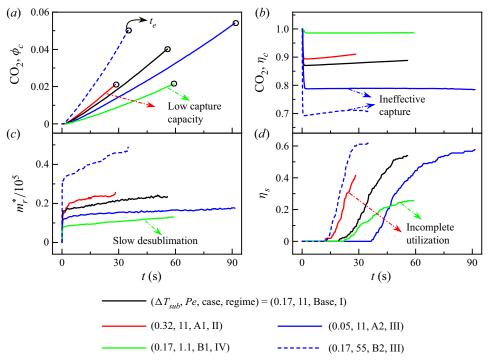


Figure 10. Analysis of CO₂ capture performance in cases Base, A1-A2 and B1-B2 with subcooling degrees $\Delta T_{sub} = 0.05, 0.17, 0.32$ and Péclet numbers Pe = 1.1, 11, 55. (a) The volume fraction of captured solid CO₂ (ϕ_c). (b) The capture efficiency of the injected CO₂ (η_c). (c) The overall desublimation rate (m_r^*). (d) The utilization of the cylinder surface (η_s). The four desublimation regimes are joint-controlled (I), diffusion-controlled (II), desublimation-controlled (III) and convection-controlled (IV).

To further discuss the CO₂ capture performance under different desublimation regimes (or cases), temporal evolutions of four metrics are recorded in figure 10, including the volume fraction of captured solid CO₂ (ϕ_c), the overall desublimation rate (m_r^*), the capture efficiency of the injected CO₂ (η_c), and the utilization of the cylinder surface (η_s). Here, ϕ_c is calculated as the volume of captured solid CO₂ over the volume of the domain, which reflects the CO₂ capture capacity, and η_c is determined based on the mass fluxes at the inlet and the outlet as

$$\eta_c = \frac{\sum_{x=0} uY - \sum_{x=l_x} uY}{\sum_{x=0} uY}.$$
(4.5)

The utilization of the cylinder surface is determined based on the local frost thickness δ_f along the angular direction. As illustrated in figure 9(*b*), the surface area satisfying the criterion $\delta_f/l_x \ge 0.02$ is considered to be utilized effectively for desublimation. Thus η_s is calculated as the ratio of the effective surface to the total surface of the cylinder. As shown in figure 10, for each simulation case, temporal evolutions of these four metrics are recorded until the termination time instant t_e with $\delta_{fin} = 0.048l_x$.

By comparing values of t_e among the four desublimation regimes, the diffusioncontrolled regime is found to possess the fastest growth of the SCL and the earliest termination of desublimation (figure 10*a*). Nevertheless, this regime features the low CO₂ capture capacity and the incomplete utilization of the cylinder surface (figures 10*a*,*d*). This is attributed to the fast CO₂ desublimation rate and the cluster-like SCL structure. Then, under the convection-controlled regime, the insufficient CO₂ supply results in the slow CO₂ desublimation rate (figure 10*c*) and the incomplete growth of the SCL on the cylinder. Subsequently, this leads to the low CO₂ capture capacity and the incomplete utilization of the cylinder surface (figures 10*a*,*d*). The highest CO₂ capture efficiency is achieved under the convection-controlled regime (figure 10*b*), which, however, is due to the slow gas injection rate (or the insufficient CO₂ supply) rather than the efficient CO₂ desublimation process. After that, under the desublimation-controlled regime, the desublimation rate is weaker than the CO₂ supply. The injected CO₂ is not fully desublimated on the cylinder surface but flows out partially without phase change. Consequently, this yields the ineffective capture of the injected CO₂ (figure 10*b*). Finally, by comparison, the joint-controlled regime features relatively large capture capacity of CO₂, fast desublimation rate, high capture efficiency of the injected CO₂, and complete utilization of the cylinder surface. This regime is thus desirable in industrial applications. Note that the capture efficiency (η_c) does not reach the idealized value 1 because only one cylinder is considered in this work.

The above simulations have distinguished four desublimation regimes and demonstrated that the joint-controlled regime is favourable. To identify the desublimation regime for a wide range of ΔT_{sub} and Pe, values of the four metrics (ϕ_c , η_c , m_r^* and η_s) at the termination time instance t_e are plotted in figure 11. In cases with a relatively slow injection velocity (e.g. Pe = 1.1, 5.5), the decrease of ΔT_{sub} results in either a slight increase of the utilization of the cylinder surface or no increase at all (figure 11d). Furthermore, these cases demonstrate the relatively small CO_2 capture capacity (figure 11a) and the highly limited CO_2 desublimation rate (figure 11c). They are thus identified as the convection-controlled regime. On the other hand, as Pe increases to a larger value (e.g. Pe > 5.5), effects of ΔT_{sub} on CO₂ desublimation properties become different. Explicitly, with the decrease of ΔT_{sub} at fixed Pe, the CO₂ desublimation process is found to posses the higher CO_2 capture capacity (figure 11*a*), the smaller CO_2 capture ratio (figure 11b), and the larger utilization of the cylinder surface (figure 11d). Considering that the supplied CO_2 is almost unchanged for a given Pe, the decreased desublimation rate in relation to the decreasing ΔT_{sub} (figure 11c) plays an important role in this tendency. Accordingly, the desublimation process transfers from the diffusion-controlled regime, via the joint-controlled regime, to the desublimation-controlled regime. The discussion and comparison of CO₂ desublimation properties and SCL structures finally lead to the desublimation regime distribution in the parameter space spanned by ΔT_{sub} and *Pe* (figure 12). The boundary lines of different regimes are identified qualitatively. Based on this regime diagram, Pe is suggested to exceed a critical value (~ 0.5) to avoid the convection-controlled regime. Then, for a given Pe larger than the critical value, a moderate range of ΔT_{sub} can be identified for achieving the favourable joint-controlled regime. A relatively higher or lower ΔT_{sub} is not necessary due to the high cooling costs and the degraded CO_2 capture performance. In conclusion, the regime diagram can provide guidance on how to select operation conditions for an optimal desublimation process.

4.3. Three-dimensional results

In the above 2-D simulations, the cluster-style and dendritic-style SCLs are observed under the diffusion-controlled and joint-controlled regimes, respectively. These two porous SCLs may enlarge the gas–solid interface while blocking a part of the flue gas (or flow paths), thus affecting the CO_2 desublimation process. The complexities and effects of a porous

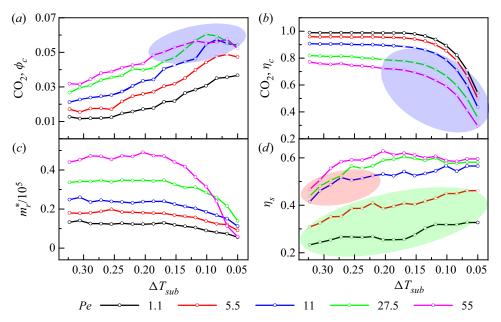
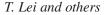


Figure 11. Analysis of CO₂ capture performance in cases with varying subcooling degrees ΔT_{sub} and Péclet numbers *Pe*. (*a*) The volume fraction of captured solid CO₂ (ϕ_c). (*b*) The capture efficiency of the injected CO₂ (η_c). (*c*) The overall desublimation rate (m_r^*). (*d*) The utilization of the cylinder surface (η_s).

SCL are expected to be different between two and three dimensions. Therefore, to verify the accuracy of the above 2-D simulations, CO₂ desublimation needs to be investigated in three dimensions. The 3-D simulation set-up is shown in figure 1. In order to render the results comparable, simulation parameters in three dimensions are set identical to those in two dimensions. Cases A-B are simulated to reflect the CO₂ desublimation properties under the four distinct regimes, with the corresponding ΔT_{sub} and *Pe* values being listed in table 1. The 3-D simulation results are then compared with those in two dimensions.

The corresponding 3-D results of cases Base and A1-A2 with Pe = 11 and $\Delta T_{sub} = 0.05, 0.17, 0.32$ are shown in figures 13(a)-13(c). Consistent with 2-D results, three desublimation regimes are identified. To be specific, as ΔT_{sub} decreases, the desublimation process changes from diffusion-controlled, via joint-controlled, to desublimation-controlled regimes. As explained above, this tendency is driven by the fact that the CO_2 desublimation rate declines and gradually becomes weaker than the supplied CO₂ via diffusion. Despite these similar regimes, SCLs in figures 13(a)-13(c)have 3-D structures that differ from 2-D cases. To quantify effects of these 3-D structures, temporal evolutions of four metrics (ϕ_c , η_c , m_r^* , η_s) are recorded and compared with 2-D results in figure 14. As can be seen, under the desublimation-controlled regime, 3-D profiles are consistent with 2-D ones. The dense and compact structure of the SCL plays an important role in this agreement. In contrast, curves of 3-D simulations differ from those in two dimensions under the joint-controlled and diffusion-controlled regimes. Explicitly, compared with 2-D simulations, the CO_2 desublimation process in three dimensions has a better CO_2 capture performance: faster desublimation rate, higher CO_2 capture ratio, and larger utilization of the cylinder surface. Under the joint-controlled and diffusion-controlled regimes, SCLs show dendritic and cluster-like structures, respectively. Two possible factors related to these pore structures help to explain the improved CO_2



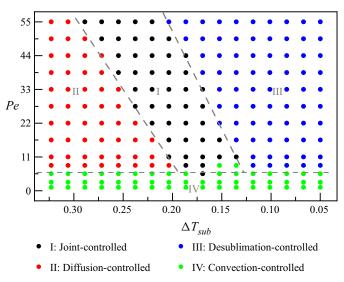


Figure 12. Analysis of CO₂ capture performance in cases with varying subcooling degrees ΔT_{sub} and Péclet numbers *Pe*. Data points of desublimation simulations plotted against ΔT_{sub} and *Pe*. The grey dashed lines divide the plane into four desublimation regimes: joint-controlled (I), diffusion-controlled (II), desublimation-controlled (III) and convection-controlled (IV).

desublimation process in three compared with two dimensions. First, the dendritic and cluster-like SCLs in three dimensions provide more gas–solid interface and solid CO₂ growth directions. To be specific, 9 and 17 growth directions are applied for 2-D and 3-D simulations, respectively. Second, the porous SCL expands flow paths in three dimensions, while it blocks flow channels in two dimensions.

As above, the corresponding 3-D cases B1-B2 with $\Delta T_{sub} = 0.17$ and Pe = 1.1, 11, 55 are simulated and compared with case Base. As shown in figures 13(a,d,e), three desublimation regimes are captured in the same vein as 2-D simulations. With the increase of Pe, CO₂ desublimation properties are determined by convection-controlled, joint-controlled and desublimation-controlled regimes, respectively. Similar to 2-D simulations, the intensified convection is considered as the major contributing factor to the transformation of desublimation regimes. To quantify the inconsistency between 2-D and 3-D simulations, temporal evolutions of ϕ_c , η_c , m_r^* and η_s are calculated. As plotted in figure 15, under the convection-controlled regime, the desublimation properties are quite similar in 2-D and 3-D simulations due to the dense SCL. Under the joint-controlled and convection-controlled regimes, however, the CO₂ desublimation process in three dimensions shows a faster desublimation rate and a better CO₂ capture performance than the process in two dimensions. Consistent with the above discussion, this difference is brought about by the dendritic and incomplete structures of the SCL.

Overall, both 2-D and 3-D simulations are able to capture the four desublimation regimes that represent different CO_2 desublimation properties and SCL structures. From quantitative comparisons, when the SCL is dense and compact, 2-D modelling reproduces well the results obtained in 3-D simulations. When it comes to porous SCLs (i.e. cluster-like, dendritic and incomplete structures), however, 3-D results show a faster and more efficient CO_2 desublimation process than 2-D results. This is due to the fact that 3-D simulations can describe the complex SCL structures more accurately. In addition, a

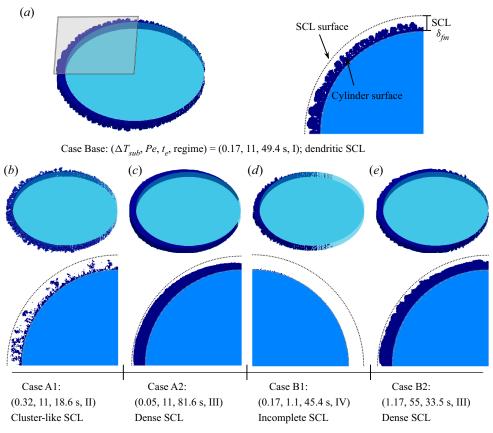


Figure 13. CO_2 desublimation properties in three dimensions. Contours of solid CO_2 and zoom-in views of SCL in cases (*a*) Base, (*b*) A1, (*c*) A2, (*d*) B1 and (*e*) B2. The four desublimation regimes are joint-controlled (I), diffusion-controlled (II), desublimation-controlled (III) and convection-controlled (IV).

drawback of 3-D simulations is that the computational cost is extremely high compared to 2-D studies. For example, to record numerically the CO₂ desublimation process in case Base until the termination time instant t_e , a 2-D simulation takes a 1.71 h parallel computation of 384 computing cores (i.e. 656.64 core-hours of computation), while a 3-D simulation spends 41.32 h of computational time using 2048 computing cores (i.e. 84 623.36 core-hours of computation). Therefore, 2-D simulations are suitable for the extensive exploration of different desublimation regimes, while 3-D simulations are a better choice for describing complex SCL structures.

5. Conclusions

In this work, a pore-scale multiple-relaxation-time lattice Boltzmann (LB) model is proposed and validated to simulate CO_2 desublimation during the cryogenic carbon capture (CCC) process. This novel LB model incorporates LB equations for solving the key physics behind CO_2 desublimation, including the unsteady fluid flow, species transport, conjugate heat transfer between the fluid and the solid phases, CO_2 desublimation kinetics at the gas–solid interface, and structural evolution of the solid CO_2 layer (SCL). These

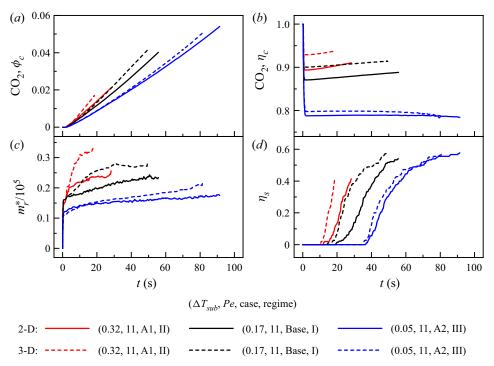


Figure 14. Comparison of CO₂ desublimation properties between 2-D and 3-D simulations for cases Base and A1-A2. (*a*) The volume fraction of captured solid CO₂ (ϕ_c). (*b*) The capture efficiency of injected CO₂ (η_c). (*c*) The overall desublimation rate (m_r^*). (*d*) The utilization of the cylinder surface (η_s). The three desublimation regimes are joint-controlled (I), diffusion-controlled (II) and desublimation-controlled (III).

physical processes, and their interactions are fully accounted for. Also, with the volume of pixel scheme, the intricate structure of the SCL was depicted at the pore scale.

Based on this model, the desublimation of CO₂ on the cooled cylinder surface is studied in both two and three dimensions with different operation conditions, namely, the gas injection velocity (Péclet number Pe) and the cylinder temperature (subcooling degree ΔT_{sub}). In 2-D simulations with different operation parameters, the CO₂ desublimation process shares similar characteristics: CO₂ desublimates on the cylinder surface and preferentially in the front surface area; injected CO₂ is captured to generate an SCL on the cylinder surface; and both heat and mass transfer are suppressed within the SCL. However, changes of Pe and ΔT_{sub} modify the gas diffusion rate, the gas convection rate and the CO₂ desublimation rate, which further bring about different pore structures of the SCL. Accordingly, four desublimation regimes are classified, depending on the relative strengths between the CO_2 supply (via gas diffusion and convection) and the CO_2 desublimation. On the one hand, with the decrease of ΔT_{sub} , the CO₂ desublimation rate decreases and gradually becomes weaker than the CO_2 supply via diffusion. As a consequence, the desublimated SCL transforms from cluster-like, via dendritic, to dense structures, which corresponds to the diffusion-controlled, joint-controlled and desublimation-controlled regimes, respectively. On the other hand, the increasing Pe represents the stronger convection and thus enhances the mass transport and the CO_2 supply. This then yields the incomplete, dendritic and dense structures of the SCL at the pore scale, corresponding to the convection-controlled, joint-controlled and desublimation-controlled

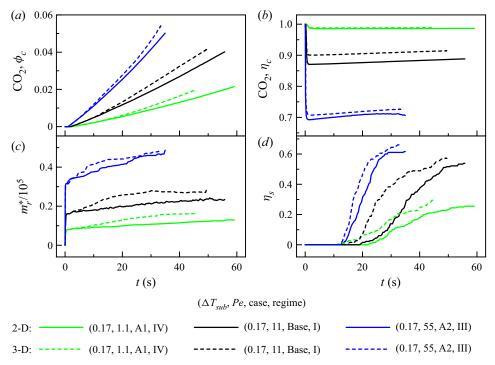


Figure 15. Comparison of CO₂ desublimation properties between 2-D and 3-D simulations for cases Base and B1-B2. (*a*) The volume fraction of captured solid CO₂ (ϕ_c). (*b*) The capture efficiency of injected CO₂ (η_c). (*c*) The overall desublimation rate (m_r^*). (*d*) The utilization of the cylinder surface (η_s). The three desublimation regimes are joint-controlled (I), desublimation-controlled (III) and convection-controlled (IV).

regimes, respectively. Under the four classified desublimation regimes, CO₂ capture performances are recorded and compared quantitatively. The CO_2 desublimation process under the joint-controlled regime is found to possess a relatively fast CO₂ desublimation rate, large CO₂ capture capacity and efficiency, and complete cylinder surface utilization. The joint-controlled regime is thus considered to be desirable for separating CO_2 from the flue gas. Moreover, 3-D simulations are conducted to investigate the CO₂ desublimation properties and the CO_2 capture performances, which are in the same vein as 2-D studies but at significantly higher computational costs. The analysis of quantitative metrics shows that under the desublimation-controlled regime with a dense SCL, CO_2 desublimation properties in two and three dimensions are almost the same. However, under the other regimes with cluster-like, dendritic and incomplete SCLs, the CO₂ desublimation process becomes faster and more efficient in three compared to two dimensions. The improved CO₂ desublimation performance is attributed to the more gas-solid interface and flow paths in three dimensions. To conclude, the newly proposed LB model has proven capability to capture CO₂ desublimation properties under various operating conditions. The simulation results provide new and important insights into the desublimation-based CCC process, which is an alternative and promising method for mitigating climate change.

As the first pore-scale study of CO_2 desublimation using the LB method, this work focuses on investigating the CO_2 desublimation properties on a single packing cylinder. In practical applications, however, a cryogenic packed bed usually consists of multiple packing cylinders, with potential interferences between them. The multiple cylinders are expected to influence the desublimation process. For example, the multiple cylinders may

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affect the temperature distribution because the thermophysical parameters between the gas and the solid phases are different. The cylinders may also modify the flow channels and subsequently affect the gas flow. These changes in temperature and flow distributions will influence the CO_2 desublimation properties and also the parameter ranges for different desublimation regimes. Also, some narrow channels may be blocked by the accumulated SCL, hence causing operational risks. Therefore, it is necessary to investigate effects of the packed bed design, including the size, number, material and geometrical position of packing cylinders, in a follow-on study.

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Appendix A. Transformation details in the MRT model

In the proposed D2Q9 and D3Q15 LB models for simulating CO₂ desublimation, the corresponding discrete velocities e_i and the weight coefficients w_i are set as (Guo & Shu 2013)

D2Q9,
$$\boldsymbol{e}_i = e \begin{bmatrix} 0 & 1 & 0 & -1 & 0 & 1 & -1 & -1 & 1 \\ 0 & 0 & 1 & 0 & -1 & 1 & 1 & -1 & -1 \end{bmatrix}$$
, (A1)

D2Q9,
$$w_i = \begin{cases} 4/9, & i = 0, \\ 1/9, & i = 1-4, \\ 1/36, & i = 5-8, \end{cases}$$
 D3Q15, $w_i = \begin{cases} 2/9, & i = 0, \\ 1/9, & i = 1-6, \\ 1/72, & i = 7-14. \end{cases}$ (A3*a*,*b*)

Also, values of the transformation matrix M in D2Q9 and D3Q15 LB models are (Guo & Shu 2013)

The transformation matrix \mathbf{M} maps the distribution functions from the physical space $\boldsymbol{\psi}$ to the moment space as $\hat{\boldsymbol{\psi}} = \mathbf{M} \cdot \boldsymbol{\psi}$. With this transformation, the evolution equations (3.3)–(3.5) are implemented in the moment space as

$$\hat{f}(\boldsymbol{x} + \boldsymbol{e}_i \delta_t, t + \delta_t) = \hat{f}(\boldsymbol{x}, t) - \boldsymbol{S} \Big[\hat{f}(\boldsymbol{x}, t) - \hat{f}^{eq}(\boldsymbol{x}, t) \Big],$$
(A6)

$$\hat{\boldsymbol{g}}\left(\boldsymbol{x} + \boldsymbol{e}_{l}\boldsymbol{\delta}_{l}, t + \boldsymbol{\delta}_{l}\right) = \hat{\boldsymbol{g}}\left(\boldsymbol{x}, t\right) - \boldsymbol{S}_{y}\left[\hat{\boldsymbol{g}}\left(\boldsymbol{x}, t\right) - \hat{\boldsymbol{g}}^{eq}\left(\boldsymbol{x}, t\right)\right],\tag{A7}$$

$$\hat{\boldsymbol{h}}\left(\boldsymbol{x}+\boldsymbol{e}_{i}\boldsymbol{\delta}_{t},t+\boldsymbol{\delta}_{t}\right)=\hat{\boldsymbol{h}}\left(\boldsymbol{x},t\right)-\boldsymbol{S}_{t}\left[\hat{\boldsymbol{h}}\left(\boldsymbol{x},t\right)-\hat{\boldsymbol{h}}^{eq}\left(\boldsymbol{x},t\right)\right]+\boldsymbol{\delta}_{t}\hat{\boldsymbol{F}}_{T}+0.5\boldsymbol{\delta}_{t}^{2}\boldsymbol{\partial}_{t}\hat{\boldsymbol{F}}_{T}.$$
(A8)

Through the Chapman–Enskog analysis on the proposed LB equations, the governing equations can be recovered with relaxation times τ , τ_y and τ_t as

$$\nu = c_s^2 (\tau - 0.5)\delta_t, \quad D = c_s^2 (\tau_y - 0.5)\delta_t, \quad \alpha = c_s^2 (\tau_t - 0.5)\delta_t, \quad (A9a-c)$$

as well as the gradient terms of temperature (∇T) as (Lei, Meng & Guo 2017; Lei *et al.* 2021)

$$\nabla_x T = -\frac{\hat{h}_3 - Tu + 0.5\delta_t F_T u}{c_s^2 \tau_t \delta_t}, \quad \nabla_y T = -\frac{\hat{h}_5 - Tv + 0.5\delta_t F_T v}{c_s^2 \tau_t \delta_t}.$$
 (A10*a*,*b*)

Except for these calculations, the other gradient term in (3.2a-c) is determined using the isotropic central scheme as (Guo, Zheng & Shi 2011)

$$\nabla(\rho c_p) = \sum_{i} \frac{w_i e_i \rho c_p \left(x + e_i \delta_t\right)}{c_s^2 \delta_t}.$$
(A11)

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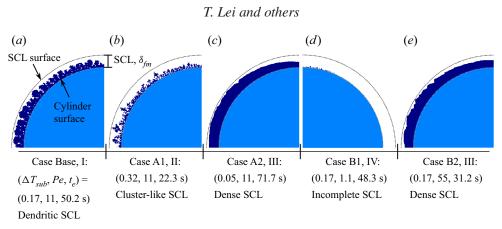


Figure 16. Sensitivity tests of R_{dp} . Zoom-in views of SCL in cases (*a*) Base, (*b*) A1, (*c*) A2, (*d*) B1 and (*e*) B2, with the desublimation probability ratio $R_{dp} = 1 : 1$. The four desublimation regimes are joint-controlled (I), diffusion-controlled (II), desublimation-controlled (III) and convection-controlled (IV).

Appendix B. Sensitivity tests of desublimation probability ratio R_{dp}

In the present model, the ratio of the desublimation probability between the nearest and the diagonal grid nodes (R_{dp}) affects the intricate structure of the SCL at the pore scale. In order to test the sensitivity of CO₂ desublimation properties to the selection of R_{dp} , simulations with different values of R_{dp} are performed and compared. Considering the distance between two grid nodes, the desublimation probability in the nearest-grid direction should be larger than or equal to that in the diagonal-grid direction. Therefore, four values of R_{dp} are considered in 2-D simulations: $R_{dp} = 1 : 0.25, 1 : 0.50, 1 : 0.75, 1 :$ 1. After simulations and comparisons under varying operation conditions (i.e. subcooling degree ΔT_{sub} and Péclet number Pe), the CO₂ desublimation process at each given R_{dp} is found to show the same desublimation properties as discussed in § 4.

As an example, figures 16 and 17 provide the simulated SCL structures and the CO₂ desublimation properties, including the captured solid CO₂ (ϕ_c), the overall desublimation rate (m_r^*), the capture efficiency of the injected CO₂ (η_c), and the utilization of the cylinder surface (η_s). Consistent with cases at $R_{dp} = 1 : 0.25$ in § 4, four desublimation regimes are classified. As ΔT_{sub} decreases from case A1 via Base to A2, SCL becomes dense and the desublimation process changes from diffusion-controlled, via joint-controlled, to desublimation-controlled regimes. In the meantime, with the increase of *Pe* from case B1 via Base to B2, fluid convection becomes intensified and the system transfers from convection-controlled, via joint-controlled, to desublimation-controlled, via joint-controlled, to desublimation-controlled regimes.

To further quantify the sensitivity of CO₂ desublimation properties to R_{dp} , temporal evolutions of the four desublimation metrics (i.e. ϕ_c , m_r^* , η_c and η_s) are compared for case Base at $R_{dp} = 1 : 0.25, 1 : 0.50, 1 : 0.75, 1 : 1$. As displayed in figure 18, with the decrease of R_{dp} , values of the captured CO₂ (ϕ_c , η_c), the desublimation rate (m_r^*) and the cylinder utilization (η_s) increase slightly, hence the improved CO₂ capture performance. However, such an improvement is insignificant, and curves for $R_{dp} = 1 : 0.50, 1 : 0.75, 1 : 1$ are in good agreement with those for $R_{dp} = 1 : 0.25$.

In general, similar desublimation regimes and CO₂ desublimation properties can be produced at each given R_{dp} . Meanwhile, under a certain operation condition, the simulated CO₂ desublimation properties at different values of R_{dp} match well with each other. Therefore, the reliability of the present findings at the selected R_{dp} has been verified.

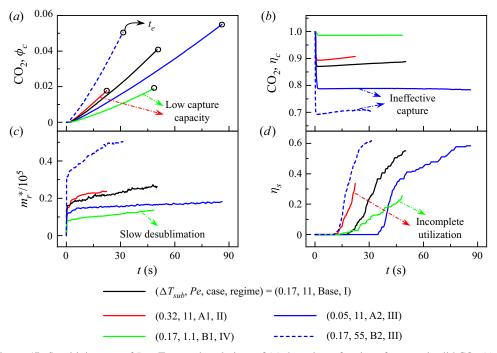


Figure 17. Sensitivity tests of R_{dp} . Temporal evolutions of (*a*) the volume fraction of captured solid CO₂ (ϕ_c), (*b*) the capture efficiency of injected CO₂ (η_c), (*c*) the overall desublimation rate (m_r^*) and (*d*) the utilization of cylinder surface (η_s) in cases Base, A1-A2 and B1-B2, with the desublimation probability ratio $R_{dp} = 1 : 1$. The four desublimation regimes are joint-controlled (I), diffusion-controlled (II), desublimation-controlled (III) and convection-controlled (IV).

Appendix C. Model validation

To validate the proposed MRT LB model, simulations of two cases are carried out in this appendix. The first case focuses on the desublimation of CO_2 over a single packing grain immersed in the quiescent flue gas. The modelled thickness of desublimated CO_2 on the packing surface is recorded versus time, which is then compared with results from the GERAs algorithm (ode15s library function of MATLAB 2009b software; Debnath *et al.* 2019). The second case is conducted to study CO_2 desublimation in a cryogenic packed bed, with the flue gas flow being considered. Temporal evolutions of the outgoing CO_2 content are simulated and compared with experimental measurements (Ali *et al.* 2014). By performing these two cases, the reliability of the present LB model for simulating CO_2 desublimation on the cooled surface can be verified.

C.1. CO_2 desublimation over a single packing

The desublimation of CO₂ on the surface of a single packing grain is first simulated to test the capability of the proposed LB model. As displayed in figure 19(*a*), the computational domain is $0 \le x \le l_x$ and $0 \le x \le l_y$. A solid packing grain is fixed in the centre of the domain, and the remaining void space is filled with flue gas. The four boundaries of the domain are set as periodic. In order to produce results comparable to those by Debnath *et al.* (2019), the same simulation parameters are set: diameter of the packing grain is $l_d = 0.01$ m, porosity is 0.637, initial flue gas temperature is $T_0 = 303$ K, initial packing

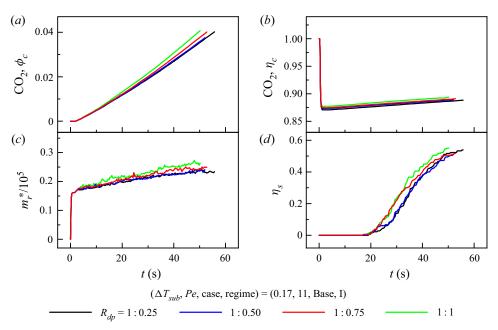


Figure 18. Sensitivity tests of R_{dp} . Temporal evolutions of (*a*) the volume fraction of captured solid CO₂ (ϕ_c), (*b*) the capture efficiency of injected CO₂ (η_c), (*c*) the overall desublimation rate (m_r^*) and (*d*) the utilization of cylinder surface (η_s) in case Base, with four desublimation probability ratios $R_{dp} = 1 : 0.25, 1 : 0.50, 1 : 0.75, 1 : 1$. The desublimation regime I is the joint-controlled regime.

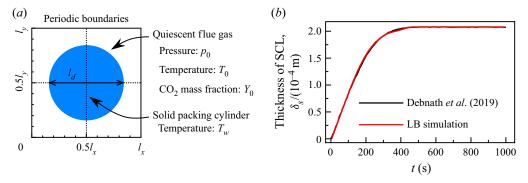


Figure 19. Validation case of CO_2 desublimation over a single packing immersed in the quiescent flue gas. (*a*) Computational domain and boundary conditions. (*b*) Comparing temporal evolutions of SCL thickness between the present LB simulations and simulations in Debnath *et al.* (2019).

temperature is $T_w = 155$ K, CO₂ mass fraction is $Y_0 = 1$, and gas pressure is $p_0 = 3$ atm. The thermophysical properties of the gas and solid phases are set as in § 4. Once the flue gas encounters the cooled packing, CO₂ desublimates to generate an SCL on the packing surface. Here, the flue gas is assumed to be quiescent, which depicts the growth of the SCL for a large exposure time of the flue gas with the packing grain (Debnath *et al.* 2019). In this case, a mesh of size 640 × 640 is used.

The calculated thickness of the SCL is recorded versus time and plotted in figure 19(b), where the numerical data reported by Debnath *et al.* (2019) are included for comparison.

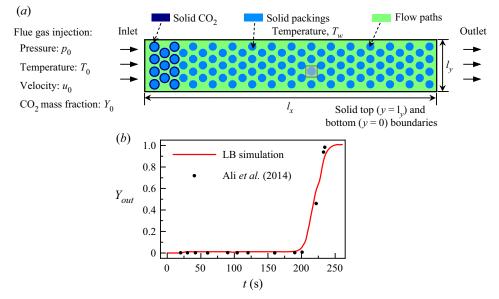


Figure 20. Validation case of CO_2 desublimation in a cryogenic packed with flue gas feed flow. (*a*) Computational domain and boundary conditions. (*b*) Comparison of the outgoing CO_2 content between the present LB results and experimental measurements in Ali *et al.* (2014).

As can be seen, our simulation results agree well with those from Debnath *et al.* (2019), indicating the reliability of our developed LB model in simulating CO_2 desublimation.

C.2. CO₂ desublimation in a cryogenic packed bed

The present MRT LB model has been shown to be capable of tracking dynamically the growth of the SCL on the cooled surface of a packing grain. Nevertheless, the gas feed flow and the multiple packing grains were not considered. To fill this gap, this subsection further introduces a cryogenic bed as shown in figure 20(a), which is packed with multiple grains and fed with a flue gas flow from the left inlet. Based on such a system, CO₂ desublimation is simulated and compared with experiments by Ali *et al.* (2014) to examine the reliability of the present MRT LB model. In this case, the computational domain is $0 \le x \le l_x$ and $0 \le x \le l_y$. From the left inlet, the flue gas is injected into the domain at the initial condition (T_0, Y_0, u_0, p_0) . The injected CO₂ deposits on the surface of cooled packing grains. Once the bed reaches saturation, the injected CO₂ leaves the domain from the right outlet without phase change. The outgoing CO₂ content at the outlet has been measured and compared with experimental data (Ali *et al.* 2014).

We simulate the case based on the countercurrent flow configuration in § 3.1 of Ali *et al.* (2014), for which the same desublimation conditions and parameters are selected. To be specific, bed size is $l_x = 0.46$ m and $l_y = 0.0418$ m, porosity is 0.637, inlet flue gas temperature is $T_0 = 293$ K, inlet CO₂ mass fraction is $Y_0 = 1$, and gas pressure is $p_0 = 1$ atm. The initial bed temperature T_w decreases from the inlet to the outlet. The thermophysical properties of the gas and solid phases are set as in our simulations in § 4. A mesh of size 640×7040 is utilized here.

Under this simulation set-up, the calculated CO_2 mass fraction at the outlet is depicted versus time in figure 20(*b*), along with the experimental data by Ali *et al.* (2014) for comparison. This shows that at first, the injected CO_2 is fully captured by packing grains

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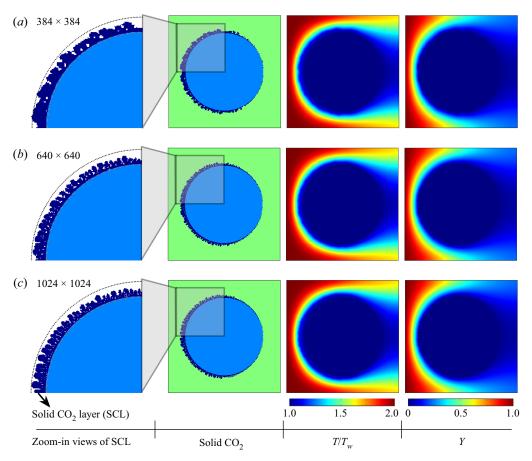


Figure 21. Grid convergence test. Contours of solid CO₂, temperature (*T*) and CO₂ mass fraction (*Y*) at t = 55.8 s in case Base with three grid resolutions: (*a*) 384×384 , (*b*) 640×640 and (*c*) 1024×1024 . Zoom-in views of the SCL in highlighted grey rectangles are provided.

and the outgoing CO_2 content remains zero. After this CO_2 capture period, the bed gradually becomes saturated with solid CO_2 , and the breakthrough of the injected CO_2 is observed at the outlet. Subsequently, the value of outgoing CO_2 content increases rapidly and finally reaches the feed composition. This trend matches well with the experimental data. Thus the present LB model is accurate for simulating CO_2 desublimation on the cooled surface during the cryogenic CO_2 capture.

Appendix D. Grid convergence tests

We perform grid-independence simulations of CO_2 desublimation on a cooled cylinder surface. Three different grids (384 × 384, 640 × 640, 1024 × 1024) are tested. As an illustration, simulation results in case Base (see table 1) are provided and discussed. The calculated contours of CO_2 mass fraction, temperature, solid CO_2 and zoom-in views at the time instant 55.8 s are provided in figure 21. All these contours under different grid resolutions show similar desublimation properties. That is, the SCL grows on the packing surface, the strong desublimation takes place in the front surface area, the injected CO_2 is effectively captured by the packing grain, and the SCL suppresses heat and mass transfer

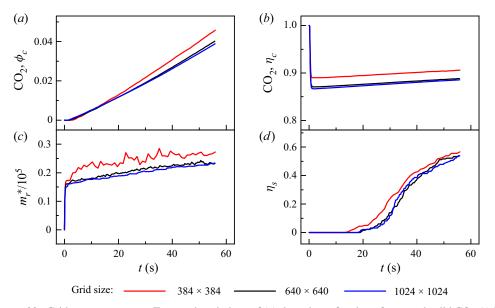


Figure 22. Grid convergence test. Temporal evolutions of (*a*) the volume fraction of captured solid CO₂ (ϕ_c), (*b*) the capture efficiency of injected CO₂ (η_c), (*c*) the overall desublimation rate (m_r^*) and (*d*) the utilization of cylinder surface (η_s), in case Base with three grid resolutions.

within it. On the other hand, inconsistencies between three tests are observed: the coarse grid (384×384) fails to describe the intricate structure of the SCL at the pore scale. Specifically, the dendritic structure is captured by grids 640×640 and 1024×1024 , while the SCL consists of large bumps but not distinct branches under the 384×384 coarse grid.

After the above qualitative observations, temporal evolutions of four metrics are compared quantitatively in figure 22. That includes the volume fraction of the captured solid CO₂ (ϕ_c), the overall desublimation rate (m_r^*), the capture efficiency of the injected CO₂ (η_c), and the utilization of the cylinder surface (η_s). Profiles of these four metrics demonstrate similar tendencies. In addition, results by grids 640 × 640 and 1024 × 1024 match well with each other but show slight discrepancies from those by the 384 × 384 coarse grid. That is, the 384 × 384 grid leads to the faster desublimation process and the slightly over-predicted CO₂ capture performance. These comparisons suggest that the grid of size 640 × 640 is fine enough to obtain grid-independent results. Thus simulations in this work are conducted with the 640 × 640 grid.

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