

THE
JOURNAL
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SYMBOLIC LOGIC

EDITED BY

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MEMBERS

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ERRATA

VOLUME 2

Page 93, line 21. For *CCpqCCqrCCpr*, read *CCpqCCqrCpr*.

VOLUME 15

Page 236, line 10 from the bottom. For (XIII 221), read (XIII 212).

Page 285, line 11. Delete the parenthesis after XIV.

VOLUME 21

Page 409, line 14. For «ZASPAVSKIJ», read «ZASLAVSKIJ».

VOLUME 24

Page 274, line 1. Add 35 at the end of the line.

Page 347, column 1. The reference «Reprinted (XXIV 191)» should be deleted in lines 28–29 and inserted instead at the end of line 30.

VOLUME 25

Page 287, line 24. For XXI 370, read XXI 367.

Page 378, line 18. For XXII 72, read XVIII 340.

VOLUME 27

Page 83, line 27. For «RószA», read «RózsA».

Page 92, line 32. For «un dihr», read «und ihr».

Page 93, line 2 from the bottom, and page 94, lines 1 and 5. For «Łos», read «Łoś».

Page 98, line 21. For α , read $|\alpha|$.

Page 100, line 18. For «*Mathématique*», read «*Mathématique*».

Page 100, line 22. Read «*Boolean*».

Page 101, line 18. For «ANTONIŃ», read «ANTONÍN».

Page 108, line 25. For «*domains*», read «*domain*».

Page 109, line 12 from the bottom. For $\mathfrak{F}(e_r\mathfrak{F}(r))$, read $\mathfrak{F}(e_r\mathfrak{F}(r))$.

Page 120, line 17 from the bottom and page 121, line 4 from the bottom. For «*Minneapolis*», read «(Minneapolis)».

Page 225, line 20. For «case», read «*case*».

Page 226, line 25. For «*language*», read «*langage*».

Page 251, line 9. For XXIII 99, read XXIII 99(14).

Page 357, line 1. For «Frayne s», read «Frayne's».

Page 359, line 24. For $\alpha^2(\bar{\alpha}^1(x))$, read $\alpha^{(2)}(\bar{\alpha}^1(x))$.

Page 369, line 13 from the bottom. For «*siti*», read «*siti*».

Page 370, line 20. For «D. VON DANTZIG», read «D. VAN DANTZIG».

Page 370, line 24. For «*Elementarmathematik*», read «*Elementar-Mathematik*».

Page 371, line 17 from the bottom. After «*confirmation*», insert «(XXVII 122)».

ERRATA

Page 472, line 21. For «thcorem», read «theorem».

Page 472, line 34. For «equivalences», read «equivalence».

VOLUME 28

Page 100, line 6 from the bottom. For «finite», read «infinite».

Page 162. The next to last asciom of group (4) should read:

$$Ax, l, y \rightarrow Ax\Delta_x, l, yl.$$