## Correspondence

DEAR EDITOR,
In 'Moving the first digit of a positive integer to the last' (Math. Gaz. 83 pp. 216-220), Braza and Tong's treatment of the problem is impressive, but they fail to observe that there is an easy way to calculate by hand numbers such that moving the first digit to the last is equivalent to a division.

Choose the first digit, say 8 , and the divisor, say 4 . We proceed using the usual paper method for division; but at each step the latest digit of the quotient provides the next digit for the dividend (together with any carry digits).

$$
4 \begin{array}{ccc}
2 & 0 & 5 \\
\hline 8^{0} & 2^{2} & 0^{0}
\end{array} \rightarrow \begin{array}{cccc}
2 & 0 & 5 & 1 \\
\hline
\end{array}
$$

The process terminates when the latest digit of the quotient equals the first digit chosen and there is no remainder outstanding. The given example will terminate at 820512 , with quotient 205128.

This method shows why there can only be one basic answer for a given first digit. and why all other answers are concatenations of the basic answer.

Yours sincerely,
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DEAR EDITOR,
I offer a couple of observations on items in the excellent July 1999 Gazette.

1. Readers of Robert J. Clarke's article might also be interested in a diagram described by Ravi Vakil in his lively book A mathematical mosaic
 (enthusiastically reviewed by Andre Toom in the January 1998 American Mathematical Monthly-'This is a book I would have like to have read as a boy'). Page 87 features what Vakil calls the Ailles Rectangle, named after an Ontario High School Teacher, Doug Ailles.

Here, from the $45^{\circ}$-triangles, $x$ and $y$ are immediately seen to be $\sqrt{3} / \sqrt{2}$ and $1 / \sqrt{2}$ so that the trigonometric ratios for $15^{\circ}$ and $75^{\circ}$ can be read off from triangle $T$.
2. An alternative proof that J. A. Scott's recalcitrant series $\sum\left(n^{1 / n}-1\right)^{p}$ converges for $p>1$ runs as follows: Fix a natural number $k$ with $k>p /(p-1)$, so that $p>k /(k-1)$. Write $n^{1 / n}=1+a_{n}$ with $a_{n} \geqslant 0$. Then, for all $n \geqslant 2 k$, we have:

