But the second line of (35) is the residue at the pole of $1/\sin \pi(\zeta - t)$. Hence the sum of the four similar expressions

= - residue at pole of
$$1/\sin \pi (\zeta - c)$$

= $-\frac{\sin \pi c}{\sin \pi (t - c) \text{ do. } x, y, z}$.

Thus for the sum of the series in (33) we have

$$S = \frac{\pi^{3} \sin \pi c}{\sin \pi (t - c) \text{ do. } x, y, z} \times \frac{\Pi(t + x + y + z - 2c)}{\Pi(y + z - c) \Pi(z + x - c) \Pi(x + y - c) \Pi(t + x - c) \text{ do. } y, 2}, \quad (36)$$
where $R(t + x + y + z - 2c) > -1$.

To exhibit the result as the summation of a series of rational terms, multiply both sides of (36) by

$$\frac{\prod t \prod x \prod y \prod z}{\prod (c-1-t) \text{ do. } x, y, z}.$$

Then

$$c + (c+2) \frac{c-t}{t+1} \text{ do. } x, y, z, + \dots + (c+2n) \frac{(c-t)^{(n)}}{(t+1)^{(n)}} \text{ do. } x, y z, + \dots$$

$$+ (c-2) \frac{t}{c-t-1} \text{ do. } x, y, z, + \dots + (c-2n) \frac{t^{(-n)}}{(c-t-1)^{(-n)}} \text{ do. } x, y, z, + \dots$$

$$= \frac{\sin \pi c}{\pi} \frac{\prod_t \prod_x \prod_y \prod_z \prod_{t=0}^{\infty} (t-c) \prod_{t=0}^{\infty} (x-c) \prod_{t=$$

For t = 0, this is equivalent to (9).

The result may be put in somewhat more striking form by writing 2a for c, and then t+a, x+a, y+a, z+a for t, x, y, z.

Of special cases of (37), those obtained by writing t = c/2, $t = \infty$, t = (c-1)/2 may be mentioned.

On the Resolution of Integral Algebraic Expressions into Factors.

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On Arithmetical Approximations. By R. F. Davis, M.A.