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Fingerprints and the Diagnosis of Zygosity in Twins*

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I. Design of the Work

I.1. INTRODUCTION

Bibliographic references, aim, material and methods of the present study, as well as the methodology especially worked out for the qualitative analysis, have already been largely described in a previous introductory note (Parisi and Di Bacco, 1967). A few minor variations having been introduced, and for the sake of completeness, essential data shall be now referred to again, before describing and discussing the results.

This research was designed with two complementary aims:

a) To apply the twin method to the study of the hereditary behaviour of digital dermatoglyphic traits, both at the qualitative and quantitative level;

b) To apply the results thus obtained to work out a method for discriminating MZ and DZ twins by means of fingerprints.

I.2. MATERIAL AND METHODS

A sample of 100, apparently healthy, same-sexed twin pairs, only selected as to sex combination and zygosity (25 $3 + 25 \ Q$ MZ, and 25 $3 + 25 \ Q$ DZ), was drawn from the Mendel Institute's large twin file and fingerprinted.

Zygosity was determined on account of the following data (cf recommendations of the WHO report on the methodology of twin studies, 1966, and Hauge et al, 1968): (a) number of choria; (b) ABO, MN and Rh blood groups; (c) eye and hair colour, according to the apposite anthropological scales; (d) information about the twins ever having been mixed up by parents, friends or relatives; (e) subjective judgements on the basis of the twins' general aspect, direct medical examination, anamnestic data etc.

Fingerprints were examined with respect to both qualitative and quantitative

* With an Appendix on Automatic Procedure by M. Umani.

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(Dx =	= right; $Sn = left$; 1a and 2a nata = 1st and 2nd born)					l born)		57361	F. ANTO	NINA BI	aola - M2		
[D	x					2	ST.			DX + SM
	I	II	III	IV	۷	RFRC	I	II	III	IV	٧	LFRC	TTRC
1a nata	W/21	Lu/15	Lu/13	La/5	Lu/6	60	8/23	Lu/10	Lu/5	Lu/5	La/7	50	110
2a nata	Lu/20	Lu/11	Lu/10	Lu/12	Lu/9	62	Lu/18	Lu/10	Lu/11	Lu/10	A/0	49	111

Tab. I. Standardized procedure for the collection of data: pattern/ridge count

traits (cf Tab. I), i.e. to the five fundamental papillary patterns [W = whorl; Lu = ulnar loop; Lr = radial loop; S = twin loops (S figure); A = arch], and to ridge counts, both single for each finger and cumulative for one or both hands (RFRC = right finger ridge count; LFRC = left finger ridge count; TFRC = total finger ridge count).

II. Methodology of the Analysis

II.1. QUALITATIVE ANALYSIS

A judgement on the similarities existing for each finger between cotwins' papillary patterns will be based upon the probability of obtaining at random and conditional upon the distribution of the five papillary patterns observed in the sample a number of concordances (namely, of coinciding patterns between cotwins' corresponding fingers) not lesser than the number observed in the sample.

The calculation of this probability is not easily done: it may however be summed up as follows.

Let us order the five papillary patterns arbitrarily. Let then ${}_{D}Z_{1}$ (i = 1; ...; 5) be the aggregate number of the ith type observed on the D finger in the two members of the n twin pairs observed. Let also ${}_{D}f_{11}$ be the number of pairs in which the finger D of both members has the pattern i, and ${}_{D}f_{13}$ the number of pairs in which one of the two members has the pattern i on his finger D while the other has the pattern j (j = 2; ...; 5. In general, j > i).

The observed sample of n pairs may be represented by a sample configuration which is a vector formed by fifteen non-negative integer numbers:

$$[I.I] D_{D}F_{r} \equiv (_{D}f_{11}; ...; Df_{55}; Df_{12}; ...; Df_{15}; ...; Df_{34}; Df_{35}; Df_{45})$$

and the number of observed concordances is $_{D}r = \Sigma_{iD}f_{1i}$.

In the previous, already cited, introductory note, it has been shown that the probability

$$\mathbf{P}_{\mathbf{r}} \left\{ {}_{\mathbf{D}} \mathbf{F}_{\mathbf{r}} \right\} {}_{\mathbf{D}} \mathbf{Z}_{1}; \ldots; {}_{\mathbf{D}} \mathbf{Z}_{5} \right\}$$

to obtain the sampling configuration at random, is:

$$[1.2] P_{\mathbf{r}} \{ {}_{\mathbf{D}}\mathbf{F}_{\mathbf{r}} \mid {}_{\mathbf{D}}\mathbf{Z}_{\mathbf{1}}; ...; {}_{\mathbf{D}}\mathbf{Z}_{\mathbf{5}} \} = \frac{n!}{\prod_{i \leq \mathbf{1}} {}_{\mathbf{D}}\mathbf{f}_{\mathbf{i}\mathbf{j}}!} \cdot \frac{\prod_{i=\mathbf{r}} {}_{\mathbf{D}}\mathbf{Z}_{\mathbf{i}}!}{(2n)!} 2^{n} - {}_{\mathbf{D}}\mathbf{r}.$$

However, [1.2] is not the probability of obtaining $_{D}r$ concordances at random, conditional upon the frequencies. This may be obtained, instead, by setting up all the sampling configurations that may be obtained from [1.1] by causing $_{D}f_{11}$ and $_{D}f_{13}$ to vary in the class of non-negative integer numbers under the conditions:

[1.3]
$$\begin{cases} \sum_{i=1}^{5} {}_{D}f_{i1} = {}_{D}r \\ {}_{2}{}_{D}f_{11} + \sum_{j=2}^{5} {}_{D}f_{1j} = {}_{D}Z_{1} \end{cases}$$

The probability of each such configurations may be calculated by means of [1.2]. Then,

$$[I.4] P_{r} \{ {}_{D}r \mid {}_{D}Z_{1}; ...; {}_{D}Z_{5} \} = \Sigma P_{r} \{ {}_{D}F_{r} \mid {}_{D}Z_{1}; ...; {}_{D}Z_{5} \}$$

(being the summations extended to all the configurations obtained under the conditions [1.3]) is actually the probability required.

Finally, if also the probability values under [1.4] are calculated for all possible values of r greater than $_{D}r$ (on putting r instead of $_{D}r$ in [1.3] and [1.4]), then:

[1.5]
$$P_r \{r \ge_D r|_D Z_1; ...; {}_D Z_5\} = \sum_{r=D}^{DR} P_r \{r|_D Z_1; ...; {}_D Z_5\},$$

where ${}_{D}R = \sum_{i=1}^{5} {}_{D}S_{1}$, with ${}_{D}S_{1} = \frac{{}_{D}Z_{1}}{2}$ or ${}_{D}S_{1} = \frac{{}_{D}Z_{1} - 1}{2}$, according to ${}_{D}Z_{1}$ being even or odd.

The [1.5] is the required probability of obtaining at random a number of concordances greater than, or equal to, that observed on the D finger, conditional upon the frequencies ${}_{D}Z_{1}$; ...; ${}_{D}Z_{5}$ of the five types of patterns referring to the D finger.

The difficulty of this procedure lies in the constructions of configurations similar to [1.1] under the conditions [1.3]. A method which makes this construction possible has already been explained (Parisi and Di Bacco, 1967: II.2), while in the Appendix to the present work details of the Fortran program are given. By employing this method it was possible to entrust to a $7044/K_{32}$ IBM computer the search for the sampling configurations. Having fixed the critical value 0.01 of the probability

of an error of the first kind, it may be said that there is a similarity with respect to the finger D between the twins, if the probability $P_r \{r \ge Dr|_D Z_1; ...; DZ_5\}$ calculated by means of [1.5] is lesser than, or equal to, 0.01. If the probability is greater than 0.01, the hypothesis is rejected.

The results of this test are shown in Tab. II, together with a synthetical judgement on the hypothesis of similarity, i.e.: "+" if it is true, "-" if it is false.

Since sex did not appear to play any relevant role, the same analysis has been carried out on the two samples of 50 MZ and 50 DZ twin pairs, irrespective of sex (third section of the table). The results of this analysis by zygosity only are quite similar to those by sex and zygosity, except that for finger II only the upper or lower probability limits are given, instead of the precise probability value [1.5]. Actually, as explained in the Appendix, an accurate computation of these four values would have required an enormous load of work, practically unnecessary for the purposes of our conclusion: in fact, also in this particular case the preassigned probability value of an error of the first kind is 0.01.

II.2. QUANTITATIVE ANALYSIS

Cumulative ridge counts, i.e. RFRC, LFRC and TFRC values, have been considered, and their correlations estimated in the four types of twin pairs (MZ \circlearrowleft , MZ \wp , DZ \circlearrowright and DZ \heartsuit) by computing, for each sample and for each count, the intraclass correlation coefficient. The twelve values of the latter are shown in the upper part of Tab. III. Their general coefficient will be indicated as r_{1jt} ($i \equiv MZ$, DZ; $j \equiv \circlearrowright$, \heartsuit ; $t \equiv R$ for RFRC, L for LFRC, T for TFRC), which is an unbiased and consistent estimator of the "true" coefficient of intra-class correlation, ρ_{1jt} .

We may reasonably assume that the bivariate random variable associated with the sample values of RFRC, LFRC and TFRC in twin pairs is fairly well approximate to a bivariate normal distribution. It is then possible to set up also a confidence interval for the coefficient ρ_{ijt} .

In fact, if $I - \alpha$, where $0 < \alpha < I$, is the confidence coefficient, the upper [lower] confidence limits for the coefficient of correlation are *:

[2.1]
$$\operatorname{tngh} \left\{ \operatorname{tngh}^{-1} \operatorname{r}_{ijt} + \frac{\lambda}{n - \frac{3}{2}} \right\}$$
$$\left[\operatorname{tngh} \left\{ \operatorname{tngh}^{-1} \operatorname{r}_{ijt} - \frac{\lambda}{n - \frac{3}{2}} \right\} \right]$$

* The justification for [2.1] lies in the following property: if the parent-population, from which the sample is obtained, is bivariate-normally distributed, then the transformation $Z_{ijt} = tngh^{-1} r_{ijt}$ is asymptotically normally distributed with mean = tngh⁻¹ ρ_{ijt} and variance = $\frac{I}{N - 3/2}$ (cf Fischer, 1921).

where n is the number of pairs making up the sample (i.e. 25) and λ is the root of the equation G (-x) = $\frac{\alpha}{2}$ if G(x) is the distribution function of the normal random variable with mean 0 and variance 1.

By choosing $1 - \alpha = 0.95$, hence $\lambda = 1.96$, we obtain the twelve confidence intervals at 95% level. They are shown in the lower part of Tab. III.

The following questions have then been examined:

(A) Is the coefficient of intra-class correlation higher in MZ than in DZ twin pairs?

(B) Is the coefficient of intra-class correlation significantly different in arrow and Q twin pairs?

(C) Is there any significant interaction between sex and zygosity for the characteristics under consideration? In other words, are sexual differences significantly diverse according to the pairs being MZ or DZ? Or, conversely: are differences due to zygosity significantly diverse according to the pairs being σ or ϕ ?

Answers to these questions have been provided (only with respect to the TFRC, because of its wider use and probably more limited random variability, as the general cumulative value) by applying the comparative orthogonal design to the two "factors", zygosity and sex, each having two "levels": MZ; DZ, and random respectively.

In our particular case, once selected the value of the probability of an error of the first kind, tests * have to be set up in order to verify the three hypotheses:

$$\begin{bmatrix} 2.2 \end{bmatrix} \qquad u_{A} = \frac{(Z_{MZ,O^{,T}} + Z_{MZ,Q,T}) - (Z_{DZ,O^{,T}} + Z_{DZ,Q,T})}{\sqrt{\frac{4}{23.5}}}$$
$$u_{B} = \frac{|(Z_{MZ,O^{,T}} + Z_{DZ,O^{,T}}) - (Z_{MZ,Q,T} + Z_{DZ,Q,T})|}{\sqrt{\frac{4}{23.5}}}$$
$$u_{C} = \frac{|(Z_{MZ,O^{,T}} - Z_{MZ,Q,T}) - (Z_{DZ,O^{,T}} - Z_{DZ,Q,T})|}{\sqrt{\frac{4}{23.5}}}$$

where $Z_{ijt} = tngh^{-1} r_{ijt}$.

The three questions, A; B; C, will be given positive answers, respectively if $u_A \ge -\lambda(\alpha)$; $u_B \ge -\lambda\left(\frac{\alpha}{2}\right)$; $u_C \ge -\lambda\left(\frac{\alpha}{2}\right)$.

* The justification for the three tests here applied is given in detail by Naddeo (1960).

Since $-\lambda(\alpha)$ and $-\lambda\left(\frac{\alpha}{2}\right)$ are the roots of the two equations, respectively $G(x) = \alpha$ and $G(x) = \frac{\alpha}{2}$ [where G(x) is the distribution function of the normal random variable with mean 0 and variance 1], if we choose $\alpha = 0.05$ we have $-\lambda\left(\frac{\alpha}{2}\right) = 1.96$ and $-\lambda(\alpha) = 1.649$.

The following values are thus obtained *:

$$u_A = 8.3438; u_B = 0.4023; u_C = 1.0427.$$

Our conclusion will therefore be that the TFRC correlation is significantly higher in MZ than in DZ pairs. On the other hand, sex does not seem to play any relevant role, nor does it appear to exist any interaction between sex and zygosity.

On the basis of these latter two results, sexes have been pulled within zygosities, and sample intraclass correlation coefficients, and respective confidence intervals (with $I - \alpha = 0.95$), have been estimated for MZ and DZ twin pairs, irrespective of sex (cf Tab. IV).

Correlation values were then estimated for each finger. Sex having already been shown not to play any relevant role, the analysis was directly carried out on the two samples of 50 MZ and 50 DZ twin pairs, irrespective of sex. The results are shown in Tab. V.

Although, because of methodological problems, the previously described test could not be applied in this case, correlation values for single fingers appear to be much higher in MZ than in DZ twin pairs, and altogether similar to those obtained for cumulative values.

* The values of u_A ; u_B ; u_C ; are based on the following values of Z_{ijt} :

 $\begin{array}{rcl} Z_{MZ}\bigcirc^{n}T &= tngh \ ^{-1} \ (o.988) \ = \ 2.555 \\ Z_{MZ} \bigtriangledown T &= tngh \ ^{-1} \ (o.983) \ = \ 2.3796 \\ Z_{DZ}\bigcirc^{n}T &= tngh \ ^{-1} \ (o.381) \ = \ o.4013 \\ Z_{DZ} \bigtriangledown T &= tngh \ ^{-1} \ (o.633) \ = \ o.7465 \end{array}$

III. Results

III.1. QUALITATIVE ANALYSIS

The results of the qualitative analysis are summarized into the six sections of Tab. II, the upper three being referred to the MZ sample and the lower three to the DZ one.

Finger		ੈ				Ŷ		$\zeta + \zeta$		
		N. of con- cordances	Proba- bility	Judge- ment	N. of con- cordances	Proba- bility	Judge- ment	N. of con- cordances	Proba- bility	Judge- ment
					a. MZ sa	mple				
	I	13	0.00876	+	17	0.00164	+	30	0.00004	+
ΤŦ	II	10	0.14430		16	0.00010	+	26	<0.01*	+
5	III	18	0.00003	+	22	0.00004	+	40	0.00000	+
S.	IV	19	0.00002	+	20	0.00001	+	39	0.00000	+
	V	20	0.00053	+	21	0.00112	+	41	0.00000	+
	Ι	14	0.00742	+	18	0.00021	+	32	0.00000	+
H	II	13	0.00219	+	18	0.00000	+	31	<0.01*	+
Е	III	21	0.00000	+	18	0.00060	+	39	0.00000	+
Ξ	IV	18	0.00016	+	21	0.00000	+	39	0.00000	+
	V	19	0.05554		22	0.00008	+	41	0.00004	+
					b. DZ sa	ample				
	I	17	0.00200	÷	12	0.20378		29	0.00294	+
ΤI	II	II	0.06805		12	0.21797	_	23	>0.01*	
5	III	17	0.05479		22	0.01114	?	39	0.00133	+
Ĩ.	IV	19	0.00701	+	11	0.65506		30	0.03899	
д	V	20	0.01031	-	18	1.00000		38	0.05542	-
	Ι	19	0.00429	+	13	0.12494	_	32	0.00291	+
H	II	13	0.01174	_	13	0.00812	+	26	<0.01*	+-
ΕF	III	14	0.48860		17	0.09283		31	0.14686	—
Г	IV	17	0.02076		18	0.00765	+	35	0.00061	+
	v	20	0.07184		19	0.48427		39	0.08177	—

Tab. II. Qualitative analys

* Only upper or lower probability limits are given, instead of the precise probability [1.5] the calculation of which would have required a practically unnecessary, enormous load of work (cf Appendix).

III.2. QUANTITATIVE ANALYSIS

The results of the quantitative analysis are summarized in Tables III, IV and V, respectively referred to the analysis of cumulative ridge counts by sex and zy-gosity, to the analysis of TFRC values by zygosity only, and to the analysis of single ridge count values, also by zygosity only.

Sample	RFRC	LFRC	TFRC
	a. Estimates of the in	traclass correlation coefficient	(9)
MZ 💍	0.960	0.975	0.988
мz	0.928	0.955	0.983
DZ 👌	0.398	0.323	0.381
DZ Q	0.687	0.565	0.633
MZ J	b. Confidence intervals $0.912 \le \rho \le 0.965$	of ρ (confidence coefficient = $0.946 \le \rho \le 0.989$	0.95) $0.973 \le \rho \le 0.994$
мzұ	$0.849 \leq ho \leq 0.967$	$0.908 \leq ho \leq 0.977$	$0.962 \leq \mu \leq 0.993$
DZ 👌	$0.019 \le \rho \le 0.679$	$0.073 \le \rho \le 0.627$	$0.004 \leq ho \leq 0.666$
DZ♀	$0.417 \le \rho \le 0.849$	$0.225 \le \rho \le 0.777$	$0.326 \le \rho \le 0.815$

Tab. III. Qualititative analysis. Guillulative Huge coulds	Tab.	III.	Quantitative	analysis:	Cumulative	ridge	counts
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Tab. IV.	Quantitative	analysis:	
TFRC	irrespective	of sex	

Tab. V. Quantitative analysis: Estimates of ρ for single ridge counts

Sample	ę	Confidence interval of p		Finger	MZ	DZ
MZ	0.985	$0.966 \leq ho \leq 0.993$		I	0.853	0.258
DZ	0.522	0.180 < 0 < 0.760	НТ	11	0.796	0.380
2.2	0.000		6	III	0.842	0.547
			RI	IV	0.907	0.528
				V	0.904	0.436
				I	0.893	0.122
			H	II	0.867	0.212
			ГЦ L	111	o.888	0.454
			ΓI	IV	0.932	0.535
				V	0.893	0.332

IV. Application of Fingerprints to the Diagnosis of Zygosity

IV.1. INTRODUCTION

The utmost importance of the twin method in human genetic studies makes the diagnosis of zygosity to be a fundamental problem of research. In fact, a large number of methods have been introduced, in the past fifty years, to meet this problem. A recent, authoritative analysis of the main ones has been provided by a WHO report on the methodology of twin studies (1966), which concludes, however, that "there is a great need for further research". Such a need is especially felt in the study of large groups, where more economic and simpler procedures are to be taken into account.

Fingerprints appear to very well meet this need; actually, they started being used for the diagnosis of zygosity in twins around 1930, and many methods have been, and keep being proposed since then. Except for the pattern score worked out by Wendt (1955), the main ones have been proposed by two British biometric schools (Maynard-Smith and Penrose, 1955; and Nixon, 1956; Slater, 1963; Slater et al, 1964) and are generally based on ridge counts.

They all consist in score methods, in which the probability of monozygosity is indirectly proportional to the difference in the cotwins' ridge counts; i.e.: the probability is higher when the difference is lower. For the sake of simplicity, as well as for methodological reasons, we have preferred to work out a method aiming to finding out a general discriminant function between MZ and DZ twin pairs, i.e. based on the classic principles of nonparametric classificatory analysis, with fixed values and probability of error. According to the results obtained in the present study, the search for the discriminant function was based on TFRC differences.

IV.2. TFRC discriminant method

The intraclass correlation coefficient may be interpreted "as a simple linear transformation of a ratio of variances between classes and within classes in the Analysis of Variance" (Kendall and Stuart, 1962).

It has been ascertained (II.2) that the value of the intraclass correlation coefficient is higher in MZ than in DZ twin pairs, and fails to show any sex difference or interaction between sex and zygosity. The modulus Δ of the difference * between

As it is implicit in the inductive techniques employed in the preceding section, we deem it reasonable to assume that the pairs of TFRC values be approximate determinations of a two-dimensional normal random variable. However, this assumption apparently fails to be very useful in attempting to establish a discriminant function of zygosity, so that we have applied a more general procedure (cf Stoller, 1954).

^{*} The use of the absolute difference, instead of the relative one, is advisable, among other things, also in view of the fact that the identification of the cotwins as first and second born is purely conventional. Of course, $\Delta^{\mathbf{x}}$, with K even, could be chosen instead of Δ , but this, as will be plain at a later stage, would be an unnecessary complication.

the two TFRC values observed on the two members of a same-sexed twin pair of unknown zygosity, may be reasonably assumed for the purpose of classifying the pair as either MZ or DZ.

The problem is then to choose a value δ_0 of the variable Δ , such that, if δ is the observed value of Δ :

[3.1]
$$\delta \leq \delta_0$$
 leads to classify the pair as MZ; whereas

[3.2]
$$\delta > \delta_0$$
 leads to classify the pair as DZ.

The choice of the discriminant value δ_0 may be based on the following considerations derived from Stoller (1954) with a few modifications.

Let us suppose we know the probabilities $p(\delta)$ and $q(\delta)$ for Δ to assume a value $\delta = 0$; 1; 2; ...; n, in MZ and DZ twins, respectively.

Let us further suppose we know the probability π for a same-sexed pair to be MZ.

Then:
$$\pi \sum_{\delta=0}^{\delta} p(\delta)$$

is the probability that a same-sexed pair be MZ and that a δ value of Δ , lesser than, or equal to $\overline{\delta}$, be observed thereon.

Similarly, the probability for a same-sexed twin pair to be DZ, and for a δ value, lesser than, or equal to $\overline{\delta}$, to be observed thereon, is:

$$(\mathbf{I} - \pi) \sum_{\delta = 0}^{\delta} q(\delta).$$

Then the probability:

$$[3.3] P(\bar{\delta}) = \pi F(\bar{\delta}) + (I - \pi) [I - G(\bar{\delta})],$$

where $F(\bar{\delta}) = \sum_{\delta = o}^{\bar{\delta}} p(\delta)$ and $G(\bar{\delta}) = \sum_{\delta = o}^{\bar{\delta}} q(\delta)$,

refers to the event of observing a value $\delta \leq \bar{\delta}$ on a MZ, or a value $\delta > \bar{\delta}$ on a DZ same-sexed pair.

If $P(\delta)$, considered as a function of δ , is maximized for $\delta = \delta_0$, then the criterion of classification under [3.1] and [3.2] possesses the desirable property of maximizing the probability of making a correct diagnosis of zygosity of a twin pair under observation. As a result, δ_0 shall be chosen so that

$$[3.4] P(\delta_0) = maximum.$$

The solution to the problem under [3.4] implies the prior knowledge both of the two distribution functions, $p(\delta)$ and $q(\delta)$, and of the probability of monozygosity (π) .

At present, in Italy, the latter may be estimated at 0.30 (Gedda and Brenci, 1961). Hence, we may insert in [3.3]:

$$\pi \simeq \frac{\dot{0.30}}{0.30 + 0.70 + 0.50} = 0.46.$$

The distribution functions $p(\delta)$ and $q(\delta)$ are unknown, and we cannot estimate them by means of the Δ values observed in the four samples under consideration. The following estimators may therefore be set up:

$$\hat{\mathrm{p}}(\delta) = rac{\mathrm{m}_{\mathcal{O}}(\delta) \,+\,\mathrm{m}_{\mathcal{Q}}(\delta)}{5^{\mathrm{O}}} \qquad \hat{\mathrm{q}}(\delta) = rac{\mathrm{n}_{\mathcal{O}}(\delta) \,+\,\mathrm{n}_{\mathcal{Q}}(\delta)}{5^{\mathrm{O}}}\,,$$

 $m_{K}(\delta)$ and $n_{K}(\delta)$ (where $K \equiv \vec{\bigcirc}; \bigcirc$) being the number of pairs which, respectively in the $\vec{\bigcirc}$ and \bigcirc MZ and $\vec{\bigcirc}$ DZ samples, have $\Delta = \delta$.

Then, the probability in [3.3], when inserting $\pi = 0.46$, is estimated by means of:

$$[3.5] \qquad \qquad \text{o.46} \ \hat{\mathbf{F}}(\bar{\delta}) \,+\, \text{o.54} \ [\mathbf{I} - \hat{\mathbf{G}}(\bar{\delta})] \,=\, \hat{\mathbf{P}}(\bar{\delta}),$$

where $\hat{\mathbf{F}}(\bar{\delta}) \,=\, \sum_{\delta=0}^{\bar{\delta}} \hat{\mathbf{p}}(\delta) \quad \text{and} \ \hat{\mathbf{G}}(\bar{\delta}) \,=\, \sum_{\delta=0}^{\bar{\delta}} \hat{\mathbf{q}}(\delta) \,.$

These quantities are obviously determinations of two random variables whose variances are $F(\bar{\delta}) [I - F(\bar{\delta})] 50^{-1}$ and $G(\bar{\delta}) [I - G(\bar{\delta})] 50^{-1}$, respectively. It follows that the standard deviation of the random variable described by the [3.5] estimate is not greater than 0.05.

Let us now consider the sequence generated by [3.5] when $\delta = 0$; 1; ...; n. If for $\bar{\delta} = \delta_0$ the sequence reaches its absolute maximum, δ_0 will be chosen according to the criterion of classification [3.1]; [3.2]. The probability of correctly classifying a twin pair under observation will be estimated by $\hat{P}(\delta_0)$ and its standard deviation will not exceed 0.05.

It should finally be noted that, in the application of this method, r values $\delta_{j}^{(1)}$ (j = 1; 2; ...; r), which maximize the sequence, are likely to be obtained. If these r values, arranged in increasing order according to the index (j) are contiguous, the following procedure may be used.

For any $\delta \leq \delta_0^{(1)}$, the observed pair will be classified as MZ, while for any $\delta > \delta_0^{(r)}$, the pair will be classified as DZ. No classification shall be assigned if $\delta_0^{(1)} < \delta \leq \delta_0^{(r)}$, but in our experience the unique value $\delta_0 = 11$ has been obtained, being

$$P(11) = 0.86$$

On the basis of these results, we suggest that a twin pair be classified as follows:

MZ, if
$$\Delta \leq 11$$
 DZ, if $\Delta > 11$.

The error of classification may be estimated in the range of 0.14.

V. Discussion and Conclusions

The qualitative analysis has shown:

1. A significantly higher concordance in MZ than in DZ twin pairs. The hypothesis of genetic conditioning thus appears fully supported.

2. A remarkable variability of single finger concordance values. Individual genetic conditioning, for single finger patterns, may thus be inferred.

3. Absence of significant influence of handedness and sex. The analysis by zygosity only, irrespective of sex, thus appears justified.

The quantitative analysis on cumulative values has shown:

1. Significantly higher correlations in MZ (~ 1) than in DZ ($\sim 0.3-0.7$) twin pairs. The hypothesis of genetic conditioning thus appears fully supported.

2. Much more limited confidence intervals in MZ than in DZ twin pairs. Almost complete genetic conditioning may thus be inferred.

3. Absence of significant influence of handedness and sex. The analysis of TFRC irrespective of sex thus appears justified.

The quantitative analysis on single values, although less extensive, has apparently yielded quite similar results to the ones of cumulative values. Also taking into account the fact that random variability must obviously be higher in single than in cumulative values, individual genetic conditioning, for single finger values, may thus be inferred.

In conclusion, our results clearly support the view of a practically complete genetic conditioning of digital dermatoglyphics. Rather than at a cumulative level for the ten fingers, as is largely believed, the latter appears to act, however, on single finger quali-quantitative traits. Actually, TFRC would hardly appear to be a trait as such, and should rather be considered as a useful, but artificial cumulative value, with a reduced random variability, and summarizing the single finger actual traits. As such we have used it in our discriminant method, which, yielding a single discriminant value between MZ and DZ twins, may provide a useful and simple tool for the diagnosis of zygosity, especially in large twin samples.

Summary

A twin study was undertaken with the twofold aim (a) of studying the hereditary behaviour of digital dermatoglyphic traits both at the qualitative and quantitative level, and (b) of working out a method for discriminating MZ and DZ twins by means of fingerprints.

Fingerprints of 50 MZ (25 \circlearrowleft and 25 \bigcirc) and 50 DZ (25 \circlearrowright and 25 \bigcirc) twin pairs were thus examined and analyzed by means of a special methodology and of a 7044/K32 IBM computer.

The qualitative analysis has shown a significantly higher concordance in MZ than

in DZ twin pairs, with a certain variability of single finger concordance values. The *quantitative* analysis has shown significantly higher correlation values in MZ than in DZ twin pairs, with very limited confidence intervals in the former. Single ridge counts apparently behave as cumulative counts on the five or ten fingers, although with an obviously higher random variability.

Digital dermatoglyphics thus appear to show practically complete genetic conditioning, which, rather than at a cumulative level for the ten fingers, as is largely believed, appears to act on *single finger* quali-quantitative traits. The total finger ridge count, rather than a trait, only appears to be a useful, but artificial cumulative value. Actually, applied to the diagnosis of zygosity, it provides, by itself, a fairly high, general probability (0.86) of a correct diagnosis.

References

- ALLEN G. (1960). The M quadruplets. II The interpretation of quantitative differences. A.Ge.Me.Ge., 9: 452.
 (1968). Diagnostic efficiency of fingerprint and blood group differences in a series of twins. A.Ge.Me.Ge.
 17: 359.
- FISHER R. A. (1921). On the probable error of the correlation coefficient with small sample. Metron, 1: 4. GEDDA L., BRENCI G. (1961). Valutazione e critica del metodo differenziale di Weinberg per la diagnosi di zigotismo. Proceed. 2nd Internat. Congr. Hum. Genet., Roma. 1963.

HAUGE M., HARVALD B., FISCHER M., JENSEN G. K., NIELSEN N. J., RAEBILD I., SHAPIRO R., VIDEBECH T. (1968). The Danish twin register. A.Ge.Me.Ge., 17: 315.

- HOLT S. B. (1957). Quantitative genetics of dermal ridge-patterns of fingers. Proceed. Ist Internat. Congr. Hum. Genet., Acta Genet. Basel, 6: 473.
- (1961a). The inheritance of dermal ridge patterns. In L.S. Penrose: Recent Advances in Human Genetics. Churchill, London.
- (1961b). Quantitative genetics of finger-print patterns. Brit. Med. Bull., 17: 247.
- KENDALL M. G., STUART A. (1962). The Advanced Theory of Statistics. G. Griffin & Co., London.

LEVENE H. (1949). On a matching problem arising in genetics. Ann. Mathemat. Statist., 20.

MAYNARD-SMITH S., PENROSE L. S. (1955). Monozygotic and dizygotic twin diagnosis. Ann. Hum. Genet., 19: 273.

— — SMITH C. A. B. (1961). Mathematical Tables for Research Workers in Human Genetics. Churchill, London. McDonald A. D. (1964). Mongolism in twins. J. Med. Genet., 1: 39.

- NADDEO A. (1960). Contributi alla Teoria Statistica del Campione. Milano.
- LANDENNA G. (1966). Metodi Statistici nella Ricerca Scientifica e nella Programmazione Industriale. I and II., Milano.
- NIXON W. L. B. (1956). On the diagnosis of twin pair ovularity and the use of dermatoglyphic data. In L. Gedda: Novant'Anni delle Leggi Mendeliane. Ed. Ist. Mendel, Roma.
- PARISI P., DI BACCO M. (1967). Le impronte digitali nei gemelli. A.Ge.Me.Ge., 16: 71.

SLATER E. (1963). Diagnosis of zygosity by fingerprints. Acta Psychiat. Scand., 39: 78.

- SLATER P., SHIELDS J., SLATER E. (1964). A quadratic discriminant of zygosity from fingerprints. J. Med. Genet., 1: 142.
- STOLLER D. S. (1954). Univariate two-population distribution. Free discrimination J. Amer. Statist. Ass., 49.
- WENDT G. G. (1955). Der individuelle Musterwert der Fingerleisten und seine Vererbung. A.Ge.Me.Ge., 4: 330.
- WENINGER M. (1964). Zur "polygenen" (additiven) Vererbung des quantitativen Wertes der Fingerbeerenmuster. Homo, 15: 96.
- W.H.O. (1966). The use of twins in epidemiological studies. Report of Investigators on Methodology of Twin Studies. A.Ge.Me.Ge., 15: 111.

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APPENDIX *

Automatic procedure for testing the qualitative hypotheses

From a numerical point of view the test of the qualitative hypothesis proposed in II.1 can be split up into the following phases:

A. Input operation and initialization of auxiliary quantities;

B. Search for the configurations [1.1] subject to the restrictions [1.3];

C. Computation of [1.2] for each configuration and cumulation of its successive values for obtaining [1.4];

D. Cumulation of the [1.4] values, comparison with the significance level and output operation, which are however closely interdependent one with the other as evidenced by Fig. 1.

A. The following boxes of Fig. 1 are concerned with this phase:

Box 1: Control for end of data.

Box 2: The following input quantities are required (the corresponding symbols used in II.1 are to be found, if any, in the second member):

N1 = number of attributes. In our own case it is 5;

K(I) = Dr number of concordances observed with respect to finger D; ALPHA = level of significance;

SINT = logical variable conditioning the output;

- = T synthetic output;
- = F analytical output;
- $Z(I) = {}_{D}Z_{1}$ number of fingerprints possessing the ith attribute.

The variable FORMAT to read-in the above quantities must be expressed by means of the variables FRM and FOR.

- Box 3: The main auxiliary quantities are:
 - NC = n number of twin pairs examined;

 $KSUP = _{D}R$ maximum number of concordances for finger D;

NC2 = number of individuals examined.

 $F = {}_{D}F_{r}$ vector containing the configurations [1.1]

- Box 4: Subroutine PRIM generates all I prime numbers not greater than NMAX and stores them into the NP vector. They will be utilized later in phase C. More details are given in Fig. 2.
- B. In order that the application of the program should not be confined only to populations whose members exhibit five attributes provision has been made for N1 to be assigned any integer value greater than I during the input phase. This has substantially affected the translation of this phase into FORTRAN IV language as such generalization does not permit us to know at the programming stage the number of routines which are nec-

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essary for describing the search process of the configurations ${}_{D}F_{r}$ (Parisi and Di Bacco, 1967, II.2).

The problem has been solved by means of only one routine to be performed at the different levels which are necessary for searching one individual configuration and to be repeated again and again for as many cycles as are the configurations satisfying [1.3]. For a better understanding of the above procedure and for enphasizing its salient aspects, the operations indicated in Boxes 5, 6 and 7 of Fig. 1 have been represented in detail on Figs. 3 and 4.

C. It is useful for computational purposes to consider [1.2] as the quotient of P_1 by P_2 , where

$$P_{1} = \frac{n!}{(2n)!} 2^{n} - p^{r} \prod_{i=r}^{5} DZ_{i}!$$
$$P_{2} = \prod_{i \leq j} f_{ij}!$$

and

in that only P_1 varies as a function of the configuration ${}_DF_r$ under consideration. Bearing in mind that P_1 and P_2 may always be expressed as products of powers of distinct positive integers not greater than 2n and n respectively, the value of the exponent of the generic base i has been assigned, for each power belonging to P_1 to the ith element of vector INIZ. Subsequently, for each configuration ${}_DF_r$ generated in phase B, the elements of vector IFACT have been equated to the corresponding ones of INIZ and the exponent of the power of the generic base i in P_1 has been subtracted from the ith element of the former vector. Hence, in order to minimize the loss of significant digits in the computation of the product of powers represented by IFACT, the latter vector has been simplified by transferring (with the aid of the prime numbers generated by the PRIM subroutine) the value of its elements whose serial number is not prime to those indicated by factoring the latter.

In this manner, all non-prime elements of IFACT are set to zero and will not be considered for the purpose of the computation of [1.2].

The operations described in boxes 8 and 9 of Fig. 1, whose details are explained by Fig. 5, refer to the present phase.

- D. The following boxes of Fig. 1 belong to this phase:
 - Box 10: Cumulation of [1.4] values as $_{Dr}$ increases from its initial value to $_{DR}$;
 - Box 11: Comparison between Dr and its maximum value;
 - Box 12: Comparison between [1.5] and ALPHA;
 - Box 13: If SINT = T in output only a judgement on the significance of the test performed is obtained. Furthermore, in the event of non-significant concordances, there will be a saving in the performance time.
 - If SINT = F in addition to the judgement as above, the probabilities relative to each $_{Dr}$ considered and their successive cumulation are obtained; Box 14: Step up of $_{Dr}$.

The statistical tests of the random association hypothesis have been carried out by an IBM 7044/32K computer.

This experience has revealed that the execution time is, for each test, a non-decreasing function of n and a non-increasing one of both _Dr and d, the latter being a dispersion measure of the papillary patterns frequencies. This measure is given by

$$d = \frac{\sum_{i=1}^{5} \left| DZ_{i} - m \right|}{5}$$

where m is the arithmetic mean of the ${}_{D}Z_{i}$.

The memory space required is approximately of $\frac{5}{2}$ (N1 + 1) N1 + 3 N1 + 5n + 3150 rds. words.

In the following pages the source program has been entirely reported in Fortran IV language.

C SUBROUTINE FOR GENERATING PRIME NUMBERS	PR I M0002 PR I M0003
SUBROUTINE PRIM(NMAX+NP+I)	PRIMODO4
DIMENSION NP(1)	PR IM0005
NP(1)=2	PR I MOOO6
NP(2)=3	PRIMODO7
NP(3)=5	PR IM0008
I=2	PRIM0009
NN = 1	PRIMO010
10 DO 50 K=4,6,2	PRIMO011
NC DM=NN+K	PR IMOO12
COM=NCOM	PRIMOD13
NS=SQRT(COM)	PRIMOO14
J≃3	PRIMO015
20 IF(NP(J).GT.NS) GOTO 40	PRIMOD16
IF(MOD(NCOM,NP(J)).EQ.0) GDTO 50	PRIMOO17
30 J=J+1	PRIMO018
GOTO 20	PRIMO019
40 IF(NCOM.GT.NMAX) RETURN	PRIMO020
I = I + 1	PR IM0021
NP(I)=NCOM	PRIMO022
50 CONTINUE	PR IM0023
NN=NCOM	PRIMOO24
GOTO 10	PRIMO025
END	PRIMOO26

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с с с	FPBT PROGRAM FOR THE STATISTICAL TEST OF THE HYPOTESES OF CONCORDANC BETWEEN THE PAPILLARY PATTERNS OF MZ AND DZ TWINS	FPBT0001 E FPBT0002 FPBT0003
С	1 FORMAT(12A6)	FPBT0004 FPBT0005
	3 FORMAT(/////12X,9HNUMBER OF,31X,10HCUMULATIVE/)	FPBT0006
	<pre>4 FURMAT(1H1///1X,12A6///) 5 FORMAT(10X,12HCUNCORDANCES,9X,13HPROBABILITIES,7X,13HPROBABILITI</pre>	ESEPBT0008
	*////)	FPB10009
	8 FORMAT(/////1X,34HSIGNIFICANT CONCORDANCES AT LEVEL ,F5.2////	FPBT0010
	9 FORMAT(/////1X,38HNOT SIGNIFICANT CUNCORDANCES AT LEVEL ,F5.2//	/)FPBT0012
	LOGICAL SINT INTEGER 7(99).E(999).G(999)	FP810013
	DIMENSIUN N(99), J(99), K(999), INIZ(999), IFACT(999), LS(999), L(999)	,NFPBT0015
r	*P(99) ,NOME(12),FRM(12),FOR(12)	FPBT0016 FPBT0017
č	PHASE A	FPBT0018
С	PEAD(5,1) (EPM(1), 1=1,12)	FPBT0019 EPBT0020
	READ(5,1) (FOR(1),1=1,12)	FPBT0021
	10 READ(5,1) (NOME(I), $I=1,12$)	FPBT0022
	READ(5 , FOR) ($Z(I)$, $I=1$, NI)	FPBT0024
	WRITE(6,4) (NOME(I),I=1,12)	FPBT0025
	IF(SINI) GUTU 12 WRITE(6.3)	FPBT0026
_	WRITE(6,5)	FPBT0028
С	12 NC2=0	EPBT0029
	KSUP=0	FPBT0031
	DO 14 I=1,N1	FPBT0032
	L(I) = Z(I)/2	FPBT0034
	14 KSUP=KSUP+L(I)	FPBT0035
	NC=NC2/2	FPBT0037
	NC1=NC+1	FP8T0038
	PRR=0.	FPBT0039
_	CALL PRIM(NC2,NP,NTP)	FPBT0041
C C	PHASE C	FP810042
č		FPBT0044
	DO 16 I=3,NC2	FPBT0045 FPBT0046
	16 IF(I.GE.NC1) INIZ(I)=-1	FPBT0047
	INIZ(2)=NC-K(1)+1	FPBT0048 FPBT0049
	IF(Z(I).LT.2) GOTO 20	FPBT0050
		FPBT0051
	18 INIZ(JL) = INIZ(JL) + 1	FPBT0053
	20 CONTINUE	FPBT0054
	22 INIZ(2)=INIZ(2)=I PROB=0_	FPBT0055
С		FPBT0057
C C	PHASE B	FPBT0058 FPBT0059
Ŭ	DD 24 I=1,NT	FPBT0060
	24 F(I)=0	FPBT0061
	17-L	

Acta	Geneticae	Medicae	et	Gemel	llo	logiae
------	-----------	---------	----	-------	-----	--------

		MI=(M-1)*N1-(M-1)*(M-2)/2	FPBT0065
		MII=MI+1 MM=MII+1	FPB10066
		NNN=NN+MI	FPBT0068
		NS=NNN-1	FPBT0069
~		LS(MII) = L(MII)	FPBT0070
C	28	.1(M)=.1(M)+1	FPBI0071
		JM=J(M)+MI	FPBT0073
	30	JJ=JM+1	FPBT0074
	36	K(JJ)≈K(JM)-F(JM) TE(X(JJ) CE 1(JJ)) CO TO 40	FPBT0075
		LS(JJ)≈K(JJ)	FPBT0078
		GD TD 50	FPBT0078
	40	LS(JJ) = L(JJ)	FPBT0079
	50	1F(JM-LI-NS) GU TU 28 KI=K(NNN)-I(NNN)	EPBI0080
		IF(KL.GT.O) GOTD 90	FPBT0082
		IF(F(JM).LE.LS(JM)) GD TD 70	FPBT0083
	60	F (JM)=0	FPBT0084
		J(M)=J(M)-1 .IM=.I(M)+MT	FPBI0085
		IF(JM.GT.MI) GDTD80	FPBT0087
		M=M-1	FPBT0088
		IF(M.LE.O) GD TD 250	FPBT0089
		MI = (M-1) + N1 + (M-1) + (M-2) / 2	FPBT0090
		MII=MI+1	FPBT0092
		MM=MII+1	FPBT0093
			FPBT0094
		MS-MM-1 JM=J(M)+MI	FPBT0095
		GD TO 80	FPBT0097
~	70	F(NNN)=K(NNN)	FPBT0098
L		I SIIM=0	EPBT0100
		DO 110 I=MII,NNN	FPBT0101
		G(I)=L(I)-F(I)	FPBT0102
		IF(M.EQ.1) G(I)=Z(I)-2*(L(I)-G(I))	FPBT0103
		IF(I) = IG(I) GOTO 100 IF(G(I) = IF = IG(II) GOTO 110	FPB10104
	100	INDEX=1	FPBT0106
		ICOM=G(I)	FPBT0107
	110	ISUM=ISUM+G(I) IE(2+100M-ISUM) 130,150,80	FPBT0108
	130	G(INDEX) = G(MII)	FPBT0110
	2.00	DO 140 I=MM,NNN	FPBT0111
	• • •	II=I+NN-1	FPBT0112
	140	L(11)=G(1) K(NNN+1)=ICOM	FPBIULI3
		M=M+1	FPBT0115
		N(M)=NN-1	FPBT0116
		GO TO 26	FPBT0117
	100	DO 160 TEMM.NNN	FPBT0119
		II = I + NN - 1	FPBT0120
	160	F(II)=G(I)	FPBT0121
ç			FPBT0122
с С		PHASE C	FPBT0123
v			

DD 190 1=2,NC2 FPBT01 190 TFACT(1)=INT2(1) FPBT01 DC 201 1=1,11 FPBT01 LV=F(1) FPBT01 DC 200 J=2,LV FPBT01 200 TFACT(JL)=TACT(JL)=1 FPBT01 200 TFACT(JL)=1 FPBT01 C FPBT01 PR=1. FPBT01 D0 200 JL=2,LV FPBT01 210 CONTINUE FPBT01 C FPBT01 PR=1. FPBT01 D0 230 JL=1,NTP FPBT01 TP=NP(JL) FPBT01 STP2/IP+IP FPBT01 JS=C2/IP+IP FPBT01 JS=1+IP2 FPBT01				
190 IFACT(1)=INIZ(1) FPBT01 00 210 1=1,II FPBT01 190 10 11 FPBT01 190 200 1=2,LV FPBT01 200 TFACT(JL)=IFACT(JL)-1 FPBT01 100 230 JL=1,NTP FPBT01 110 TFAPT0 FPBT01 111 TFAPT0 FPBT01 112 TFAPT0 FPBT01 111 TFAPT0 FPBT01 111 TFACT(JD)=IFACT(JD)+IFACT(JJI) FPBT01 112 TFACT(JL)= FPBT01 114 TFACT(JL)= FPBT01 115 TFACT(JL)= FPBT01 116 TFACT(JL)= FPBT01 116 TFACT(JL)= FPBT01 116 TFACT(JL)= FPBT01			D0 190 I=2,NC2	FPBT0125
D0 210 1=1,11 IF(F(1).LT.2) GOTO 210 LV=F(1) D0 200 JL=2,LV 200 TFACT(JL)=1FACT(JL)=1 210 CONTINUE C PR=1. D0 230 JL=1,NTP PR=10 R[P=1P, R[R[P], R[P=1P,		190	IFACT(I)=INIZ(I)	FPBT0126
<pre>IF(F(I).LT.2) GOTO 210 LV=F(I) DO 200 JL=2,LV FPBT01 FPBT01 DD 200 JL=2,LV FPBT01 200 IFACT(JL)=IFACT(JL)-1 FPBT01 FPBT01 FPBT01 DD 230 JL=1,NTP FPBT01 DD 230 JL=1,NTP FPBT01 FPBT01 FPPT0 IF=1P FPBT01 JS=NC2/IP+1P JS=NC2/IP+1P JS=NC2/IP+1P JI=JS=1+1P2 FPBT01 FPBT01 FPAT01 FPBT01 FFBT01 FFBT</pre>		-	DO 210 I=1+II	FPBT0127
Lv=F(1) FPBT01 D0 200 JL=2,LV FPBT01 200 TACT(JL)=FACT(JL)=1 FPBT01 210 CONTINUE FPBT01 C FPBT01 D0 230 JL=1,NTP FPBT01 TP=NP(JL) FPBT01 RIP=IP FPBT01 JS=NC2/IP+IP FPBT01 JS=NC2/IP+IP FPBT01 JS=NC2/IP+IP FPBT01 JS=NC2/IP+IP FPBT01 JS=NC2/IP+IP FPBT01 JS=SNC2/IP+IP FPBT01 JS=SNC2			IF(F(1).LT.2) GOTO 210	FPBT0128
DD 200 JL=2,LV FPBT01 210 CT(JL)=IFACT(JL)-1 FPBT01 210 CONTINUE FPBT01 C FPBT01 FPBT01 DD 230 JL=1,NTP FPBT01 DD 230 JL=1,NTP FPBT01 IP=NF(JL) FPBT01 FPBT01 JD=21P+IP FPBT01 FPBT01 JS=NC2/IP+IP FPBT01 FPBT01 JJ=JS=I+IP2 FPBT01 JD=J/IP JD=J/IP FPBT01 FPBT01 IFACT(JD)=IFACT(ID)+IFACT(JI) FPBT01 IFACT(JD)=IFACT(ID)+IFACT(JI) FPBT01 IFACT(JD)=IFACT(ID)+IFACT(JI) FPBT01 220 IFACT(JD)=IFACT(ID) FPBT01 PR0B=PR0B+PR FPBT01 FPBT01 C PHASE B FPBT01 C PHASE B FPBT01 C PHASE D FPBT01 IF(IN)+INAL FPBT01 FPBT01 GO TD 36 FPBT01 FPBT01 C PHASE D			LV=F(I)	FPBT0129
200 TFACT(JL)=TFACT(JL)-1 FPBT01 210 CONTINUE FPBT01 210 CONTINUE FPBT01 00 230 J=1,NTP FPBT01 00 230 J=1,NTP FPBT01 00 230 J=1,NTP FPBT01 1P=NPJU1 FPBT01 FPBT01 1P=21P+1P FPBT01 FPBT01 JS=NC2/1P+1P FPBT01 FPBT01 JJ=3J=S-1+2P FPBT01 FPBT01 JJ=3J=1+1P FPBT01 FPBT01 JJ=3J=1+1P FPBT01 FPBT01 JJ=3J=1+1P FPBT01 FPBT01 JD=3I/IP FPBT01 FPBT01 JD=3I/IP FPBT01 FPBT01 IFACT(JD)=IFACT(ID)+IFACT(JI) FPBT01 IFACT(JD)=FPAR*IP*IFACT(ID) FPBT01 220 FFACT(JD)+IFACT(JI) FPBT01 220 IFACT(JD)+IFACT(JD) FPBT01 C PHASE FPBT01 C PHASE FPBT01 C			$DD 200 JL = 2 \cdot LV$	FPBT0130
210 CONTINUE FPBT01 C FPBT01 FPBT01 DD 230 JL=1,NTP FPBT01 IP=NP(JL) FPBT01 FPBT01 RIP=IP FPBT01 FPBT01 JD JS=NC2/IP=IP FPBT01 JS=NC2/IP=IP FPBT01 FPBT01 JJS=NC2/IP=IP FPBT01 FPBT01 JJS=JS=I+IP2 FPBT01 FPBT01 JDS=J/IP FPBT01 FPBT01 IFACT(JJ)==IFACT(JD)+IFACT(JI) FPBT01 FPBT01 Z20 IFACT(JN)=IFACT(IP) FPBT01 FPBT01 PROB FPBT01 FPBT01 FPBT01 D TO I=MN+NN FPBT01 ITO FIASE FPBT01 FPBT01 D FO FPBT01 </td <td></td> <td>200</td> <td>IFACT(JL)=IFACT(JL)-1</td> <td>FPBT0131</td>		200	IFACT(JL)=IFACT(JL)-1	FPBT0131
C PR=1. FPBT01 DD 230 JL=1,NTP FPBT01 TP=NP(JL) FPBT01 RTP=TP FPT0 FPBT01 JS=NC2/IP+TP FPT0 FPBT01 JS=NC2/IP+TP FPT01 JS=NC2/IP+TP FPT01 JS=ST+TP2 FPT01 JS=JS-T+TP2 FPBT01 JD=JJ/IP FPT01 IFACT(JD)=TFACT(ID)+TFACT(JI) FPBT01 IFACT(JD)=TFACT(JD)+TFACT(JI) FPBT01 220 FFACT(JD)=TFACT(JP) FPBT01 PROB=PR0B+PR FRFATCT(TP) FPBT01 C PHASE B FPBT01 TI=T+NN-1 FPBT01 IF(JM)-LS(JM))30,30,60 FPBT01 IF(JM)=F(JM)+KL FPBT01 C PHASE D FPBT01 C PHASE D FPBT01 IF(JM)-LS(JM))30,30,60 FPBT01 C PHASE D FPBT01 IF(F,JM)-LS(JM))30,30,60 FPBT01 C PHASE D FPBT01 C PHA		210	CONTINUE	FPBT0132
PR=1. FPBT01 DD 230 JL=1,NTP FPBT01 IP=NP(JL) FPBT01 RIP=IP FPBT01 JS=NC2/IP+IP FPBT01 JD=J/IP FPBT01 FD FPBT01 CO PHASE B CO PHASE B CO PHASE CO PHASE <	c			FP8T0133
DD 230 JL=1,NTP FPBT01 IP=NP(JL) FPBT01 RIP=IP FPBT01 J2=IP+IP FPBT01 JS=NC2/IP+IP FPBT01 JS=Stars FPBT01 JS=Stars FPBT01 JS=Stars FPBT01 JS=Stars FPBT01 JD=JI/IP FPBT01 FACT(JD)=IFACT(JD)+IFACT(JI) FPBT01 C FPBT01 Stars FPBT01 PROB=PR+RIP+*IFACT(IP) FPBT01 PROB=PR+RIP+*IFACT(IP) FPBT01 C PHASE B FPBT01	Ŭ		PR=1.	FPBT0134
IP=NP(JL) FPBT01 RIP=IP FPBT01 IP=2IP+IP FPBT01 JS=NC2/IP*IP FPBT01 IF(1P2.GT.JS) GUT0 230 FPBT01 D0 220 I=IP2,JS,IP FPBT01 JD=J/IP FPBT01 IFACT(IP)=IFACT(IP)+IFACT(JI) FPBT01 IFACT(ID)=IFACT(JD)+IFACT(JI) FPBT01 220 IFACT(JI)=0 FPBT01 220 IFACT(JI)= FPBT01 PR0B=PR0B+PR FPBT01 C PHASE B FPBT01 D0 170 I=MM,NNN FPBT01 II=I+NN-1 FPBT01 II=I+NN-1 FPBT01 IFF(JM)+LS(JM))30,30,60 FPBT01 90 F(JM)=F(JM)+XL FPBT01 GO 10 36 FPBT01 C PHASE D FPBT01 <			DO 230 JI =1.NTP	EPBT0135
RIP:IP FPBT01 IP2=IP+IP FPBT01 JS=NC2/IP*IP FPBT01 IF(IP2=GT.JS) GOTD 230 FPBT01 D0 220 I=IP2,JS,IP FPBT01 JD=JI/IP FPBT01 JD=JI/IP FPBT01 IFACT(JD)=IFACT(IP)+IFACT(JI) FPBT01 IFACT(JD)=IFACT(JD)+IFACT(JI) FPBT01 220 IFACT(JD)=IFACT(IP)+IFACT(JI) FPBT01 230 RP=RPR*RIP*IFACT(IP) FPBT01 PROB=PROB+PR FPBT01 C PHASE B FPBT01 D0 170 I=MM,NNN FPBT01 II=I+NN-1 FPBT01 IS0 F(JM)=F(JM)+1 FPBT01 ITO F(II)=0 FPBT01 S0 F(JM)=F(JM)+1 FPBT01 IF(F(JM)-LS(JM))30,30,60 FPBT01 G0 ID 36 FPBT01 C PHASE D FPBT01			TP=NP(.11)	EPBT0136
IP2=IP+IP FPBT01 JS=NC2/IP*IP FPBT01 JS=NC2/IP*IP FPBT01 IF(IP2.GT.JS) GUTD 230 FPBT01 D0 220 I=IP2,JS,IP FPBT01 JD=J/IP FPBT01 JD=J/IP FPBT01 IFACT(IP)=IFACT(IP)+IFACT(JI) FPBT01 IFACT(JD)=IFACT(JD)+IFACT(JI) FPBT01 220 IFACT(JD)=IFACT(IP) FPBT01 PROB=PR0B+PR FPBT01 C PHASE B FPBT01 C PHASE B FPBT01 D0 170 I=MM,NNN FPBT01 FPBT01 II=I+NN-1 FPBT01 FPBT01 ITO F(IN)=C(JM)+1 FPBT01 FPBT01 S0 F(JM)=F(JM)+1 FPBT01 FPBT01 G0 ID 36 FPBT01 FPBT01 C PHASE D FPBT01 G0 ID 36 FPBT01 FPBT01 C PHASE D FPBT01 S250 PRR=PR0B+PRR FPBT01 FPBT01 IF(SINI) GOTO 254 FPBT01 FPBT01 S250 PRR=PR0B+PRR FPBT01 FPBT01 S254 IF(PRR.LT.ALPHA) GOTO 260 FPB			RIP=IP	EPBT0137
JS=NC2/IP+IP FPBT01 JS=NC2/IP+IP FPBT01 IF(1P2.GT.JS) GUTD 230 FPBT01 DC 220 I=P2,JS,IP FPBT01 JD=JI/IP FPBT01 IFACT(JD)=IFACT(IP)+IFACT(JI) FPBT01 IFACT(JD)=IFACT(JD)+IFACT(JI) FPBT01 IFACT(JD)=IFACT(JD)+IFACT(JI) FPBT01 220 FACT(JD)=FACT(JD)+IFACT(JI) FPBT01 230 PR=PR+RIP+*IFACT(IP) FPBT01 PROB=PROB+PR FPBT01 C PHASE B FPBT01 D0 170 I=MM,NNN FPBT01 II=I+NN-1 FPBT01 IT=F(F(JM)+LS(JM))*1 FPBT01 S0 F(JM)=F(JM)+1 FPBT01 G0 TD 36 FPBT01 C PHASE D FPBT01 G0 TD 36 FPBT01 C PHASE D FPBT01 C <td< td=""><td></td><td></td><td>IP2=IP+IP</td><td>FPBT0138</td></td<>			IP2=IP+IP	FPBT0138
IF(1P2,GT.JS) GUTD 230 FPBT01 DC 220 I=P2,JS,IP FPBT01 JJ=JS-I+IP2 FPBT01 JD=J/1P FPBT01 IFACT(IP)=IFACT(IP)+IFACT(JI) FPBT01 IFACT(JD)=IFACT(JD)+IFACT(JI) FPBT01 PR05 FPBT01 C PHASE B FPBT01 C PHASE B FPBT01 C PHASE B FPBT01 C PHASE B FPBT01 C PHASE D FPBT01 <			IS=NC2/IP+TP	EPBT0139
D0 220 I=IP2, JS, IP FPBT01 JI=JS-I+IP2 FPBT01 JD=JJ/IP FPBT01 IFACT(JD)=IFACT(JD)+IFACT(JI) FPBT01 1FACT(JD)=IFACT(JD)+IFACT(JI) FPBT01 220 IFACT(J1)=0 FPBT01 230 PR=PR*RIP**IFACT(IP) FPBT01 PROB=PR0B+PR FPBT01 C PHASE B FPBT01 II=I+NN-1 FPBT01 10 I70 I=MM,NNN FPBT01 II=I+NN-1 FPBT01 10 I70 F(II)=0 FPBT01 90 F(JM)=F(JM)+1 FPBT01 10 F(II)=0 FPBT01 90 F(JM)=F(JM)+1 FPBT01 10 G0 TD 36 FPBT01 11 F(F(JM)-LS(JM))30,30,60 FPBT01 90 F(JM)=F(JM)+KL FPBT01 11 F(F(JM)-LS(JM))30,30,60 FPBT01 12 G0 TD 36 FPBT01 12 C PHASE D FPBT01 130 F(JM)=F(JM)+KL FPBT01 141 F(ST1) FPDBT01 FPBT01 150 F(JM)=F(JM)+KL FPBT01 FPBT01 150 F(JM)=F(JM)+KL FPBT01 FPBT01 150 KT1E(S,F) ALPHA <td></td> <td></td> <td>1E(102-GT. 15) GOTO 230</td> <td>EPBT0140</td>			1E(102-GT. 15) GOTO 230	EPBT0140
J1=JS-1+IP2 FPBT01 J0=JI/IP FPBT01 IFACT(ID)=IFACT(ID)+IFACT(JI) FPBT01 IFACT(JD)=IFACT(JD)+IFACT(JI) FPBT01 220 IFACT(JD)= FPBT01 230 PRP*R*IFACT(IP) FPBT01 230 PRP*R*IFACT(IP) FPBT01 230 PRP*R*IFACT(IP) FPBT01 230 PRP*R*IFACT(IP) FPBT01 C PHASE B FPBT01 C PHASE B FPBT01 170 F(II)=0 FPBT01 30 F(JM)=F(JM)+1 FPBT01 170 F(IJ)=0 FPBT01 30 F(JM)=F(JM)+1 FPBT01 170 F(IJ)=0 FPBT01 30 F(JM)=F(JM)+1 FPBT01 171 IF(F(JM)-LS(JM))30,30,60 FPBT01 30 F(JM)=F(JM)+KL			$DO 220 I = IP2 \cdot IS \cdot IP$	EPBT0141
J0=JI/IP FPBT01 IFACT(IP)=IFACT(IP)+IFACT(JI) FPBT01 IFACT(JD)=IFACT(JD)+IFACT(JI) FPBT01 220 IFACT(JD)=IFACT(JD)+IFACT(JI) FPBT01 230 PR=PR*RIP**IFACT(IP) FPBT01 PROB=PROB+PR FPBT01 FPBT01 C PHASE B FPBT01 C PHASE B FPBT01 IT=I+NN=1 FPBT01 FPBT01 170 F(JM)=F(JM)+1 FPBT01 171 F(F(JM)-LS(JM))30,30,60 FPBT01 172 GO TD 36 FPBT01 173 F(JM)=F(JM)+KL FPBT01 174 FPBT01 FPBT01 175 KITE(6,7) K(1), PD0B,PRR FPBT01 174 FPBT01 FPBT01 175 MRITE(6,7) ALPHA FPBT01			JT = IS - I + TP2	EPRT0142
IFACT(IP)=IFACT(JD)+IFACT(JI) FPBT01 IFACT(JD)=IFACT(JD)+IFACT(JI) FPBT01 220 IFACT(JD)=IFACT(JD)+IFACT(JI) FPBT01 230 PR=PRT+TFACT(IP) FPBT01 PROB=PROB+PR FPBT01 C PHASE B FPBT01 II=1+NN-1 FPBT01 II=1+NN-1 FPBT01 10 F(JM)=F(JM)+1 FPBT01 170 F(II)=0 FPBT01 80 F(JM)=F(JM)+1 FPBT01 170 F(IM)=F(JM)+1 FPBT01 171 F(F(JM)+1 FPBT01 172 F(JM)=F(JM)+1 FPBT01 173 F(JM)=F(JM)+1 FPBT01 174 F(FFR, JM)+1 FPBT01 175 F(JM)=F(JM)+1 FPBT01 176 F(JM)=F(JM)+KL FPBT01 177 F(JM)=F(JM)+KL FPBT01 178 FPBT01 FPBT01 179 FPBT01 FPBT01 179 FPBT01 FPBT01 170 FPBT01 FPBT01 170 F(I)=F,PR FPBT01				EPRT0143
IFACT(JD)=IFACT(JD)+IFACT(JI) FPBT01 220 IFACT(JD)=FACT(JP) FPBT01 230 PR=PR=RIP=*IFACT(IP) FPBT01 PROB=PROB+PR FPBT01 C PHASE B FPBT01 C PHASE B FPBT01 D0 170 F(I1)=0 FPBT01 170 F(I1)=0 FPBT01 FPBT01 30 F(JM)=F(JM)+1 FPBT01 FPBT01 170 F(I1)=0 FPBT01 FPBT01 80 F(JM)=F(JM)+1 FPBT01 FPBT01 170 F(I1)=0 FPBT01 FPBT01 80 F(JM)=F(JM)+1 FPBT01 FPBT01 170 F(I1)=0 FPBT01 FPBT01 80 F(JM)=F(JM)+KL FPBT01 FPBT01 GO TD 36 FPBT01 FPBT01 C PHASE D FPBT01 C PHASE D <td></td> <td></td> <td>16ACT/10)=16ACT/10)+16ACT(11)</td> <td>EPBT0144</td>			16ACT/10)=16ACT/10)+16ACT(11)	EPBT0144
220 IFACT(J)=0 FPBT01 230 PR=PR*RIP**IFACT(IP) FPBT01 PR0B=PR0B+PR FPBT01 C PHASE B FPBT01 C PHASE B FPBT01 D0 170 I=MM,NNN FPBT01 II=I+NN-1 FPBT01 FPBT01 170 F(II)=0 FPBT01 80 F(JM)=F(JM)+1 FPBT01 170 F(IJ)=0 FPBT01 80 F(JM)=F(JM)+30,30,60 FPBT01 90 F(JM)=F(JM)+8L FPBT01 G0 10 36 FPBT01 C PHASE D FPBT01 250 PRR=PR0B+PRR FPBT01 C PHASE D FPBT01 C PHASE D FPBT01 250 PRE=PR0B+PRR FPBT01 COTO 260 FPBT01 FPBT01 <td></td> <td></td> <td>I = ACT(ID) = I = ACT(ID) + I = ACT(IT)</td> <td>EPBTO145</td>			I = ACT(ID) = I = ACT(ID) + I = ACT(IT)	EPBTO145
230 PR=PR*RIP**IFACT(IP) FPBT01 PR0B=PR0B+PR FPBT01 C PHASE B FPBT01 C PHASE B FPBT01 D0 170 I=MM,NNN FPBT01 II=I+NN-1 FPBT01 FPBT01 170 F(I)=0 FPBT01 80 F(JM)=F(JM)+1 FPBT01 90 F(JM)=F(JM)+1 FPBT01 GO ID 36 FPBT01 C PHASE D FPBT01 GO ID 36 FPBT01 C PHASE D FPBT01 <		220		EPATOLAS
PROB=PROB+PR FPBT01 C PHASE B FPBT01 C PBT01 FPBT01 D0 170 I=MM,NNN FPBT01 FPBT01 II=I+NN-1 FPBT01 FPBT01 170 F(II)=0 FPBT01 FPBT01 80 F(JM)=F(JM)+1 FPBT01 FPBT01 0 G0 T0 36 FPBT01 FPBT01 C PHASE D FPBT01 G0 T0 36 FPBT01 FPBT01 C PHASE D FPBT01 C PHASE D FPBT01 G0 T0 36 FPBT01 FPBT01 C PHASE D FPBT01 COTO 260 <t< td=""><td></td><td>220</td><td>PR=PR+RIP++IFACT(IP)</td><td>EP8T0147</td></t<>		220	PR=PR+RIP++IFACT(IP)	EP8T0147
C PHASE B FPBT01 C PHASE B FPBT01 C PHASE B FPBT01 C PFBT01 IT=I+NN-1 FPBT01 IT=I+NN-1 FPBT01 IT0 F(II)=0 FPBT01 B0 F(JM)=F(JM)+1 FPBT01 IF(F(JM)+LS(JM))30,30,60 FPBT01 G0 TD 36 FPBT01 G0 TD 36 FPBT01 C PHASE D FPBT01 C FP		2 50		EPBT0148
C PHASE B FPBT01 C D0 170 I=MM,NNN FPBT01 II=I+NN-1 FPBT01 170 F(II)=0 FPBT01 90 F(JM)=F(JM)+1 FPBT01 17(F(JM)-LS(JM))30,30,60 FPBT01 0 G0 TD 36 FPBT01 C PHASE D FPBT01 C PHASE D FPBT01 C PHASE D FPBT01 C PHASE D FPBT01 250 PRR=PR0B+PRR FPBT01 250 PRR=PR0B+PRR FPBT01 250 PRR=PR0B+PRR FPBT01 254 IF(SINT) G0T0 254 FPBT01 255 WRITE(6,7) K(1)+PR0B,PRR FPBT01 256 WRITE(6,7) ALPHA G0T0 260 FPBT01 256 WRITE(6,9) ALPHA FPBT01 260 K(1)=K(1)+1 FPBT01 1F(K(1)-LE.KSUP) G0T0 22 1F(PBT01 256 FPBT01 1F(K(1)-LE.KSUP) G0T0 256 FPBT01 1F(K) FPBT01 FPBT01 1F(K) FPBT01 FPBT01 1F(K) FPBT01 FPBT01 1F(K) FPBT01 FPBT01 1F(F) FPBT01 FPBT01 FPBT01 FPBT01 1F(F) FPBT01 FPBT01 FPBT01 FPBT01 1F(F) FPBT01 FPBT01 FPBT01 FPBT01 FPBT01 1F(F) FPBT01 FPB	r		TROB-TRODIER	EDBIO140
C FPBT01 D0 170 I=MM,NNN FPBT01 II=I+NN-1 FPBT01 170 F(II)=0 FPBT01 80 F(JM)=F(JM)+1 FPBT01 90 F(JM)=F(JM)+KL FPBT01 G0 TD 36 FPBT01 C PHASE D FPBT01 C PHASE D FPBT01 C PHASE D FPBT01 C PHASE D FPBT01 250 PRR=PRDB+PRR FPBT01 IF(SINT) G0T0 254 FPBT01 G0TD 260 FPBT01 254 IF(PRR.LT.ALPHA) G0T0 260 FPBT01 255 WRITE(6,9) ALPHA G0T0 260 FPBT01 260 K(1)=K(1)+1 FPBT01 IF(K(1).LE.KSUP) G0T0 22 FPBT01 IF(K1).LE.KSUP) G0T0 256 FPBT01 IF(K1).LE.KSUP) G0T0 256 FPBT01 IF(PRR.GE.ALPHA) G0T0 256 FPBT01 IF(PRR.GE.ALPHA) G0T0 256 FPBT01 IF(PRT01 FPBT01 C FPBT01 FPBT01 FPBT01 FP	č			EPST0150
C DD 170 I=MM,NNN FPBT01 II=I+NN-1 FPBT01 170 F(II)=0 FPBT01 80 F(JM)=F(JM)+1 FPBT01 IF(F(JM)-LS(JM))30,30,60 FPBT01 90 F(JM)=F(JM)+KL FPBT01 GO TD 36 FPBT01 C PHASE D FPBT01 C FPBT01 FPBT01 C FPBT01 FPBT01 COTO 10 FPBT01 FPBT01 IF(PR.GE.ALPHA) GOTO 256 FPBT01 IF(PR.GE.ALPHA) GOTO 256 FPBT01 IF(PR.GE.ALPHA) GOTO 256 <t< td=""><td>ř</td><td></td><td>THASE D</td><td>EPBT0151</td></t<>	ř		THASE D	EPBT0151
D0 110 1-100 AU 110 1 111 1+NN-1 FPBT01 170 F(11)=0 FPBT01 80 F(JM)=F(JM)+1 FPBT01 1F(F(JM)-LS(JM))30,30,60 FPBT01 90 F(JM)=F(JM)+KL FPBT01 GO TD 36 FPBT01 C PHASE D FPBT01 C PHASE D FPBT01 250 PRR=PR0B+PRR FPBT01 FPBT01 IF(SINT) GOTO 254 FPBT01 GOTO 260 WRITE(6,7) K(1), PROB, PRR FPBT01 GOTO 260 254 IF(PRR.LT.ALPHA) GOTO 260 FPBT01 SPBT01 256 WRITE(6,9) ALPHA FPBT01 FPBT01 GOTO 10 FPBT01 SPBT01 260 K(1)=K(1)+1 FPBT01 FPBT01 1F(FRR.GE.ALPHA) GOTO 22 FPBT01 IF(PRR.GE.ALPHA) GOTO 256 FPBT01 WRITE(6,8) ALPHA GOTO 256 FPBT01 GOTO 10 END FPBT01	Č		DO 170 T-MM. NNN	EPBT0152
170 F170 FPBT01 170 F(JM)=F(JM)+1 FPBT01 1F(F(JM)-LS(JM))30,30,60 FPBT01 90 F(JM)=F(JM)+KL FPBT01 GO TD 36 FPBT01 C PHASE FPBT01 250 PRR=PR0B+PRR FPBT01 GOTO 254 FPBT01 GOTO 260 FPBT01 GOTO 260 FPBT01 256 WRITE(6,9) ALPHA GOTO 22 GOTO 10 FPBT01 IF(K11)-LE-KSUP) GOTO 22 FPBT01 IF(K11)-LE-KSUP) GOTO 256 FPBT01 WITE(6,8) ALPHA GOTO 256 FPBT01 GOTO 10 FPBT01 EN				EDBT0152
10 F(JM)=F(JM)+1 FPBT01 90 F(JM)=F(JM)+KL FPBT01 G0 TD 36 FPBT01 C PHASE D FPBT01 C GOTO 254 FPBT01 GOTO 260 FPBT01 GOTO 260 254 IF(FRR.LT.ALPHA) GOTO 260 FPBT01 256 WRITE(6,9) ALPHA FPBT01 GOTO 10 FPBT01 FPBT01 1F(K(1)-LE.KSUP) GOTO 22 FPBT01 IF(PRR.GE.ALPHA) GOTO 256 FPBT01 WRITE(6,8) ALPHA GOTO 10 FPBT01 GOTO 10 FPBT01 FPBT01 END FPBT01 FPBT01 <td></td> <td>170</td> <td>E(II)=0</td> <td>EDBTO154</td>		170	E(II)=0	EDBTO154
IF(F(JM)-LS(JM))30,30,60 FPBT01 90 F(JM)=F(JM)+KL FPBT01 GO TD 36 FPBT01 C PHASE D FPBT01 C FPBT01 FPBT01 GOTD 260 FPBT01 GOTD 260 254 F(PRR.LT.ALPHA) GOTD 260 FPBT01 GOTD 10 FPBT01 FPBT01 260 K(1)=K(1)+1 FPBT01 IF(PRR.GE.ALPHA) GOTD 256 FPBT01 IF(PRR.GE.ALPHA) GOTD 256 FPBT01 WRITE(6,8) ALPHA FPBT01 GOTO 10 FPBT01 END FPBT01		110	F(11)+E(1N)+1	
11 (10) = (10) + KLFPBT01G0 TD 36FPBT01CPHASE DCFPBT01CFPBT01CFPBT01250 PRR=PR0B+PRRFPBT01IF (SINT) GOTO 254FPBT01wR1TE(6,7) K(1), PR0B, PRRFPBT01GOTD 260FPBT01254 IF (PRR.LT.ALPHA) GOTO 260FPBT01255 WR1TE(6,9) ALPHAFPBT01GOTO 10FPBT01260 K(1)=K(1)+1FPBT01IF (PRR.GE.ALPHA) GOTO 256FPBT01IF (PRR.GE.ALPHA) GOTO 256FPBT01IF (PRR.GE.ALPHA) GOTO 256FPBT01GOTO 10FPBT01IF (PRR.GE.ALPHA) GOTO 256FPBT01BODFPBT01		50	TELEL IN)-1 (LIN) 30.30.60	EPBT0156
GO TO 36 FPBTO1 GO TO 36 FPBTO1 C PHASE D FPBTO1 C PHASE D FPBTO1 C PHASE D FPBTO1 250 PRR=PRDB+PRR FPBTO1 FPBTO1 IF(SINT) GOTO 254 FPBTO1 WRITE(6,7) K(1),PROB,PRR FPBTO1 GOTO 260 FPBTO1 254 IF(PRR.LT.ALPHA) GOTO 260 FPBTO1 256 WRITE(6,9) ALPHA GOTO 260 GOTO 10 FPBTO1 260 K(1)=K(1)+1 FPBTO1 IF(PR.GE.ALPHA) GOTO 22 FPBTO1 IF(PR.GE.ALPHA) GOTO 256 FPBTO1 END FPBTO1		00		EPRT0157
GO TH JO FPBT01 C FPBT01 C FPBT01 250 PRR=PR0B+PRR FPBT01 IF(SINT) GOTO 254 FPBT01 WR1TE(6,7) K(1),PR0B,PRR FPBT01 GOTO 260 FPBT01 254 IF(PRR.LT.ALPHA) GOTO 260 FPBT01 256 WRITE(6,9) ALPHA FPBT01 GOTO 10 FPBT01 260 K(1)=K(1)+1 FPBT01 IF(KK1).LE.KSUP) GOTO 22 FPBT01 IF(PRR.GE.ALPHA) GOTO 256 FPBT01 WRITE(6,8) ALPHA GOTO 10 GOTO 10 FPBT01 IF(PRT.GE.ALPHA) GOTO 256 FPBT01 IF(PRT.GE.ALPHA) GOTO 256 FPBT01 WRITE(6,8) ALPHA GOTO 10 END FPBT01		90		EP810158
C PHASE D FPBT01 C PHASE D FPBT01 250 PRR=PR0B+PRR FPBT01 IF(SINT) GOTO 254 FPBT01 WRITE(6,7) K(1),PR0B,PRR FPBT01 GOTO 260 FPBT01 256 WRITE(6,9) ALPHA GOTO 260 GOTO 10 FPBT01 260 K(1)=K(1)+1 FPBT01 IF(KR.LT.ALPHA) GOTO 22 FPBT01 260 K(1)=K(1)+1 FPBT01 IF(KR.LT.ALPHA) GOTO 22 FPBT01 IF(KR.GE.ALPHA) GOTO 256 FPBT01 IF(PRR.GE.ALPHA) GOTO 256 FPBT01 WRITE(6,8) ALPHA FPBT01 GOTO 10 FPBT01 END FPBT01	r		00 18 50	EPBT0159
C FPBT01 250 PRR=PRDB+PRR FPBT01 IF(SINT) GOTO 254 FPBT01 WRITE(6,7) K(1),PRDB,PRR FPBT01 GOTO 260 FPBT01 254 IF(PRR.LT.ALPHA) GOTO 260 255 IF(PRR.LT.ALPHA) GOTO 260 256 WRITE(6,9) ALPHA GOTO 10 FPBT01 260 K(1)=K(1)+1 IF(PR.GE.ALPHA) GOTO 22 IF(PRR.GE.ALPHA) GOTO 256 WRITE(6,8) ALPHA GOTO 10 FPBT01 IF(PRR.GE.ALPHA) GOTO 256 WRITE(6,8) ALPHA GOTO 10 FPBT01 IF(PRR.GE.ALPHA) GOTO 256 WRITE(6,8) ALPHA GOTO 10 FPBT01 END FPBT01	ř		PHACE D	EPRIOIS
250 PRR=PR0B+PRR FPBT01 IF(SINT) GOTO 254 FPBT01 wRITE(6,7) K(1),PR0B,PRR FPBT01 GOTO 260 FPBT01 254 IF(PRR.LT.ALPHA) GOTO 260 FPBT01 256 WRITE(6,9) ALPHA FPBT01 GOTO 10 FPBT01 260 260 K(1)=K(1)+1 FPBT01 16(K(1)=K(1)+1 FPBT01 IF(PR.GE.ALPHA) GOTO 22 17(K(1).LE.KSUP) GOTO 256 FPBT01 WRITE(6,8) ALPHA FPBT01 GOTO 10 FPBT01 IF(PR.GE.ALPHA) GOTO 256 FPBT01 IF(PR.GE.ALPHA) GOTO 256 FPBT01 BOD FPBT01	ř		111/254 0	EP810161
IF(SINT) GOTO 254 FPBTOI WRITE(6,7) K(1),PROB,PRR FPBTOI GOTO 260 FPBTOI 254 IF(PRR.LT.ALPHA) GOTO 260 FPBTOI 255 WRITE(6,9) ALPHA GOTO 260 GOTO 10 FPBTOI 260 K(1)=K(1)+1 FPBTOI IF(PRR.GE.ALPHA) GOTO 22 FPBTOI IF(PRR.GE.ALPHA) GOTO 256 FPBTOI WRITE(6,8) ALPHA GOTO 10 BOTO 10 FPBTOI IF(PR.GE.ALPHA) GOTO 256 FPBTOI IF(PR.GE.ALPHA) GOTO 256 FPBTOI URITE(6,8) ALPHA FPBTOI GOTO 10 FPBTOI END FPBTOI	C	250	PRR=PROB+PRR	EPRT0162
WR 11E(6,7) K(1),PROB,PRR FPBTO1 GOTD 260 FPBTO1 254 IF(PRR.LT.ALPHA) GOTO 260 FPBTO1 256 WR 11E(6,9) ALPHA FPBTO1 GOTD 10 FPBTO1 260 K(1)=K(1)+1 FPBTO1 1F(K(1).LE.KSUP) GOTO 22 FPBTO1 1F(PRR.GE.ALPHA) GOTO 256 FPBTO1 WR 1TE(6,8) ALPHA FPBTO1 GOTO 10 FPBTO1 END FPBTO1		200	TE(SINT) COTO 254	EPBT0163
GOTD 260 FPBT01 254 IF(PRR.LT.ALPHA) GOTD 260 FPBT01 256 WRITE(6,9) ALPHA FPBT01 GOTD 10 FPBT01 260 K(1)=K(1)+1 FPBT01 IF(K(1)-LE.KSUP) GOTD 22 FPBT01 IF(PRR.GE.ALPHA) GOTD 256 FPBT01 WRITE(6,8) ALPHA FPBT01 GOTD 10 FPBT01 END FPBT01			WRITE(6.7) K(1) PROBARR	EPST0164
254 IF(PRR.LT.ALPHA) GOTO 260 FPBT01 256 WRITE(6,9) ALPHA FPBT01 GOTO 10 FPBT01 IF(PR.(1)+1) FPBT01 1F(K(1).LE.KSUP) GOTO 22 FPBT01 1F(PRR.GE.ALPHA) GOTO 256 FPBT01 WRITE(6,8) ALPHA FPBT01 GOTO 10 FPBT01 FPBT01 END FPBT01 FPBT01				EPRIO165
256 WRITE(6,9) ALPHA FPBT01 GOTO 10 FPBT01 260 K(1)=K(1)+1 FPBT01 IF(KK1)+LE-KSUP) GOTO 22 FPBT01 IF(PR.GE.ALPHA) GOTO 256 FPBT01 WRITE(6,8) ALPHA GOTO 256 GOTO 10 FPBT01 GOTO 10 FPBT01 END FPBT01		254		EPBT0166
GOTO 10 FPBT01 260 K(1)=K(1)+1 FPBT01 IF(K(1)-LE-KSUP) GOTO 22 FPBT01 IF(PRR.GE.ALPHA) GOTO 256 FPBT01 WRITE(6,8) ALPHA FPBT01 GOTO 10 FPBT01 END FPBT01		254	WPITE(6.0) AIDMA	EPBT0167
260 K(1)=K(1)+1 FPBT01 IF(K(1)-LE-KSUP) GOTO 22 FPBT01 IF(PRR.GE.ALPHA) GOTO 256 FPBT01 WRITE(6,8) ALPHA FPBT01 GOTO 10 FPBT01 END FPBT01		200	ΠΝΑΙΕΙΟΥΣΥ ΑΕΓΠΑ ΕΠΤΟ ΙΝ	EPRT0168
IF(K(1).LE.KSUP) GOTO 22 FPBTO1 IF(K(1).LE.KSUP) GOTO 256 FPBTO1 WRITE(6,8) ALPHA FPBTO1 GOTO 10 FPBTO1 END FPBTO1		260	K(1)=K(1)+1	EDATOIRO
IF(PR.GE.ALPHA)GOTO256FPBTO1WRITE(6,8)ALPHAFPBTO1GOTO10FPBTO1ENDFPBTO1		200	TE(K(1), LE, KSHD) COTO 22	EDBT0107
WRITE(6,8) ALPHAFPBT01GOTO 10FPBT01ENDFPBT01			$\frac{1}{1} \frac{1}{1} \frac{1}$	EDATO171
GOTO 10 FPBTO1 END FPBTO1			WRITELARN ALDHA	EDAT0172
END FPBT01			COTO 10	EPAT0172
			END	EPRT0174
				11010114

Flow Charts (Figs. 1-5)



Fig. 1







Fig. 4



RIASSUNTO

È stato condotto uno studio gemellare con il duplice scopo: 1. di studiare il comportamento ereditario dei dermatoglifi digitali a livello sia qualitativo che quantitativo, e 2. di elaborare un metodo per distinguere i gemelli MZ dai DZ mediante le impronte digitali.

Le impronte digitali di 50 coppie MZ (25 $\stackrel{\circ}{\xrightarrow{}}$ e 25 $\stackrel{\circ}{\xrightarrow{}}$) e 50 DZ (25 $\stackrel{\circ}{\xrightarrow{}}$ e 25 $\stackrel{\circ}{\xrightarrow{}}$) sono dunque state esaminate ed analizzate con una metodologia originale e un calcolatore IBM 7044/K32.

L'analisi qualitativa ha indicato una concordanza significativamente più elevata nelle coppie MZ che nelle DZ, con una certa variabilità fra i valori di concordanza di ogni singolo dito. L'analisi quantitativa ha indicato delle correlazioni significativamente più elevate nelle coppie MZ che nelle DZ, con intervalli di confidenza molto limitati nel primo caso. I conteggi singoli presentano un comportamento analogo a quello dei conteggi cumulativi compiuti sulle 5 o 10 dita, pur con una variabilità casuale ovviamente più elevata.

I dermatoglifi digitali risultano dunque presentare un condizionamento genetico praticamente completo che più che a un livello cumulativo per le 10 dita, come generalmente si ritiene, sembra agire a livello dei caratteri quali-quantitativi delle singole dita. Il numero totale delle creste, più che un carattere, sembra essere un valore cumulativo utile ma artificiale; applicato alla diagnosi di zigotismo, esso fornisce da solo una probabilità generale di una giusta diagnosi relativamente elevata (0.86).

RÉSUMÉ

Une étude gémellaire a été conduite avec le but 1. d'étudier l'hérédité des dermatoglyphes digitaux au point de vue qualitatif et quantitatif, et 2. de développer une méthode pour séparer les jumeaux MZ et DZ moyennant les empreintes digitales.

Les empreintes digitales de 50 couples MZ (25 \bigcirc et 25 \bigcirc) et 50 DZ (25 \bigcirc et 25 \bigcirc) ont été examinées et analysées par une méthodologie originale et un computer IBM 7044/K32.

L'analyse qualitative a indiqué des valeurs de concordance significativement plus élevées chez les MZ vis-à-vis des DZ, avec une certaine variabilité parmi les différentes valeurs pour chaque doigt. L'analyse quantitative a indiqué des valeurs de corrélation significativement plus élevées chez les MZ vis-à-vis des DZ, avec des intervalles de confiance très limités chez les premiers. Le numéro des crêtes sur chaque doigt a un comportement similaire aux numéros complexifs pour 5 ou 10 doigts, tout en présentant une variabilité casuelle évidemment plus élevée.

Les dermatoglyphes digitaux présentent donc un conditionnement génétique pratiquement complet qui, plutôt qu'à un niveau cumulatif pour les 10 doigts (ainsi que l'on croit généralement), paraît agir sur les caractères qualiquantitatifs de chaque doigt. Le numéro total des crêtes, au lieu qu'un caractère, paraît être une valeur complexive utile, mais artificielle, qui, appliquée au diagnostic de zygotisme, donne une probabilité générale relativement élevée (0.86) d'un diagnostic correct.

ZUSAMMENFASSUNG

Verf. führten eine Zwillingsuntersuchung durch, die folgende Ziele verfolgte: 1. die Vererbung der Fingerleisten sei es qualitativ als quantitativ gesehen zu untersuchen und 2. eine Methode auszuarbeiten, die es gestattet, auf Grund der Fingerleisten EZ von ZZ zu unterscheiden.

Es wurden daher mit Hilfe einer 7044/K32 IBM-Büromaschine und nach einer besonderen Methode die Fingerleisten von 50 EZ und 50 ZZ-Paaren (jeweils 25 $\stackrel{\circ}{\supset}$ und 25 $\stackrel{\circ}{\bigcirc}$) untersucht und analysiert.

Die qualitative Analyse zeigte eine wesentlich höhere Konkordanz der EZ gegenüber den ZZ mit einigen Schwankungen in den Konkordanzwerten der einzelnen Finger. Die quantitative Analyse wies auf bedeutend höhere Korrelationen bei den EZ- als bei den ZZ-Paaren hin mit sehr beschränkten « Confidence-Intervals » bei den ersteren. Die Auszählungen an den einzelnen Fingern ergaben ähnliche Werte wie diejenigen, die sich über 5 oder 10 Finger erstreckten, wenn auch die Zufallsschwankungen dabei natürlich höher sind.

Die Fingerhautleisten scheinen somit praktisch voll und ganz erbbendingt zu sein. Während allgemein angenommen wird, dass sich die Erblichkeit kumulativ auf die 10 Finger auswirkt, so scheint sie hingegen eher an den qualitativ-quantitativen Merkmalen der einzelnen Finger zum Ausdruck zu kommen. Die Gesamtleistenzahl (total finger ridge count) würde demnach weniger ein Merkmal als einen nützlichen jedoch künstlichen Kumulativwert darstellen: wenn man ihn auf die Eiigkeitsdiagnose anwendet, so liefert er in der Tat allein schon eine relativ hohe allgemeine Wahrscheinlichkeit für eine richtige Diagnose (0.86).