A whole-genome analysis using robust asymmetric distributions

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Summary

This study is aimed at improving the analysis of data used in identifying marker-associated effects on quantitative traits, specifically to account for possible departures from a Gaussian distribution of the trait data and to allow for asymmetry of marker effects attributable to phenotypic divergence between parental lines. A Bayesian procedure for analysing marker effects at the whole-genome level is presented. The procedure adopts a skewed *t*-distribution as a prior distribution of marker effects. The model with the skewed *t*-process includes Gaussian prior distributions, skewed Gaussian prior distributions and symmetric *t*-distributions as special cases. A Markov Chain Monte Carlo algorithm for obtaining marginal posterior distributions of the unknowns is also presented. The method was applied to a dataset on three traits (live weight, carcass length and backfat depth) measured in an F₂ cross between Iberian and Landrace pigs. The distribution of marker effects was clearly asymmetric for carcass length and backfat depth, whereas it was symmetric for live weight. The *t*-distribution seems more appropriate for describing the distribution of marker effects on backfat depth.

1. Introduction

Recent development of molecular techniques has provided a massive number of molecular markers and, as a consequence, dense genetic maps are now available for a number of species. An obvious use of this molecular information is for marker-assisted selection in livestock and plant populations (Whittaker, 2001). The basic idea of marker-assisted selection is to detect and exploit linkage disequilibrium between mutations that cause genetic variations and presumably neutral molecular markers.

Over the last decade, many quantitative trait loci (QTL) mapping experiments have been performed to detect regions of the genome involved in genetic regulation of quantitative traits (Pe *et al.*, 1993; Devicente *et al.*, 1993; Andersson *et al.*, 1994). In these studies, statistical analyses were usually carried

out via a genomic scan using likelihood (Lander & Botstein, 1989) or regression techniques (Haley *et al.*, 1994). With these approaches, the model of analysis allows for one or a few genome locations at a time.

Recently some authors have proposed the combined use of all available markers. For instance, Whittaker (2001) and Lange & Whittaker (2001) proposed ridge regression methods, while Gianola *et al.* (2003) and Xu (2003) developed Bayesian approaches. The procedures of Gianola *et al.* (2003) and Xu (2003) employ prior Gaussian distributions for effects associated with molecular markers. Mekkawy (2005) compared the two procedures by simulation, and showed that the method of Gianola *et al.* (2003) produced better predictions of genetic merit.

However, the assumption of a prior Gaussian distribution, common to both Gianola *et al.* (2003) and Xu (2003), for effects associated with molecular markers may be unrealistic if some of the markers are associated with major effects. Therefore, it is possible that a more robust distribution, such as a

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t-distribution, could be more appropriate (Lange *et al.*, 1989) as prior. Further, asymmetric distributions (Fernandez & Steel, 1998) may provide a more flexible prior for effects associated with genetic markers.

The objective of this paper is to describe a procedure based on Gianola *et al.* (2003), but with robust asymmetric prior distributions instead, and to evaluate its performance in a case involving data from a crossing experiment with Iberian and Landrace pigs.

2. Asymmetric robust distribution

Under the assumption of prior independence between markers, Gianola *et al.* (2003) assume the following Gaussian prior distribution for additive marker effects:

$$f(\mathbf{q}|\sigma_q^2) = \prod_{i=1}^n \frac{1}{\sqrt{2\pi\sigma_q^2}} \exp\left[-\frac{q_i^2}{2\sigma_q^2}\right]$$

where $\mathbf{q} = \{q_i\}$ is the vector of additive genetic marker effects, σ_q^2 is the variance of the additive genetic marker effects and n is the number of markers.

Here, we present an alternative prior distribution following Fernandez & Steel (1998), with density:

$$f(\mathbf{q}|\sigma_q^2, \gamma) = \prod_{i=1}^n \frac{1}{\gamma + \frac{1}{\gamma}} \left\{ f(\frac{q_i}{\gamma}) I_{[\mathbf{0}, \infty)}(q_i) + f(q_i \gamma) I_{(-\infty, \mathbf{0}]}(q_i) \right\}$$

$$\tag{1}$$

where γ is the asymmetry parameter, and f(x) is the following univariate t-density:

$$f(x) = \frac{\Gamma\left[\frac{1}{2}(\nu+1)\right]}{\sigma_q \sqrt{\nu \pi} \Gamma\left(\frac{1}{2}\nu\right)} \left(1 + \frac{x^2}{\nu \sigma_q^2}\right)^{\frac{-(\nu+1)}{2}} \tag{2}$$

with v representing the degrees of freedom parameter of the t-distribution.

3. Application

(i) Experimental design

Three Iberian boars from the genetically isolated Guadyerbas line (Toro *et al.*, 2000) were mated with 31 non-inbred Landrace sows. Six boars and 73 sows from their offspring, generation F_1 , were the parents of 577 F_2 animals. The Iberian pig is characterized by its extremely fat body composition. Landrace animals were the maternal line used at Nova Genetica S. A. experimental farm. The two parental lines differ substantially in growth, carcass and meat quality traits (Serra *et al.*, 1998).

The F₂ pigs were raised under standard intensive conditions on the experimental farm Nova Genetica.

Feeding was *ad libitum*, and males were not castrated. A total of 321 individuals from 58 full-sib families were recorded for carcass weight, carcass length and backfat depth. The average (\pm SD) age at slaughter was $175 \cdot 5 \pm 5 \cdot 5$ days. Average (\pm SD) carcass weight, carcass length and backfat depth were $74 \cdot 9 \pm 9 \cdot 82$ kg., $79 \cdot 26 \pm 3 \cdot 96$ cm and $28 \cdot 31 \pm 7 \cdot 90$ mm, respectively.

(ii) Genotyping

DNA of parent animals was extracted from blood using a saline precipitation protocol, and DNA from F₁ and F₂ pigs was extracted using a commercial protocol (Boehringer Mannheim). Animals were genotyped for 92 markers (90 microsatellites and 2 PCR-RFLP), chosen to provide highly informative input based on the index of Ron et al. (1995). A broad description of the markers is presented in Table 1. Markers provided a uniform coverage of the 18 autosomes. PCRs were carried out in a MJ Research Thermal Cycler. The microsatellite PCR products were analysed with Genescan software on capillary electrophoresis equipment with fluorescence detection (ABI PRIMS 310 Genetic Analyzer). Genotypes were stored in the Gemma database (Iannucelli et al., 1996).

(iii) Statistical analysis

Statistical analysis of carcass weight, carcass length and backfat depth for the F₂ population was carried out using univariate Bayesian methods. The likelihood of the data given the parameters of the model was

$$\begin{split} f(\mathbf{y}|\pmb{\beta},\mathbf{q},\sigma_e^2,\mathbf{M}) \\ \propto \frac{1}{\sigma_e^{n_d}} \exp\left[-\frac{(\mathbf{y}\!-\!\mathbf{X}\pmb{\beta}\!-\!\mathbf{M}\mathbf{q})'(\mathbf{y}\!-\!\mathbf{X}\pmb{\beta}\!-\!\mathbf{M}\mathbf{q})}{2\sigma_e^2}\right] \end{split}$$

where \mathbf{y} is the vector of data (321 records); $\boldsymbol{\beta}$ is the vector of systematic effects (2 levels for sex, 58 levels for family, and a regression on age of slaughter); \mathbf{q} is the vector of additive effects associated with the markers (92 levels); \mathbf{X} is an incidence matrix relating the systematic effects to the data; \mathbf{M} is an unknown incidence matrix relating the additive marker effects to the data; σ_e^2 is the residual variance; and n_d is the number of data points.

The incidence matrix \mathbf{M} is an n_d (number of data points) $\times n_m$ (number of markers) random matrix, with entries equal to 1, 0 or -1, depending on whether the two alleles were of Iberian origin (1), one was Iberian and the other was a Landrace allele (0), or both were Landrace alleles (-1). The prior distribution of the matrix was determined by the probability of origin given the marker data ($f(\mathbf{M}|\mathbf{M}ks)$), which was calculated using the algorithm

Chr IC IC Marker Pos IC Chr Marker Pos Chr Marker Pos 1 SW1515 0.53S0143 0.780.06 S0035 0.00.6512 0.0**CGA** 30.1 0.99SW1057 44.3 0.96GH 31.4 0.710.5757.7 SW874 0.98S0113 46.2 S0087 1.00 48.6 S0155 55.0 0.78SW316 81.2 0.90S0106 81.7 0.790.48SW1828 85.0 0.85S0228 96.0 0.57 13 S0219 0.0108.7 SW1881 0.82SW935 30.9 0.542 0.00.70IGF2 SW2419 145.30.96SWR100 64.00.97S0141 30.3 0.937 0.0 SW398 0.96S0025 0.7381.4 SW240 41.8 0.980.76SW1056 91.2 0.41S0064 40.1 SW395 64.70.95**TNFB** 68.9 0.93 SW769 121.5 0.580.99S0226 72.4 S0066 87.8 0.99SW857 0.00.8914 S0378 87.0 0.93SW632 111.9 0.94SW1125 18.8 0.92**SWR308** 130.1 1.00 137.7 S0101 0.92SW210 42.2 0.82SW72 0.01.00 3 SW764 160.3 0.94 55.8 0.87S0007 S0206 25.6 0.518 SW2410 0.00.98 SW1557 90.80.43S0216 55.1 1.00 114.00.75SW905 26.00.60SW2515 77.5 S0002 0.72SWR110 44.7 1.00 15 SW919 0.01.00 Sw349 86.0 0.990.98S0017 66.5 SW1111 0.56 16.3 S0225 0.8386.1 4 SW2404 0.0 0.80S0149 38.3 1.00 SW61 109.1 1.00 SW936 0.850.8556.0 S0301 40.879.9 0.45SW1119 9 S0001 59.5 0.88SW983 0.00.99 $72 \cdot 8$ SW839 1.00 SW911 31.1 0.710.0SW742 0.9916 DECR2 78.8 0.18SW2571 79.5 0.73S0298 18.4 0.4495.1 SW2517 S0214 1.00 SW2093 109.2 0.9935.9 1.00 SW445 116.8 1.00 SW1349 160.9 0.7669.4 0.37S0061 S0097 134.4 0.8410 S0038 0.00.7417 SW24 0.01.00 45.5 S0070 0.82SW1920 28.3 0.950.98 5 SW413 0.00.97 SW1626 100.5SW2431 72.2 0.51SW2425 66.1 0.5011 S0385 0.00.8718 SW1023 0.00.85S0005 81.8 1.00 SW787 21.5 0.84IGF1 113.8 0.91S0071 43.1 0.75

SW703

 $72 \cdot 3$

1.00

Table 1. Marker positions (Pos) and information content (IC) at position sorted by chromosome (Chr)

described by Haley et al. (1994); Mks stands for markers.

0.95

130.9

The prior distribution of the additive marker effects was as described in the previous section in expressions (1) and (2). In addition, the prior distribution for systematic effects (β) was:

$$f(\beta|\beta^0,\sigma_\beta) = N(1\beta^0, \mathbf{I}\sigma_\beta)$$

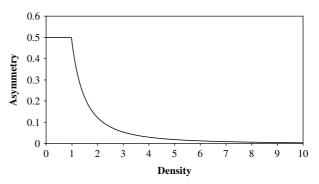
SWR111

where $1 \ \beta^0$ is the vector of prior means for the systematic effects, (1 is an $n_m \times 1$ vector of ones) and σ_{β} is the prior standard deviation. Here, β^0 was set to 0, and σ_{β} was set to 10^6 . Prior distributions of the variance components (σ_e^2 and σ_q^2) were set to

$$f(\sigma_e^2) = \chi^{-2}(\nu_e, s_e^2)$$

$$f(\sigma_q^2) = \chi^{-2}(\nu_q, s_q^2)$$

with $v_e = v_q = 0$, and $s_e^2 = s_q^2 = -2$, thus yielding uniform distributions. In addition, the prior distribution of the degrees of freedom of the *t*-distribution (*v*) was flat between 1 and 100. Finally, the prior distribution of the asymmetry parameter (γ) was assumed to be uniform between 0 and 1 with density of 0·5, and with



S0120

35.1

1.00

Fig. 1. Prior density of the asymmetry parameter (γ) .

a density of $\frac{0.5}{\gamma^2}$ for values over 1. This distribution assigns an equal probability (0.5) to values below and over 1, and it is invariant with respect to an arbitrary choice of the sign of the genetic effects favouring the Landrace or the Iberian line. This prior distribution is presented in Fig. 1.

(iv) Markov Chain Monte Carlo algorithm

A Gibbs sampling procedure (Gelfand & Smith, 1990) was performed to obtain samples from marginal

posterior distributions of the parameters. The Gibbs sampling procedure involves an updating sampling scheme of the fully conditional distributions of all unknown parameters involved in the model. Here, the conditional distributions of each level of the systematic effects was univariate normal, and the conditional distribution of the residual variance (σ_e^2) was a scale inverted chi-square distribution. Sampling of elements of the random incidence matrix (**M**) was performed by drawing each element from a discrete probability distribution in the following way:

$$p(M_{ij} = k | \beta, \mathbf{q}, \sigma_e^2, \mathbf{y}, Mks)$$

$$= \frac{f(\mathbf{y} | \beta, \mathbf{q}, \sigma_e^2, M_{ij} = k) f(M_{ij} = k | Mks)}{\sum_{k=-1,0,1} f(\mathbf{y} | \beta, \mathbf{q}, \sigma_e^2, M_{ij} = k) f(M_{ij} = k | Mks)}$$

where $f(M_{ij}=k|\beta,\mathbf{q},\sigma_e^2,\mathbf{y})$ is the conditional distribution of the elements of $\mathbf{M}=\{-1,0,1\}$ given the data, systematic and marker effects and the residual variance. In contrast, sampling from the conditional distribution for each level of the marker effects (q_i) , the variance of the marker effects (σ_q^2) , the asymmetry parameter (γ) and the degrees of freedom of the t-distribution (ν) was performed using a Metropolis–Hastings algorithm (Hastings, 1970) with a uniform proposal distribution with a range of 10 units around the value of the previous iteration.

Based on output from the Gibbs sampler, the percentage of variance explained by the marker effects (h_a^2) was calculated as

$$h_q^2 = \frac{\sum_{i=1}^{n_m} 0.5q_i^2}{\sum_{i=1}^{n_m} 0.5q_i^2 + \sigma_e^2}$$

since the additive variance explained by the *i*th marker is $0.5q_i^2$.

We also calculated an 'empirical marginal prior' distribution of the *i*th marker effect evaluated by averaging the conditional prior distributions in (1) over the posterior samples for σ_q^2 and γ at each iteration by using the Rao-Blackwell argument:

$$f(q_i) = \sum_{j}^{niter} f(q_i | \sigma_{q_j}^2, \gamma_j) / niter.$$

Above, *niter* is the total number of iterations after convergence, and σ_{qj}^2 and γ_j are the variance of the additive genetic marker effects and the asymmetry parameter, respectively, sampled in the *j*th iteration. The objective of this empirical marginal prior distribution is to represent the prior influence on the marker effects.

The Gibbs sampling analysis was performed by running 110 000 iterations, with the first 10 000 discarded as burn-in. Convergence was checked using the CODA software (Best *et al.*, 1995). All 100 000 samples were used for extracting posterior features.

4. Results

(i) Live weight

The distribution of posterior means of additive marker effects with the Gaussian and the asymmetric t prior distributions for live weight are presented in Fig. 2 (top panel). The most extreme effect was the -1.01 kg associated with marker SW24 in SSC17. The mean of the posterior distribution of the asymmetry parameter (γ) was 1.00, and the posterior standard deviation was 0.08 (Fig. 3, top panel). These results imply that the probability mass below 0 in the empirical marginal prior distribution of the marker effects was 0.50, as can be observed in Fig. 4 (top panel). In addition, the posterior mode of the degrees of freedom of the t-distribution was 16, and the probability that the degrees of freedom were larger than 30 was 52.59 % (Fig. 5, top panel). Moreover, the posterior mean estimate of the variance pertaining to the effects associated with the markers was 0.411 (0.144), and the posterior mean estimate of residual variance was 45.64 (4.63). Finally, the posterior mean of the proportion of variance explained by the markers in the F_2 population was 0.441 (0.094).

(ii) Carcass length

Results for posterior mean estimates of the additive marker effects with the Gaussian and asymmetric t prior distributions on carcass length are presented in Fig. 2 (centre panel). The effects with the highest absolute values were associated with markers S0001 (-0.28 cm), SW2571 (-0.31 cm) and SW24(-0.40 cm), located in SSC4, SSC9 and SSC17, respectively. The posterior distribution of γ for carcass length is presented in Fig. 3 (centre panel), and had a mean of 1.27 and a standard deviation of 0.15. The posterior probability of γ being below 1.00 was only 1.02%. These results imply that the probability mass below 0 in the empirical marginal prior distribution of the marker effects was 0.61 (Fig. 4, centre panel). In addition, the posterior distribution of the degrees of freedom of the t-distribution had a mode at 13, and the posterior probability of degrees of freedom being greater than 30 was 45.26% (Fig. 5, centre panel). The posterior mean estimate of the variance of the effects associated with the markers was 0.026 (0.014) and the posterior mean estimate of the residual variance was 4.59 (0.48). The posterior mean of the proportion of variance explained by the markers in the F₂ population was 0.327 (0.121).

(iii) Backfat depth

Posterior mean estimates of the additive marker effects with Gaussian and asymmetric *t* prior distributions are presented in Fig. 2 (bottom panel). The

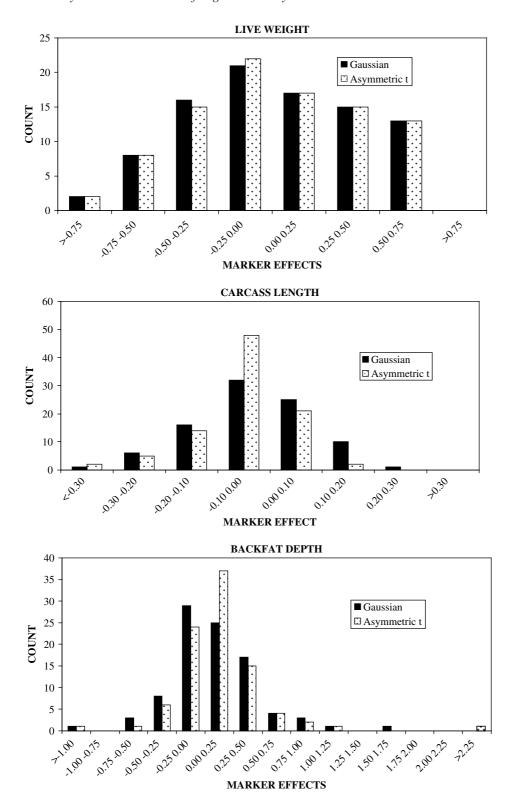


Fig. 2. Posterior mean estimates with the Gaussian and asymmetric t models for marker effects for live weight, carcass length and backfat depth.

most sizeable additive effects were associated with markers S0001 (+0.99 mm) in SSC4, SW316 (+1.09 mm) and S0228 (+2.30 mm) in SSC6, and S0101 (-1.05 mm) in SSC7. The posterior mean and

standard deviation of γ were 0.87 and 0.08, respectively (Fig. 3, bottom panel), with a posterior probability of γ greater than 1 equal to 4.7%. As a consequence, the probability mass below 0 in the

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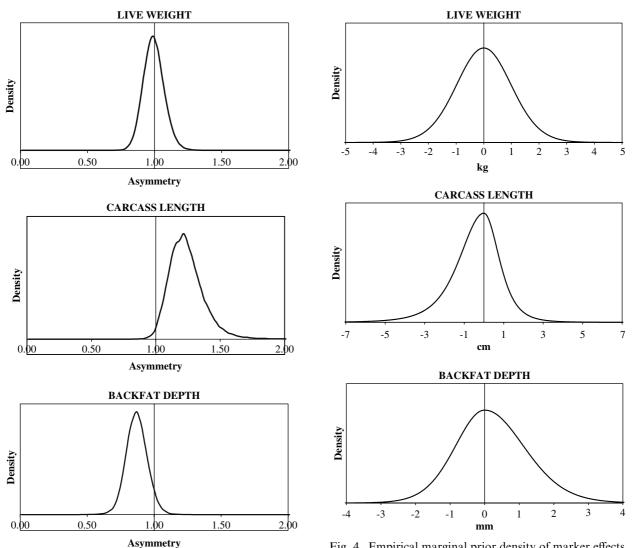


Fig. 3. Posterior density of the asymmetry parameter (γ) for live weight, carcass length and backfat depth.

Fig. 4. Empirical marginal prior density of marker effects for live weight, carcass length and backfat depth.

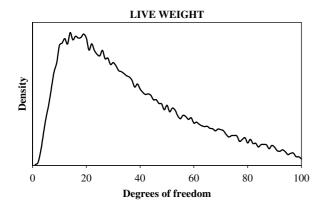
empirical marginal prior distribution of the marker effects was 0.43 (Fig. 4, bottom panel). In Fig. 5 (bottom panel), we present the posterior distribution of the degrees of freedom of the *t*-distribution, with a posterior mode of 2, and a probability of the degrees of freedom being greater than 30 equal to only 17.98%. The posterior mean estimate of the variance of the effects associated with the markers was 0.195 (0.120), and the posterior mean estimate of the residual variance was 22.94 (2.31). The posterior mean of the proportion of variance explained by the markers in the F_2 population was 0.397 (0.170).

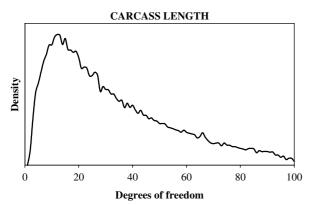
5. Discussion

The *t*-distribution has been widely used to model deviations from Gaussian assumptions (Lange *et al.* 1989), even in the field of quantitative genetics (Stranden & Gianola, 1999; Rosa *et al.*, 2004).

However, these *t*-distributions have been used mostly to model residuals, due to the suspect unknown nonrandom preferential treatment associated with some observations (Stranden & Gianola, 1999). In our case, we used it to model the prior distribution of effects associated with molecular markers. The *t*-distribution can account better than the Gaussian distribution for heavy tails, and its use is justified on the basis of evidence suggesting that some markers or segments of the genome are strongly associated with major genes or QTL. In the present study, we replaced the prior Gaussian distribution with a robust *t*-distribution in the procedure designed by Gianola *et al.* (2003).

Furthermore, the symmetric distribution of Gianola *et al.* (2003) was replaced by an asymmetric distribution (Fernandez & Steel, 1998), which allows for differences in the density of positive and negative effects. Most experiments for detecting QTL are based on F₂ designs involving crosses between divergent lines. With this scheme, most of the QTL effects are





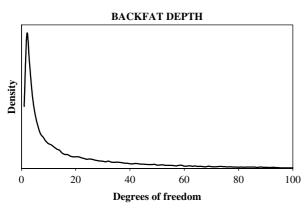


Fig. 5. Posterior density of the degrees of freedom (v) of the t-distribution for live weight, carcass length and backfat depth.

expected to favour the most productive line, whereas only a few are expected to be cryptic, or to favour the lowest production line. Therefore, the asymmetric distributions described by Fernandez & Steel (1998) can be very useful for modelling asymmetry of effects.

It must be noted that the symmetric Gaussian prior defined by Gianola *et al.* (2003) is a particular case of the proposed model. The asymmetric robust distribution converges to the Gaussian distribution when the asymmetry parameter (γ) is equal to 1 and when the degrees of freedom of the *t*-distribution are large enough.

One of the most controversial points in Bayesian analysis is the specification of prior distributions.

Here, the prior distribution of γ (Fig. 1) was assumed flat between 0 and 1 with a probability of 0·5, and with a density equal to $\frac{0.5}{\gamma^2}$ when γ is greater than 1. This distribution ensured that 50% of prior probability was below $\gamma=1$ and 50% over $\gamma=1$ and, in addition, that the probability of a subspace between 0 and 1 was equal to the probability between the reciprocal of the boundaries of the subspace. For example, the prior probability of γ being between 0·3 and 0·5 was 0·1, which is the same as the probability of it being between $\frac{1}{0.3}$ and $\frac{1}{0.5}$. In addition, the prior distribution of the degrees of freedom was assumed to be uniform between values of 1 and 100. The upper limit of 100 was established by assuming that differences between t-distributions with degrees of freedom over 100 are negligible, so the resulting formula would be equivalent to that of a univariate Gaussian distribution.

In the case analysed, we presented results for three traits, leading to different pictures with respect to asymmetry and degrees of freedom of the t-distribution. The posterior distribution of γ was centred on 1 for live weight, whereas the probability of γ being over 1 was higher for carcass length and lower for backfat depth (Fig. 3). These results support the idea that the empirical marginal prior distribution of the marker effects should be asymmetric for backfat depth and carcass length (Fig. 4). As a consequence, such an empirical marginal prior distribution implies an increase in the proportion of negative effects on carcass length relative to a Gaussian prior distribution (Fig. 2, centre panel). This would favour the Landrace line, due to the differences between the two breeds reported in the literature (Serra et al., 1998). Similarly, an increase in the proportion of positive effects (favouring the Iberian line) was observed for backfat depth (Fig. 2, bottom panel). Again, these results are consistent with differences between the parental breeds reported in the literature. For instance, Serra et al. (1998) reported that mean backfat was 48 mm for the Iberian and 20 mm for the Landrace pigs, respectively.

With respect to the degrees of freedom of the *t*-distribution, posterior distributions for live weight and carcass length had modes, means and medians close to 20, while the probability of their respective degrees of freedom being over 30 was around 50%. These results imply that the distribution of marker effects does not differ substantially from a Gaussian distribution, and that including a robustness correction is not strictly needed. On the other hand, for backfat depth, the posterior distribution of the degrees of freedom had a mode of 2, and the posterior probability of being over 30 was only 17.98%. Here, the robustness 'correction' was useful, and these results agree with those presented by Varona *et al.* (2002), showing that some QTL with major effects

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could explain differences between the two lines. These QTL effects associated with markers S0001 (+0.99 mm) in SSC4, SW316 (+1.09 mm) and S0228 (+2.30 mm) in SSC6, and S0101 (-1.05 mm) in SSC7.

The case studied provided a simple description of differences between two line origins in an F_2 experiment. Marker effects for live weight were appropriately described with a Gaussian prior distribution, whereas marker effects for carcass length were clearly asymmetric, and for backfat depth a skewed t-distribution seemed more appropriate.

The 92 marker effects were assumed to be drawn from a single distribution, but extensions to this model can be implemented with ease. Marker effects could be split into between- and within-chromosome deviations, as suggested by Gianola et al. (2003). Moreover, the evidence of co-expression in adjacent regions of the genome (Caron et al., 2001) suggests a covariance structure between the various marker effects. In this sense, multivariate skew distributions (Gupta, 2003; Gupta et al., 2004) could be used to accommodate relationships between markers in the prior distribution, and even to estimate the relationship parameter(s) via a Metropolis–Hastings algorithm (Hastings, 1970). In addition, background polygenic effects could also be modelled by assuming either a multivariate normal distribution with the numerator relationship matrix (Quaas, 1976), or with multivariate t-distributions as proposed by Stranden & Gianola (1999), and the segregation variance could be modelled as suggested by Birchmeier et al. (2002).

The procedure proposed by Xu (2003) differs from that proposed by Gianola *et al.* (2003) in the definition of the prior distributions. The former author proposed a prior distribution unique to each of the marker effects, whereas Gianola *et al.* (2003) argued that marker effects are a sample from a more general prior distribution. A skewed *t*-distribution can also be fitted in the procedure of Xu (2003), by assuming that the asymmetry parameter (γ) and the degrees of freedom (t) are common to all prior distributions of the marker effects.

In conclusion, as illustrated in this study, the skewed t prior distribution proposed offers flexibility and robustness concerning the distribution of genetic effects associated with molecular markers. The use of shrinkage as suggested by Whittaker (2001) and Lange & Whittaker (2001), and generalized into a Bayesian setting by Gianola $et\ al.\ (2003)$, avoids problems due to overparameterization, and colinearity causing unstable least-squares estimates. The skewed t-distribution retains the desirable properties described in Gianola $et\ al.\ (2003)$ but also makes it possible to describe differences between lines in an F_2 cross more adequately. This procedure can also be used to make a global description of differences

between parental lines due to additive, dominance and epistatic effects.

Some other possible extensions of the procedure can be considered. First, the number of degrees of freedom can vary between positive and negative effects, accounting for possible differences in heavy tails favouring each of the founder lines. Second, the residual distribution considered here was Gaussian, but it can be replaced by a skewed *t*-distribution, following Von Rohr & Hoeschele (2002). In addition, further research must be done to compare the proposed model with other alternatives for modelling asymmetry of effects, such us the use of mixtures of distributions (Gianola *et al.*, 2006).

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References

- Andersson, L., Haley, C. S., Ellegren, H., Knott, S. A., Johansson, M., Andersson, K., Andersson-Eklund, L., Edfors-Lilja, I., Fredholm, M., Hansson, I., Hakansson, J. & Lundstrom, K. (1994). Genetic mapping of quantitative trait loci for growth and fatness in pigs. *Science* 263, 1771–1774.
- Best, N., Kathryn, M. K. & Vines, K. (1995). CODA: convergence diagnosis and output analysis software for Gibbs sampling output. Version 3.0. Cambridge: Medical Research Council Biostatistics Unit.
- Birchmeier, A. N., Cantet, R. J. C., Fernando, R. L., Morris, C. A., Holgado, F., Jara, A. & Cristal, M. S. (2002). Estimation of segregation variance for birth weight in beef cattle. *Livestock Production Science* 76, 27–35.
- Caron, H., Van Schaik, B., Van der Mee, M., Baas, F., Riggins, G., Van Sluis, P., Hermus, M. C., Van Asperen, R., Boon, K., Voute, P. A., Heisterkamp, S., Van Kampen, A. & Versteeg, R. (2001). The human transcriptome map: clustering of highly expressed genes in chromosomal domains. *Science* 291, 1289–1292.
- DeVicente, M. C. & Tanksley, S. D. (1993). QTL analysis of transgressive segregation in an interspecific tomato cross. *Genetics* 134, 585–596.
- Fernandez, C. & Steel, M. F. J. (1998). On Bayesian modelling of fat tails and skewness. *Journal of the American Statistical Association* **93**, 359–371.
- Gelfand, A. & Smith, A. F. M. (1990). Sampling based approaches to calculating marginal densities. *Journal of* the American Statistical Association 85, 398–409.
- Gianola, D., Perez-Enciso, M. & Toro, M. A. (2003). On marker-assisted prediction of genetic values: beyond the ridge. *Genetics* 163, 347–365.
- Gianola, D., Heringstad, B. & Odegaard, J. (2006). On the quantitative genetics of mixture characters. *Genetics* 173, 2247–2255.
- Gupta, A. K. (2003). Multivariate skew *t*-distribution. *Statistics* **37**, 359–363.
- Gupta, A. K., Gonzalez-Farias, H. & Domínguez-Molina, J. (2004). A multivariate skew normal distribution. Journal of Multivariate Analysis 89, 181–190.

- Haley, C. S., Knott, S. A. & Elsen, J. M. (1994). Mapping quantitative trait loci in crosses between outbred lines using least squares. *Genetics* **136**, 1195–1207.
- Hastings, W. K. (1970). Monte-Carlo methods using Markov chains and their applications. *Biometrika* 57, 97.
- Iannucelli, E., Wolosyn, N., Arhainx, J., Gellin, J. & Milan, D. (1996). Gemma: a database to manage and automate microsatellite genotyping. In *Proceedings of* the International Society of Animal Genetics Conference, Tours, France, p. 88.
- Lander, E. S. & Botstein, D. (1989). Mapping mendelian factors underlying quantitative traits using RFLP linkage maps. *Genetics* 121, 185–199.
- Lange, C. & Whittaker, J. C. (2001). On prediction of genetic values in marker-assisted selection. *Genetics* 124, 743–756.
- Lange, K. L., Little, R. J. A. & Taylor, J. M. H. (1989).
 Robust statistical modelling using the t-distribution.
 Journal of the American Statistical Association 84, 881–896.
- Mekkawy, W. (2005). QTL bayesian analysis. Doctoral thesis, Universidad Politecnica de Valencia.
- Pe, M. E., Gianfranceschi, L., Taramino, G., Tarchini, R., Angelini, P., Dani, M. & Binelli, G. (1993). Mapping quantitative trait loci (QTLs) for resistance to *Gibberella* zeae infection in maize. *Molecular and General Genetics* 241, 11–16.
- Quaas, R. L. (1976). Computing diagonal elements and inverse of a large numerator relationship matrix. *Biometrics* **32**, 949–953.
- Ron, M., Lewin, H., Da, Y., Band, M., Yanai, A., Blank, Y., Feldmesser, E. & Weller, J. I. (1995). Prediction of informativeness for microsatellite markers among

- progeny of sires used for detection of economic trait loci in dairy cattle. *Animal Genetics* **26**, 439–441.
- Rosa, G., Gianola, D. & Padovani, C. R. (2004). Bayesian longitudinal data analysis with mixed models and thick-tailed distributions using MCMC. *Journal of Applied Statistics* **31**, 855–873.
- Serra, X., Gil, M., Pérez-Enciso, M., Oliver, M. A., Vazquez, J. M., Gispert, M., Diaz, I., Moreno, F., Latorre, J. L. & Noguera, J. L. (1998). A comparison of carcass, meat quality and histochemical characteristics of Iberian (Guadyerbas line) and Landrace pigs. *Livestock Production Science* 56, 215–223.
- Stranden, I. & Gianola, D. (1999). Mixed effects linear models with *t*-distributions for quantitative genetic analysis: a Bayesian approach. *Genetics Selection Evolution* 31, 25–42.
- Toro, M. A., Rodrigáñez, J., Silió, L. & Rodríguez, C. (2000). Genealogical analysis of a closed herd of black hairless Iberian pigs. Conservation Biology 14, 1843–1851.
- Varona, L., Ovilo, C., Clop, A., Noguera, J. L., Pérez-Enciso, M., Coll, A., Folch, J. M., Barragán, C., Toro, M. A., Babot, D. & Sanchez, A. (2002). QTL mapping for growth and carcass traits in an Iberian by Landrace pig intercross: additive, dominant and epistatic effects. *Genetical Research* 80, 145–154.
- Von Rohr, P. & Hoeschele, I. (2002). Bayesian QTL mapping using skewed Student *t*-distributions. *Genetics Selection Evolution* **34**, 1–21.
- Whittaker, J. C. (2001). Marker-assisted selection and introgression. In *Handbook of Statistical Genetics* (ed. D. J. Balding, M. Biship & C. Cannings), pp. 673–693. Chichester: Wiley.
- Xu, S. (2003). Estimating polygenic effects using markers of the entire genome. *Genetics* **163**, 789–801.