

ARTICLE

Expectation formation and the Phillips curve revisited

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Abstract

This paper studies expectation formation of professional forecasters in the context of the Phillips curve. We assess whether professionals form their expectations regarding inflation and unemployment consistent with the Phillips curve based on individual forecast data taken from the ECB Survey of Professional Forecasters. We consider expectations over different horizons and do not restrict the analysis to point forecasts but we also take the information inherent in density forecasts into account. We explicitly consider the role of anchoring of inflation expectations as potential source of nonlinearity, and we also assess whether the Phillips curve relation translates to a link between uncertainty regarding inflation and unemployment. Our findings show that professionals tend to build their expectations in line with the Phillips curve but this is only observed for expectations made for shorter horizons. For longer horizons, the Phillips curve connection is much weaker. This relationship also depends on the degree of anchoring and results in a connection between uncertainty regarding future inflation and unemployment.

Keywords: Anchoring; inflation expectations; Phillips curve; uncertainty

1. Introduction

Phillips (1958) first found an inverse relationship between inflation and unemployment,¹ which has been verified by Samuelson and Solow (1960) shortly thereafter. Today, it is well-known that this relationship between inflation and unemployment crucially depends on the degree of anchoring of inflation expectations (Blanchard, 2016; Ball and Mazumder, 2019). If inflation expectations are strongly anchored in the sense that they correspond to the inflation target of the central bank,² there is a (temporary) relationship between inflation and unemployment. However, if inflation expectations are not anchored, the relationship solely exists between unemployment and the change in inflation (Blanchard, 2016).³ This underlines the importance of expectation building by market participants in this context. Therefore, the present study aims to shed further light on the way how expectations are made by professional forecasters and especially, whether they are in line with the concept of the Phillips curve. In doing so, we exploit the variation of expectations regarding inflation and unemployment across forecasters, over time and across different horizons given in the ECB Survey of Professional Forecasters, and we estimate an expectation-based version of the Phillips curve.

An increase in the degree of anchoring of inflation expectations is sometimes argued to result in a flattening of the slope of the Phillips curve (Jørgensen and Lansing, 2019; Bundick and Smith, 2024; Barnichon and Mesters, 2021). Therefore, we explicitly account for the possibility of a non-linear relationship between expectations regarding inflation and unemployment by considering the degree of anchoring of inflation expectations. For this purpose we apply a measure proxying the degree of anchoring by exploiting the information in both point and density forecasts for inflation taken from the ECB Survey of Professional Forecasters. In this context, we follow Czudaj

(2023a) extending the approach proposed by Bems et al. (2021), which is based on three different features characterizing the degree of anchoring on an aggregate level, by considering six different features and by computing this measure on an individual level for each forecaster. When estimating our expectation-based version of the Phillips curve, we explicitly account for nonlinearity stemming from the degree of anchoring.

Furthermore, adding to the literature concerning spillovers between different dimensions of uncertainty (Klößner and Sekkel, 2014; Ter Ellen et al. 2019; Glas, 2020; Caggiano et al. 2020; Thiem, 2020; Beckmann et al. 2023), we check whether an expectation-based relationship between inflation and unemployment also translates into an association between the uncertainties regarding inflation and unemployment. In doing so, we proxy these uncertainties by individual forecasters' standard deviations derived from their distributional forecasts for inflation and unemployment. In addition, we also study the heterogeneity across forecasters and over time when considering both types of Phillips curve relationships.

Therefore, the contribution of the present study compared to the existing literature is threefold. First, we do not solely focus on point forecasts when assessing the consistency of professional forecasts with the concept of the Phillips curve, but we also take forecasts for the whole distribution in account. Second, we explicitly address the role of anchoring of inflation expectations for the estimation of an expectation-based Phillips curve relationship. Third, we assess a Phillips curve-based link between uncertainty regarding inflation and unemployment. Our findings suggest that professional forecasters act in line with the Phillips curve for lower forecast horizons but not for medium-run forecasts. The inclusion of the anchoring measure indicates some nonlinearity in the relationship. In addition, we also find the existence of a co-movement of the uncertainties regarding future inflation and unemployment according to the Phillips curve.

The remainder of the paper is organized as follows: The next section reviews the most relevant literature. Section 3 provides an in-depth description of our dataset, including the construction of different measures we are considering and of our empirical methodology. Section 4 presents and discusses our empirical findings, while Section 5 concludes.

2. Review of the literature

In a general sense, the present paper extends the literature, which examines the expectation building mechanism using survey forecast data while focusing on the behavior of economic agents, and/or the macroeconomic models they rely upon (Coibion and Gorodnichenko, 2012, 2015a; Bordalo et al. 2020; Czudaj, 2022, 2023b; Glas and Heinisch, 2023). More specifically, the utilization of survey-based expectations data for the estimation of an expectation-based Phillips curve to study whether (professional) forecasters follow the concept of the Phillips curve when making their forecasts has already been considered in the previous literature. In this section, we briefly review the most closely related studies to make clear how the present study deviates from them.

In this vein, Dräger et al. (2016) first compute the share of consumers in the University of Michigan survey of consumers, who form their expectations consistent with the Phillips curve in the sense that they expect increases in inflation corresponding with decreases in unemployment and vice versa. Then, they assess whether this share of consumers is affected by central bank communication or by the corresponding media reporting.

Fendel et al. (2011) use monthly data from the survey of professional forecasters conducted by Consensus Economics for the G7 economies to assess whether professionals form their expectations in line with the Phillips curve for the sample period from October 1989 to December 2007. Their study relies on fixed-event forecasts for the current and the next year and finds a negative relationship between unemployment and inflation for the short-run and/or the medium-run for all G7 economies except of Germany.⁴ In addition, they also test for nonlinearity by the inclusion of the level of inflation uncertainty, a squared term for unemployment expectations, or a recession dummy. In this case, inflation uncertainty is proxied by the cross-sectional variance across

forecasters, and therefore, actually is a measure of disagreement among forecasters, which does not necessarily correspond to the uncertainty of forecasters.⁵ Rülke (2012) extends this study to six Asian-Pacific countries.

Same as the present study, Frenkel et al. (2011) also use data from the ECB Survey of Professional Forecasters for the sample period between 1999Q1 and 2010Q4 to reassess whether the expectation formation of professionals is in line with the Phillips curve after the global financial crisis by extending the regression model by a dummy variable for the crisis. They basically conclude that the global financial crisis has not changed the way how professional forecasters form their expectations. Casey (2020) extends this analysis by considering the surveys of professional forecasters of the ECB, the US Fed, and the Bank of England for a sample period until 2017 and by also focusing on estimates on an individual forecaster level. Clements (2024) also checks whether professional forecasters form the expectations in line with the Phillips curve by using U.S. Survey of Professional Forecasters data and estimating a hybrid Phillips curve for each individual forecaster while testing whether forecasters who started later to participate in the survey differ systematically from earlier participants.

To the best of our knowledge, none of the existing studies belonging to this strand of the literature has also considered the information inherent in density forecasts but solely rely on point forecasts. None of them has explicitly considered the role of anchoring as potential source of non-linearity and none of them has assessed a Phillips curve based link between uncertainty regarding inflation and unemployment. The present study fills all these gaps. In addition, our sample period includes two recent interesting episodes: first, the period around 2014 and 2022 characterized by policy rates hitting the effective zero lower bound associated with low inflation rates (i.e., below the inflation target) and second, the period thereafter, in which inflation increased to historical levels and monetary policy has been tightened.

In addition, by relying on an individual measure of anchoring of inflation expectations, the present study also connects to the large literature studying whether inflation expectations are (de-)anchored using survey data, financial market data, or both (Gurkaynak et al. 2010; Jochmann et al. 2010; Beechey et al. 2011; Galati et al. 2011; Strohsal and Winkelmann, 2015; Scharnagl and Stapf, 2015; Łyziak and Paloviita, 2017; Natoli and Sigalotti, 2018; Hachula and Nautz, 2018; Buono and Formai, 2018). Most recently, survey data have been used to construct anchoring measures (Grishchenko et al. 2019; Bems et al. 2021; Beckmann and Czudaj, 2023; Czudaj, 2023a). In the present paper, we especially follow Czudaj (2023a), who extends the approach proposed by Bems et al. (2021). The latter use survey data provided by Consensus Economics to construct an anchoring measure on an aggregated level for several economies based on three different metrics. Czudaj (2023a) considers six instead of three metrics characterizing the degree of anchoring and computes the measure on an individual forecaster level instead of using an aggregate for the economy as a whole. In addition, Czudaj (2023a) studies the association of the level of anchoring with expectations regarding the stance of monetary policy and different cost-push factors.

3. Data and empirical methodology

3.1 Data

3.1.1 Forecast survey data

The data have been collected from the ECB Survey of Professional Forecasters (SPF) for the quarterly sample period from 1999Q1 to 2023Q1. More precisely, we rely on individual fixed-horizon point forecasts and density forecasts for the inflation rate and the unemployment rate for the Euro Area. These forecasts have been made at the beginning of each quarter by various forecasters representing professional institutions (i.e., major banks and research institutes across the whole Euro Area). The fixed-horizon forecasts are provided for horizons of one-year-ahead, two-years-ahead, and five-years-ahead ($h = 1, 2, 5$) and therefore allow a comparison between short-run

expectations ($h = 1, 2$) and medium-run expectations ($h = 5$). Most of these professionals are probably familiar with the general concept of the Phillips curve and/or its economic foundation. Therefore, it appears to be interesting to study whether these professionals actually form their expectations regarding inflation and unemployment in line with the Phillips curve. The number of participating forecasters varies over the different waves of the survey between 30 and 61 within the considered sample period with a mean of about 42 forecasters and a total of 106 different institutions (see Figure A1).

The black points in Figures 1 and 2 illustrate individual quarterly point forecasts for the inflation rate and the unemployment rate in the Euro Area (both in percent per annum) for the three horizons ($h = 1, 2, 5$). The red lines provide the corresponding cross-sectional mean forecasts across forecasters for each point in time, and the blue lines illustrate realized inflation and unemployment rates (taken from ECB Statistical Data Warehouse) referring to the periods, at which the forecasts have been made. First of all, the graphs show that there is some degree of heterogeneity across the forecasters, which tends to increase in “crises periods” usually characterized by severe uncertainty. For inflation, the largest dispersion across forecasters is observed in the current high inflation period. For unemployment, the strongest disagreement among forecasters becomes evident in the first year of the COVID-19 pandemic between 2020 and 2021, where many forecasters have expected a much larger unemployment rate in the Euro Area than has actually been materialized. Second, we also see a clear difference between short-run horizon ($h = 1, 2$) and medium-run horizon ($h = 5$) forecasts. We basically see for both macro variables that short-run forecasts are usually closely related to current realizations but medium-run forecasts are not. Five-years-ahead inflation forecasts are very constant over the sample period lying on average pretty close to the inflation target of the ECB of 2%. This illustrates that inflation expectations were strongly anchored over the sample period, although we also see a mild drift in the most recent high inflation period. Except for this recent period, unemployment expectations for $h = 5$ were on average much lower than realized unemployment. When assuming that professionals build their medium-run unemployment expectations based on their view about the “natural rate of unemployment,” this would imply that they have considered a negative output gap over the entire sample period resulting in a too low inflation rate according to the Phillips curve relationship.

While several existing studies on the expectation formation mechanism rely on the point forecasts taken from this data set (see e.g., Andrade and Le Bihan, 2013; Dovern, 2015; Czudaj, 2022, 2023b), the information inherent in the density forecasts have rarely been exploited (see e.g. Abel et al. 2016). Therefore, in the next subsection, we also consider density forecasts for our analysis.

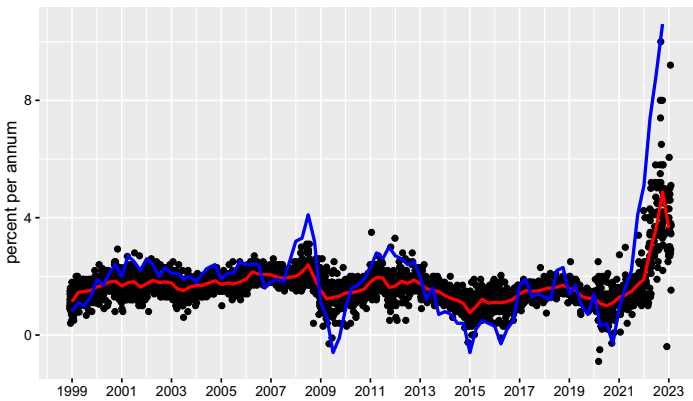
3.1.2 Distributional forecasts

The participants are also asked to assign subjective probabilities ($p_{i,k,t,h}$) to predefined intervals, into which the inflation rate and the unemployment rate might fall. These probability distributions provide individual forecasts for the entire distribution, which also include information about the uncertainty surrounding the point forecasts as well as the skewness and kurtosis. Nowadays, tail probabilities are also considered being relevant to assess the likelihood of “inflation disasters” (Hilscher et al. 2022).

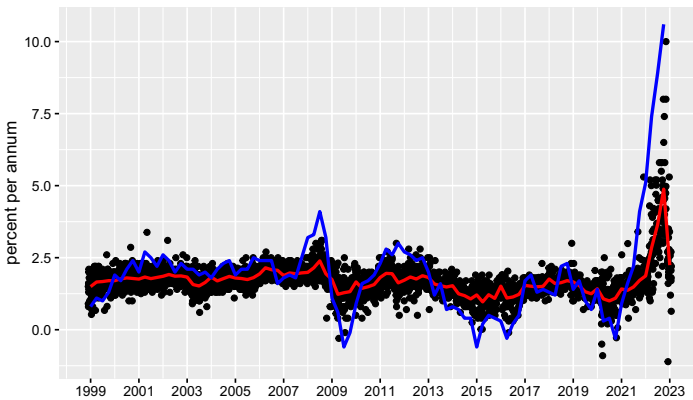
Therefore, to foster our understanding on the expectation formation mechanism, we extract individual information from distributional forecasts by following Abel et al. (2016) and Glas and Hartmann (2022). In doing so, we rely on the “mass-at-midpoint” approach and compute the following measures:

$$\mu_{i,t,h} = 1/100 \sum_{k=1}^K p_{i,k,t,h} m_k, \quad (1)$$

Panel (a): $h = 1$



Panel (b): $h = 2$



Panel (c): $h = 5$

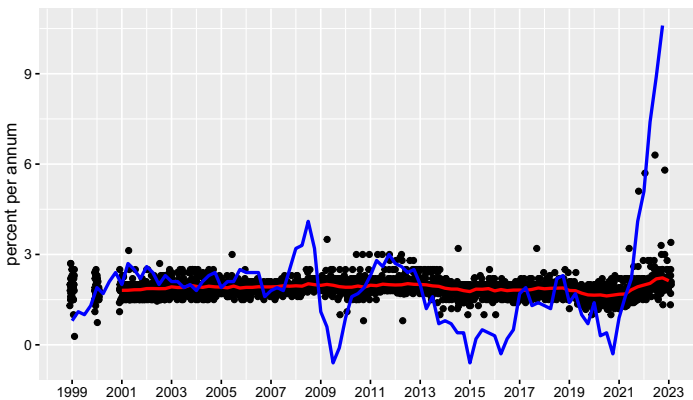


Figure 1. Inflation point forecasts. The black points represent individual quarterly point forecasts for the inflation rate in the Euro Area (in percent per annum) for different horizons h (one-year-ahead, two-years-ahead, and five-years-ahead) for the period from 1999Q1 to 2023Q1 taken from the ECB Survey of Professional Forecasters. The red lines provide the corresponding cross-sectional mean forecasts across forecasters for each point in time and the blue lines illustrate realized inflation rates (taken from ECB Statistical Data Warehouse) referring to the periods, at which the forecasts have been made.

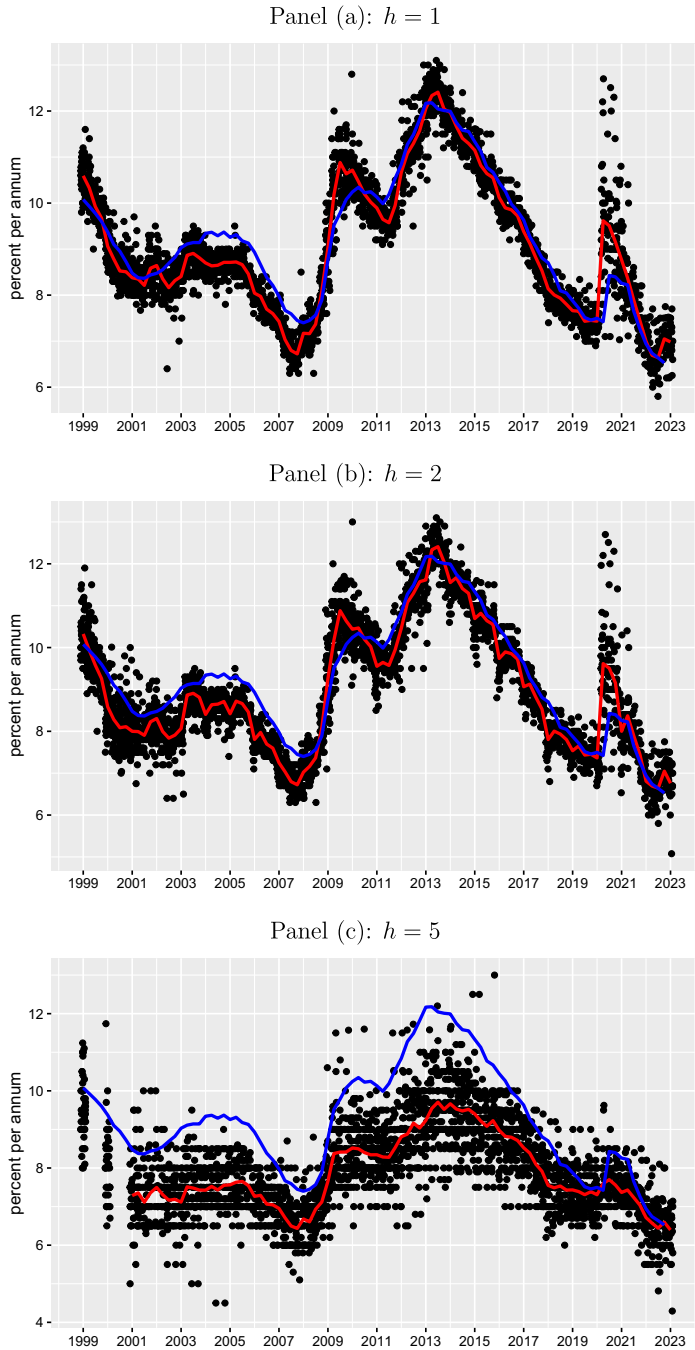


Figure 2. Unemployment point forecasts. The black points represent individual quarterly point forecasts for the unemployment rate in the Euro Area (in percent per annum) for different horizons h (one-year-ahead, two-years-ahead, and five-years-ahead) for the period from 1999Q1 to 2023Q1 taken from the ECB Survey of Professional Forecasters. The red lines provide the corresponding cross-sectional mean forecasts across forecasters for each point in time, and the blue lines illustrate realized inflation rates (taken from ECB Statistical Data Warehouse) referring to the periods, at which the forecasts have been made.

$$\sigma_{i,t,h}^2 = 1/100 \sum_{k=1}^K p_{i,k,t,h} (m_k - \mu_{i,t,h})^2, \quad \sigma_{i,t,h} = \sqrt{\sigma_{i,t,h}^2}, \tag{2}$$

$$\text{skew}_{i,t,h} = 1/100 \sum_{k=1}^K p_{i,k,t,h} [(m_k - \mu_{i,t,h})/\sigma_{i,t,h}]^3, \tag{3}$$

$$\kappa_{i,t,h} = 1/100 \sum_{k=1}^K p_{i,k,t,h} [(m_k - \mu_{i,t,h})/\sigma_{i,t,h}]^4, \tag{4}$$

where $\mu_{i,t,h}$, $\sigma_{i,t,h}^2$, $\sigma_{i,t,h}$, $\text{skew}_{i,t,h}$, and $\kappa_{i,t,h}$ denote individual forecasters’ mean, variance, standard deviation, skewness, and kurtosis, respectively. Moreover, m_k represents the middle of each interval. and K is the number of intervals. $p_{i,k,t,h}$ stand for the individual probabilities assigned by forecasters, and i , t , h , and k are indexes for individual forecaster, period (i.e., quarter of a year), forecast horizon, and interval, respectively. In this context, it is also worth noting that the interior intervals in the ECB SPF have gaps of 0.1 percentage points between each other. These have been closed by extending the lower and upper bound of each interval by 0.05 following a convention in the existing literature (Abel et al. 2016; Glas and Hartmann, 2022). To compute the midpoints m_k , the intervals in both tails of the distribution have been assumed to have a width that is double as wide as the width of the interior intervals.

The means of the individual density forecasts $\mu_{i,t,h}$ are usually very close to the point forecasts provided by the forecasters for most of the forecasters, which shows that the distributional forecasts are largely consistent with the point forecasts. In the following, we especially rely on the individual standard deviations $\sigma_{i,t,h}$ as a proxy for forecasters’ ex ante uncertainty regarding their inflation and unemployment forecasts. The individual standard deviations $\sigma_{i,t,h}$ for inflation and unemployment forecasts are plotted over time in Figures A2 and A3 in the Appendix. Figure 3 shows the cross-sectional means across forecasters at each point in time for the three forecast horizons ($h = 1, 2, 5$). First of all, it becomes clear that uncertainty generally increases with the horizon h . Second, it also becomes evident that forecast uncertainty has substantially increased during the global financial crisis between 2008 and 2009 and has not returned to pre-crisis levels since then. Third, another severe rise in forecast uncertainty is observed in 2020—the first year of the COVID-19 pandemic. Unemployment forecast uncertainty has dropped since then while inflation forecast uncertainty has accelerated even further.

3.1.3 Anchoring measure

We also use the information derived from distributional forecasts, to construct an individual forecasters’ proxy for the degree of anchoring of inflation expectations following Czudaj (2023a) and referring to Bems et al. (2021), who construct an anchoring measure on an aggregated level for several economies based on survey data provided by Consensus Economics.

Similar to Bems et al. (2021), our anchoring measure is based on six subindexes, which are computed for each individual forecaster (Czudaj, 2023a):⁶ First, we compute the absolute deviation of individual inflation expectations from the ECB’s inflation target of 2%:

$$\text{Metric}_{1,i,t,h} = \sqrt{(\widehat{\pi}_{i,t,h} - 2\%)^2}, \tag{5}$$

where $\widehat{\pi}_{i,t,h}$ denotes inflation expectations of forecaster i made in period t for horizon h with $h = 1, 2, 5$ years. This metric is rooted in the idea that well-anchored inflation expectations should be very close to the inflation target. Hence, any deviation from the ECB’s target indicates a lower degree of anchoring.

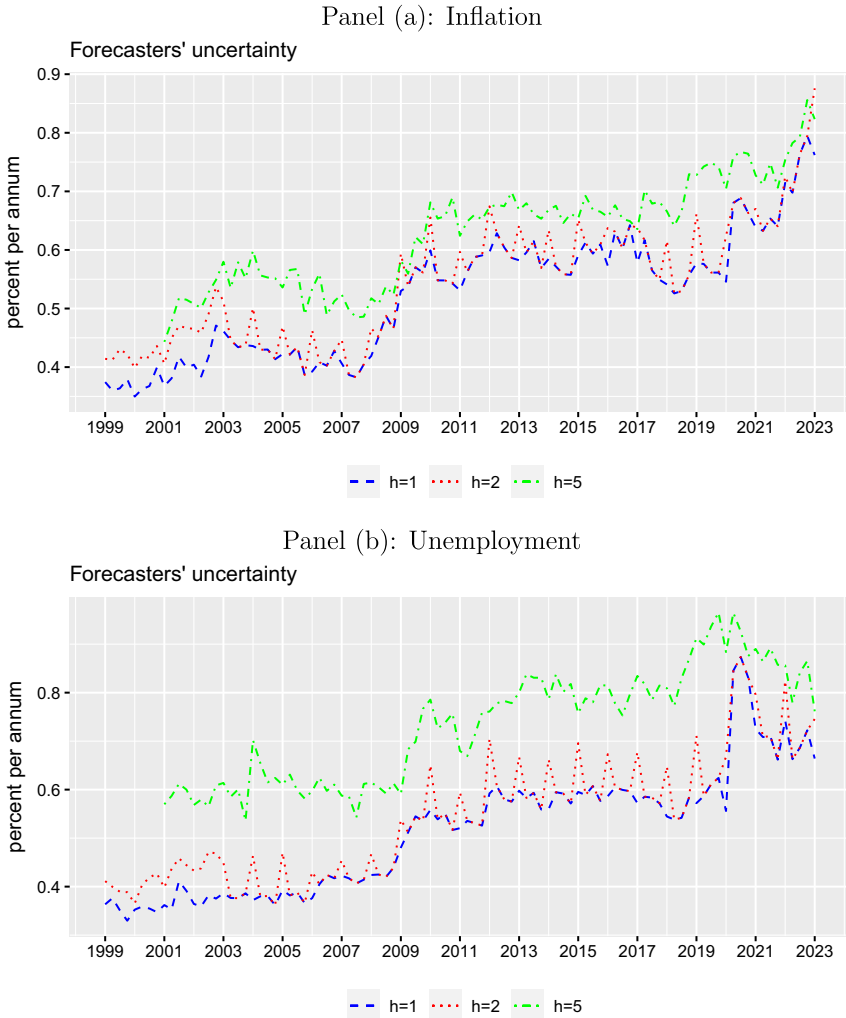


Figure 3. Forecasters' uncertainty of density forecasts. The plots illustrate means of standard deviations across forecasters derived from individual quarterly density forecasts for the inflation rate and the unemployment rate in the Euro Area (in percent per annum) for different horizons h (one-year-ahead, two-years-ahead, and five-years-ahead) for the period from 1999Q1 to 2023Q1 taken from the ECB Survey of Professional Forecasters.

Second, we also take the absolute variation of inflation expectations from the forecaster-specific time-series mean:

$$\text{Metric}_{2,i,t,h} = \sqrt{(\widehat{\pi}_{i,t,h} - \bar{\pi}_{i,h})^2}, \tag{6}$$

where $\bar{\pi}_{i,h}$ is the time-series mean of inflation expectations for each forecaster i . The idea behind $\text{Metric}_{2,i,t,h}$ is that well- anchored inflation expectations rarely need to be revised by professionals.

Third, we also calculate the dispersion of inflation expectations, i.e., the absolute difference of individual inflation expectations to the cross-sectional mean across forecasters:

$$\text{Metric}_{3,i,t,h} = \sqrt{(\widehat{\pi}_{i,t,h} - \bar{\pi}_{t,h})^2}, \tag{7}$$

where $\bar{\pi}_{t,h}$ represents the cross-sectional mean forecast across forecasters at each point in time. The rationale behind this metric is that professional forecasters should not strongly disagree regarding future inflation, if inflation expectations are well anchored. Therefore, a stronger disagreement indicates a lower degree of anchoring.

As further three metrics, following the idea of Czudaj (2023a), we take the uncertainty, skewness, and kurtosis derived from density forecasts as outlined in Section 3.1.2:

$$\text{Metric}_{4,i,t,h} = \sigma_{i,t,h}, \quad \text{Metric}_{5,i,t,h} = \text{skew}_{i,t,h}, \quad \text{Metric}_{6,i,t,h} = \kappa_{i,t,h}. \tag{8}$$

Finally, we aggregate the six anchoring metrics outlined above into one measure since they exhibit complementary features describing the degree of anchoring. First, the individual metrics are standardized across forecasters and over time to have a mean of zero and a variance of unity:

$$\text{Standard Metric}_{n,i,t,h} = -\frac{(\text{Metric}_{n,i,t,h} - \overline{\text{Metric}}_{n,h})}{\sigma(\text{Metric})_{n,h}}, \quad n = 1, \dots, 6, \tag{9}$$

where $\overline{\text{Metric}}_{n,h}$ and $\sigma(\text{Metric})_{n,h}$ stand for the sample average and the sample standard deviation of the corresponding metric across forecasters i and time periods t . In addition, we change the sign of each metric in equation (9) as in this case an increase (a decrease) of the corresponding measure indicates a higher (lower) degree of anchoring. This results in a straightforward interpretation of our anchoring measure. Second, we compute the simple mean across the six standardized metrics to get our final anchoring measure:

$$\text{Anchor}_{i,t,h} = \frac{1}{6} \sum_{n=1}^6 \text{Standard Metric}_{n,i,t,h}, \quad h = 1, 2, 5. \tag{10}$$

The resulting anchoring measure is illustrated in Figure 4 for each horizon ($h = 1, 2, 5$), and each individual forecaster represented by the black dots and on an aggregated level visualized by the red line showing the cross-sectional mean. On average, it seems that inflation expectations have been widely anchored within the Euro Area for nearly the entire sample period. However, as discussed by Czudaj (2023a), we also see periods, in which some forecasters have believed in a de-anchoring of inflation expectations. For the short-run horizons ($h = 1, 2$), we also see mild evidence for a de-anchoring of inflation expectations for the period around the global financial crisis (2008–2009) and the beginning of the period of ultralow policy rates (2014–2016) on an aggregated level, where the cross-sectional means turn into negative. However, in the most recent high inflation period, we observe a clear de-anchoring, especially when focusing on the short-run horizon ($h = 1, 2$). This evidence of a de-anchoring in some periods is roughly in line with previous studies for the Euro Area (Strohsal and Winkelmann, 2015; Łyziak and Paloviita, 2017; Natoli and Sigalotti, 2018; Buono and Formai, 2018; Grishchenko et al. 2019).⁷ Again, when referring to the medium-run horizon ($h = 5$), we do not see much indication of de-anchoring over most of the sample period on an aggregated level, although we also see a mild de-anchoring in the most recent period.

3.2 Empirical methodology

We have constructed a large panel data set, which is used to estimate an expectation-based Phillips curve relationship to check whether professional forecasters build their forecasts in line with the concept of the Phillips curve. In doing so, we consider different versions of the following general regression model:

$$E_{i,t}(\pi_{t+h}) = \beta_1 E_{i,t}(u_{t+h}) + \beta_2 E_{i,t-1}(\pi_{t+h}) + \beta_3 \text{Anchor}_{i,t,h} + \beta_4 \text{Anchor}_{i,t,h} \times E_{i,t}(u_{t+h}) + \beta_5 \text{Anchor}_{i,t,h} \times E_{i,t-1}(\pi_{t+h}) + \mu_i + \gamma_t + \varepsilon_{i,t} \tag{11}$$

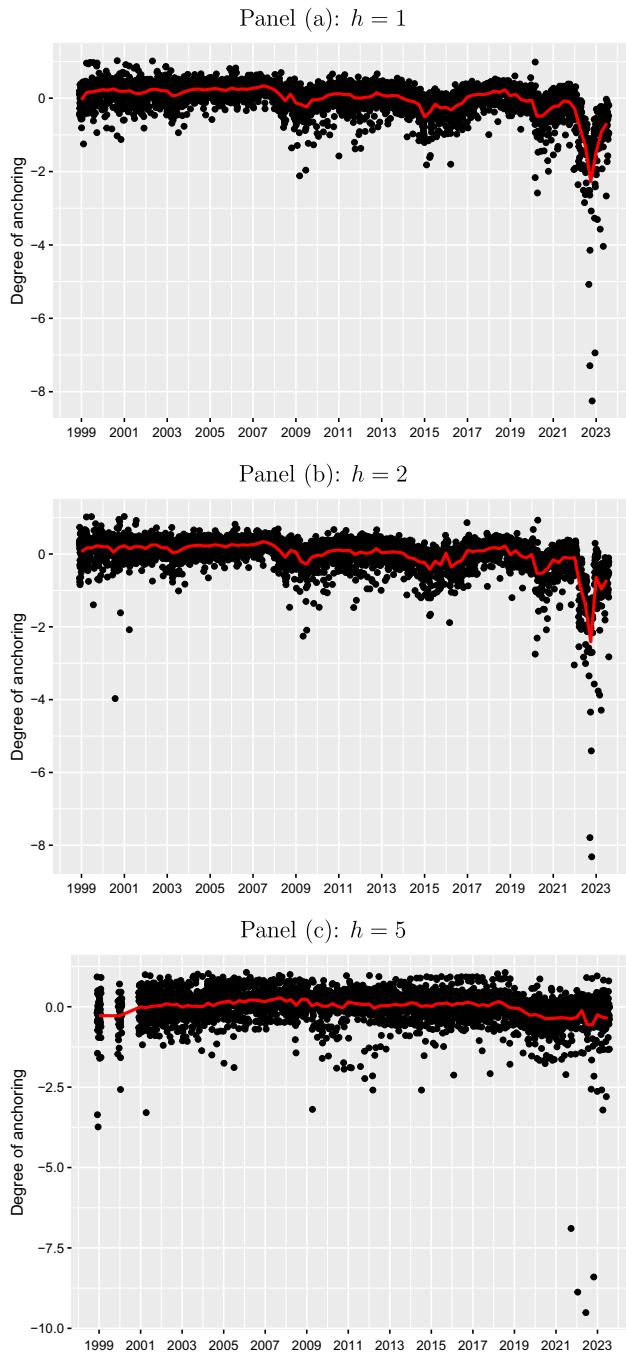


Figure 4. Anchoring measures. The black points represent individual quarterly anchoring measures derived from information inherent in inflation point and density forecasts for different horizons h (one-year-ahead, two-years-ahead, and five-years-ahead) for the period from 1999Q1 to 2023Q1 taken from the ECB Survey of Professional Forecasters. The red lines provide the corresponding cross-sectional means across forecasters for each point in time.

where $E_{i,t}(\pi_{t+h})$ represents inflation expectations made in period t by forecaster i for a horizon of h -years-ahead, $E_{i,t}(u_{t+h})$ denotes the corresponding unemployment expectations, $E_{i,t-1}(\pi_{t+h})$ gives inflation expectations made in the previous quarter, and $\text{Anchor}_{i,t,h}$ is a proxy measuring the individual degree of anchoring of inflation expectations derived in Section 3.1.3. The inclusion of lagged inflation expectations is necessary for three reasons: first, it allows for the presence of serial correlation due to an overlapping sample in the measurement of inflation.⁸ Second, it also controls for the possibility of a lower degree of anchoring for individual forecasters, in which case they might build their expectations based on the recent past.⁹ Third, it also accounts for a delay in updating the information set by forecasters, which has been found in the previous literature (Coibion and Gorodnichenko, 2015a). μ_i , γ_t , and $\varepsilon_{i,t}$ characterize time-invariant forecaster-specific fixed effects, time-fixed effects, and idiosyncratic errors, respectively. μ_i captures a potential heterogeneity across forecasters in forecasting inflation, and γ_t allows for any information that is available to each forecaster. The latter controls for all realized macroeconomic variables, which are observed by all forecasters.¹⁰

The anchoring measure is included into the model as the Phillips curve relationship is known to depend on the anchoring of inflation expectations: If inflation expectations are anchored, there is a relationship between inflation and unemployment. However, if inflation expectations are de-anchored, then the relationship exists between the unemployment rate and the change in inflation. The latter version of the Phillips curve is known as the accelerationist Phillips curve (Blanchard, 2016; Hazell et al. 2022). Therefore, we examine whether there is a nonlinear relationship between inflation expectations and unemployment expectations depending on the degree of anchoring. In doing so, we have included the anchoring measure and two interaction terms between the anchoring measure and the other two variables into equation (11).

To check for robustness the general regression model provided in equation (11) has been used in different variants by restricting it to a pooled regression model with and without lagged inflation expectations as well as to a fixed-effects model with and without time-fixed effects. In addition, we have also estimated the model applying the Arellano and Bond (1991) GMM estimator to account for the so-called Nickell (1981) bias and an iterative Cochrane and Orcutt (1949) estimator to additionally control for serial correlation.

The same model has also been estimated for aggregated time-series data using cross-sectional means across forecasters:

$$\begin{aligned} \bar{E}_t(\pi_{t+h}) = & \beta_0 + \beta_1 \bar{E}_t(u_{t+h}) + \beta_2 \bar{E}_{t-1}(\pi_{t+h}) + \beta_3 \overline{\text{Anchor}}_{t,h} \\ & + \beta_4 \overline{\text{Anchor}}_{t,h} \times \bar{E}_t(u_{t+h}) + \beta_5 \overline{\text{Anchor}}_{t,h} \times \bar{E}_{t-1}(\pi_{t+h}) + \varepsilon_t, \end{aligned} \tag{12}$$

where $\bar{E}_t(\pi_{t+h})$, $\bar{E}_t(u_{t+h})$, and $\overline{\text{Anchor}}_{t,h}$ are the corresponding cross-sectional means across forecasters for each variable.

The existence of a negative expectation-based Phillips curve relationship between inflation and unemployment as given in parsimonious form by

$$E_{i,t}(\pi_{t+h}) = \beta_0 + \beta_1 E_{i,t}(u_{t+h}) + \varepsilon_{i,t} \quad \text{with } \beta_1 < 0 \tag{13}$$

would result in a positive relationship between the variances of inflation and unemployment:

$$\sigma_{i,t}^2(\pi_{t+h}) = \beta_1^2 \sigma_{i,t}^2(u_{t+h}) + \sigma_{i,t}^2(\varepsilon_{i,t}) \quad \text{if } \text{Cov}(E_{i,t}(u_{t+h}), \varepsilon_{i,t}) = 0. \tag{14}$$

Therefore, we also study the relationship between the standard deviations of the variables derived from individual distributional forecasts as proxies for ex ante uncertainty (see Section 3.1.2) while again relying on different versions of the following general regression model:

$$\begin{aligned} \sigma_{i,t}(\pi_{t+h}) = & \beta_1 \sigma_{i,t}(u_{t+h}) + \beta_2 \sigma_{i,t-1}(\pi_{t+h}) + \beta_3 \text{Anchor}_{i,t,h} + \beta_4 \text{Anchor}_{i,t,h} \times \sigma_{i,t}(u_{t+h}) \\ & + \beta_5 \text{Anchor}_{i,t,h} \times \sigma_{i,t-1}(\pi_{t+h}) + \mu_i + \gamma_t + \varepsilon_{i,t} \end{aligned} \tag{15}$$

where $\sigma_{i,t}(\pi_{t+h})$ represents inflation uncertainty proxied by the standard deviation of density forecasts made in period t by forecaster i for a horizon of h -years-ahead, $\sigma_{i,t}(u_{t+h})$ denotes the correspondingly computed unemployment uncertainty, $\sigma_{i,t-1}(\pi_{t+h})$ gives inflation uncertainty based on the previous quarters density forecasts, and all other variables are defined as in equation (11). Analogously, we have also considered the same model for aggregated time-series data again using cross-sectional means across forecasters:

$$\begin{aligned} \bar{\sigma}_t(\pi_{t+h}) = & \beta_0 + \beta_1 \bar{\sigma}_t(u_{t+h}) + \beta_2 \bar{\sigma}_{t-1}(\pi_{t+h}) + \beta_3 \overline{\text{Anchor}}_{t,h} \\ & + \beta_4 \overline{\text{Anchor}}_{t,h} \times \bar{\sigma}_t(u_{t+h}) + \beta_5 \overline{\text{Anchor}}_{t,h} \times \bar{\sigma}_{t-1}(\pi_{t+h}) + \varepsilon_t. \end{aligned} \quad (16)$$

The presumed negative relationship between expectations of professional forecasters regarding inflation and unemployment is shown in Figure 5 for each forecast horizon, where each point color refers to a different forecaster. Overall, we see that higher levels of inflation expectations tend to correspond to lower unemployment expectations and vice versa. However, the plots also visualize that unemployment expectations have varied stronger compared to inflation expectations over most parts of the sample period, for which inflation expectations have been relatively stable. This observation motivates us to also study the heterogeneity in the Phillips curve relationship across forecasters and over time, which is done at a later stage of the analysis (see Section 4.3). In addition, we see that the relationship tends to lessen with the forecast horizon h . See also Figure A4 in the Appendix for the corresponding relationship on an aggregated level.

In line with our presumption (see equations (13) and (14)), the negative relationship between expectations regarding inflation and unemployment results in a positive relationship between the corresponding standard deviations as illustrated in Figure 6. Figure A5 in the Appendix visualizes the corresponding relationship on an aggregated level.

4. Empirical findings

The empirical findings for the estimated regression models mentioned in Section 3.2 are discussed in the next subsections.

4.1 Expectations-based Phillips Curve

Tables 1 to 3 report the estimated coefficients for the regression models given by equations (11) and (12) for $h = 1, 2, 5$, respectively. Starting with the results for $h = 1$ provided in Table 1 and relying on the very basic pooled regression model, we find a significantly negative Phillips curve relationship between inflation expectations and unemployment expectations of around -0.18. The inclusion of lagged inflation expectations substantially increases the explanatory power of the model (the adjusted R^2 increases from 0.17 to 0.58). The coefficient of lagged inflation expectations lies around 0.75, and the Phillips curve coefficient drops in magnitude to just -0.06 but is still significantly different from zero. The consideration of forecaster-specific effects does not add much to the explanatory power and does not change anything. The inclusion of time-fixed effects is much more important: it raises the model's explanatory power to 0.73. This is not surprising when considering the sample period running from 1999 to 2023, which includes severe crises and the corresponding policy responses to them. The Phillips curve coefficient stays relatively robust to this change, only the coefficient of lagged inflation expectations is lowered substantially. The results also remain relatively robust when using the Arellano and Bond (1991) GMM estimator.

When also including the anchoring measure and the two interaction terms, we find, first of all, that the anchoring measure itself has a significantly negative association with inflation expectations (at the 5% level). This is fully plausible as a lower degree of anchoring usually corresponds

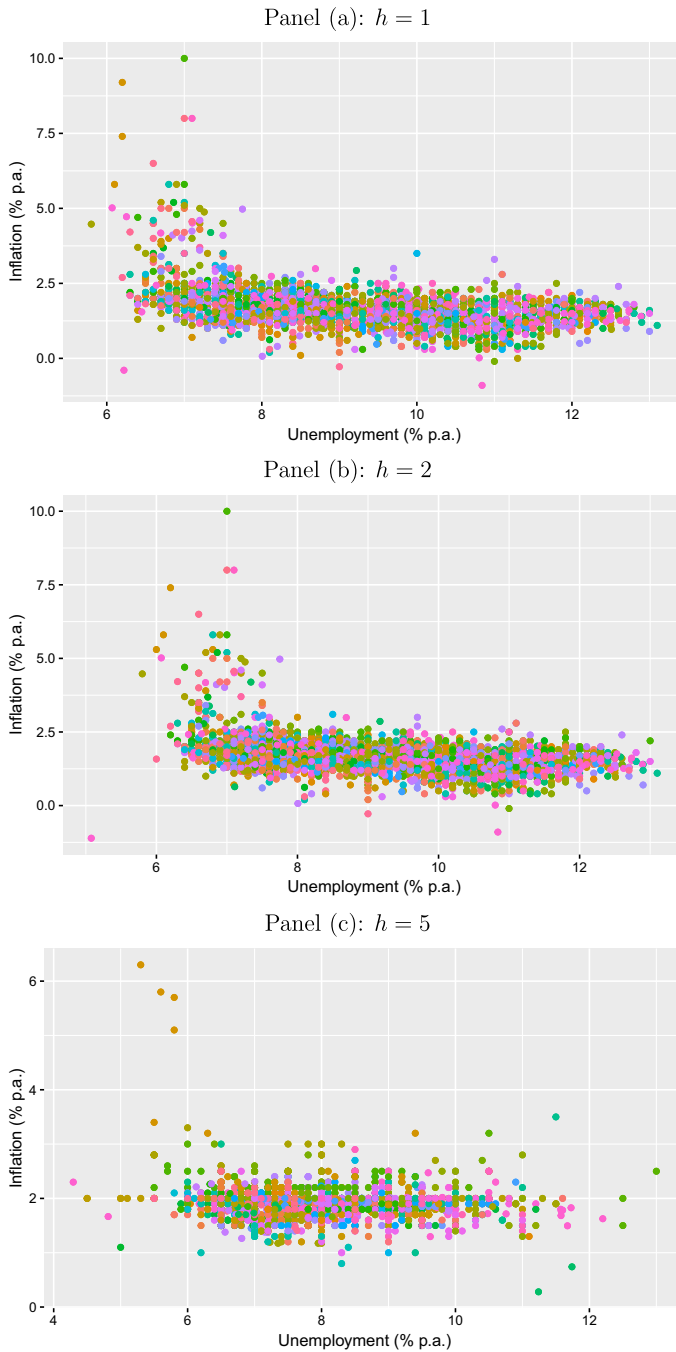


Figure 5. Phillips curve expectations relationship. The plots illustrate the relationship between inflation expectations and unemployment expectations for the Euro Area on an individual forecaster level for different horizons h (one-year-ahead, two-years-ahead, and five-years-ahead) for the period from 1999Q1 to 2023Q1 taken from the ECB Survey of Professional Forecasters. Each point color refers to a different forecaster.

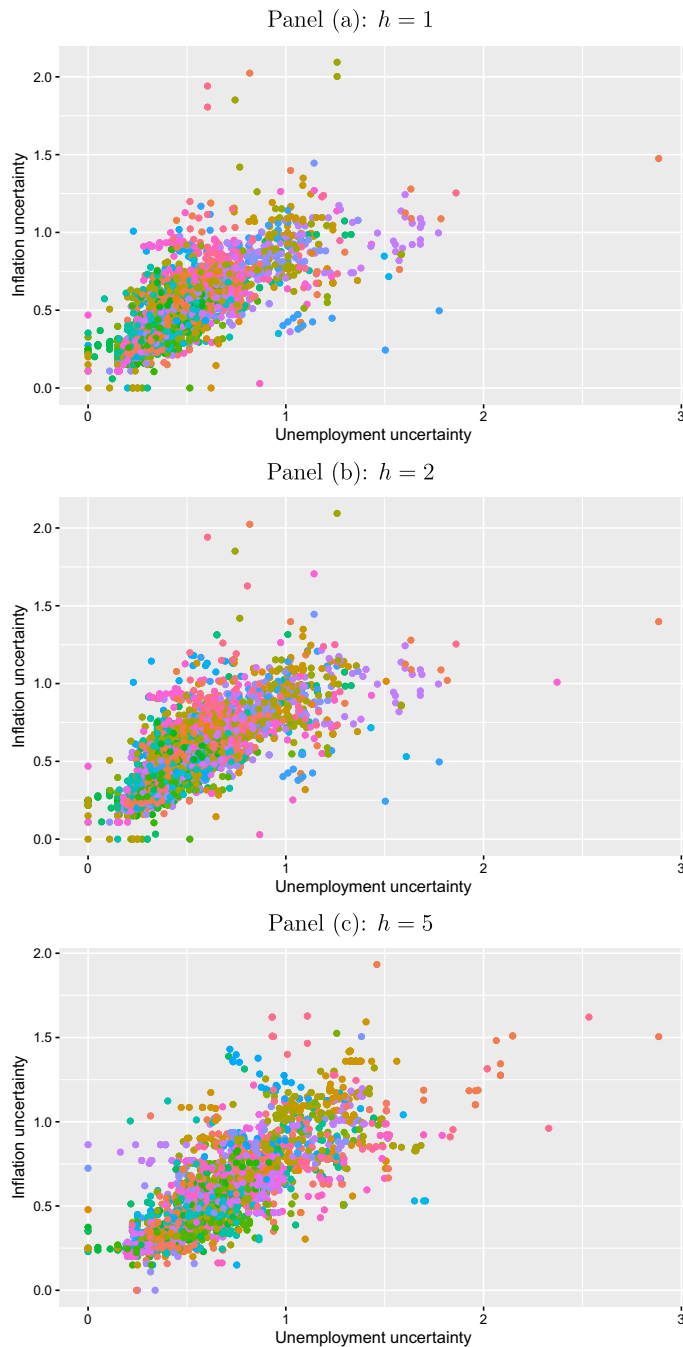


Figure 6. Phillips curve uncertainty relationship. The plots illustrate the relationship between inflation uncertainty and unemployment uncertainty for the Euro Area on an individual forecaster level for different horizons h (one-year-ahead, two-years-ahead, and five-years-ahead) for the period from 1999Q1 to 2023Q1 taken from the ECB Survey of Professional Forecasters. Each point color refers to a different forecaster. Uncertainty is proxied by the standard deviation of each forecasters density forecast.

Table 1. Phillips curve expectations regression results for $h = 1$

	Individual-level panel data							Aggregated time-series data			
	Basic	Lagged	FE	FE	FE+	AB	CO	Basic	Lagged	Anchor	CO
$E_{i,t}(u_{t+h})$	-0.1759	-0.0618	-0.0656	-0.0645	-0.0203	-0.0852	-0.0193	-0.1915	-0.0498	-0.0522	-0.1010
SE	(0.0141)	(0.0058)	(0.0065)	(0.0244)	(0.0199)	(0.0114)	(0.0199)	(0.0707)	(0.0225)	(0.0245)	(0.0327)
p -value	[0.0000]	[0.0000]	[0.0000]	[0.0082]	[0.3073]	[0.0000]	[0.3327]	[0.0080]	[0.0295]	[0.0355]	[0.0027]
$E_{i,t-1}(\pi_{t+h})$		0.7532	0.7454	0.4386	0.3439	0.5443	0.3337		0.8801	0.7185	0.4052
SE		(0.0383)	(0.0412)	(0.0542)	(0.0227)	(0.0446)	(0.0227)		(0.0972)	(0.0875)	(0.0748)
p -value		[0.0000]	[0.0000]	[0.0000]	[0.0000]	[0.0000]	[0.0000]		[0.0000]	[0.0000]	[0.0000]
Intercept	3.2735	0.9945						3.4145	0.6755	0.9754	1.9373
SE	(0.1326)	(0.0949)						(0.6448)	(0.2614)	(0.3371)	(0.3607)
p -value	[0.0000]	[0.0000]						[0.0000]	[0.0113]	[0.0048]	[0.0000]
$Anchor_{i,t,h}$					-0.3181		-0.3251			-5.7188	-5.7902
SE					(0.1559)		(0.1569)			(1.8719)	(0.7163)
p -value					[0.0414]		[0.0385]			[0.0030]	[0.0000]
$Anchor_{i,t,h} \times E_{i,t}(u_{t+h})$					0.0742		0.0754			0.5753	0.5669
SE					(0.0157)		(0.0158)			(0.1719)	(0.0699)
p -value					[0.0000]		[0.0000]			[0.0012]	[0.0000]
$Anchor_{i,t,h} \times E_{i,t-1}(\pi_{t+h})$					-0.0789		-0.0792			0.3486	0.3369
SE					(0.0094)		(0.0095)			(0.1733)	(0.0784)
p -value					[0.0000]		[0.0000]			[0.0472]	[0.0000]

Table 1. Continued.

	Individual-level panel data							Aggregated time-series data			
	Basic	Lagged	FE	FE	FE+	AB	CO	Basic	Lagged	Anchor	CO
Forecasters FE	No	No	Yes	Yes	Yes	Yes	Yes	No	No	No	No
Time FE	No	No	No	Yes	Yes	Yes	Yes	No	No	No	No
\bar{R}^2	0.1689	0.5823	0.5818	0.7300	0.7635	0.8292	0.7858	0.2538	0.7901	0.9054	0.7685
$T \times N$	3566	2992	2992	2992	1674	2992	1674	97	96	96	96

Note: The table reports coefficient estimates, heteroskedasticity and autocorrelation robust (HAC) standard errors (SE) according to Arellano (1987), p -values, the adjusted R^2 (\bar{R}^2) and the number of observations ($T \times N$) for different versions of the following general regression model:

$$E_{i,t}(\pi_{t+h}) = \beta_1 E_{i,t}(u_{t+h}) + \beta_2 E_{i,t-1}(\pi_{t+h}) + \beta_3 \text{Anchor}_{i,t,h} + \beta_4 \text{Anchor}_{i,t,h} \times E_{i,t}(u_{t+h}) + \beta_5 \text{Anchor}_{i,t,h} \times E_{i,t-1}(\pi_{t+h}) + \mu_i + \gamma_t + \varepsilon_{i,t}$$

where $E_{i,t}(\pi_{t+h})$ represents inflation expectations made in period t by forecaster i for a horizon of h -years-ahead, $E_{i,t}(u_{t+h})$ denotes the corresponding unemployment expectations, $E_{i,t-1}(\pi_{t+h})$ gives inflation expectations made in the previous quarter, and $\text{Anchor}_{i,t,h}$ is a proxy measuring the individual degree of anchoring of inflation expectations. μ_i , γ_t , and $\varepsilon_{i,t}$ characterize time-invariant forecaster-specific fixed effects, time-fixed effects, and idiosyncratic errors, respectively. This general regression model has been restricted to a pooled regression model with (Lagged) and without lagged inflation expectations (Basic), to a fixed-effects (FE) model with and without time-fixed effects and the anchoring measure (FE+). In addition, we have also estimated the model applying the Arellano and Bond (1991) GMM estimator (AB) and an iterative Cochrane and Orcutt (1949) estimator (CO). The same model has also been estimated for aggregated time-series data using cross-sectional means across forecasters:

$$\bar{E}_t(\pi_{t+h}) = \beta_0 + \beta_1 \bar{E}_t(u_{t+h}) + \beta_2 \bar{E}_{t-1}(\pi_{t+h}) + \beta_3 \overline{\text{Anchor}}_{t,h} + \beta_4 \overline{\text{Anchor}}_{t,h} \times \bar{E}_t(u_{t+h}) + \beta_5 \overline{\text{Anchor}}_{t,h} \times \bar{E}_{t-1}(\pi_{t+h}) + \varepsilon_t.$$

Table 2. Phillips curve expectations regression results for $h = 2$

	Individual-level panel data							Aggregated time-series data			
	Basic	Lagged	FE	FE	FE+	AB	CO	Basic	Lagged	Anchor	CO
$E_{i,t}(u_{t+h})$	-0.1500	-0.0741	-0.0797	-0.0762	-0.0594	-0.0859	-0.0584	-0.1632	-0.0710	-0.0755	-0.1661
SE	(0.0121)	(0.0059)	(0.0064)	(0.0195)	(0.0177)	(0.0145)	(0.0179)	(0.0704)	(0.0253)	(0.0346)	(0.0382)
p -value	[0.0000]	[0.0000]	[0.0000]	[0.0001]	[0.0008]	[0.0000]	[0.0012]	[0.0227]	[0.0060]	[0.0319]	[0.0000]
$E_{i,t-1}(\pi_{t+h})$		0.5927	0.5780	0.3522	0.2540	0.4806	0.2218		0.6467	0.2879	-0.0007
SE		(0.0342)	(0.0353)	(0.0412)	(0.0249)	(0.0325)	(0.0250)		(0.2362)	(0.1612)	(0.0666)
p -value		[0.0000]	[0.0000]	[0.0000]	[0.0000]	[0.0000]	[0.0000]		[0.0074]	[0.0775]	[0.9916]
Intercept	3.0540	1.3639						3.1639	1.2421	1.8831	3.1796
SE	(0.1120)	(0.0848)						(0.6493)	(0.5259)	(0.5403)	(0.3924)
p -value	[0.0000]	[0.0000]						[0.0000]	[0.0203]	[0.0008]	[0.0000]
$\text{Anchor}_{i,t,h}$					-0.2296		-0.2785			-5.5891	-5.5922
SE					(0.1673)		(0.1693)			(2.6208)	(0.8314)
p -value					[0.1702]		[0.1001]			[0.0357]	[0.0000]
$\text{Anchor}_{i,t,h} \times E_{i,t}(u_{t+h})$					0.0861		0.0917			0.6473	0.5785
SE					(0.0146)		(0.0148)			(0.2512)	(0.0820)
p -value					[0.0000]		[0.0000]			[0.0116]	[0.0000]
$\text{Anchor}_{i,t,h} \times E_{i,t-1}(\pi_{t+h})$					-0.1571		-0.1537			0.1188	0.2308
SE					(0.0387)		(0.0390)			(0.2216)	(0.0861)
p -value					[0.0001]		[0.0001]			[0.5933]	[0.0088]

Table 2. Continued.

	Individual-level panel data							Aggregated time-series data			
	Basic	Lagged	FE	FE	FE+	AB	CO	Basic	Lagged	Anchor	CO
Forecasters FE	No	No	Yes	Yes	Yes	Yes	Yes	No	No	No	No
Time FE	No	No	No	Yes	Yes	Yes	Yes	No	No	No	No
\bar{R}^2	0.1475	0.4367	0.4396	0.7000	0.6929	0.7542	0.7145	0.2252	0.5625	0.8150	0.8007
$T \times N$	3487	2895	2895	2895	1570	2895	1570	97	96	96	96

Note: The table reports coefficient estimates, heteroskedasticity and autocorrelation robust (HAC) standard errors (SE) according to Arellano (1987), *p*-values, the adjusted R^2 (\bar{R}^2) and the number of observations ($T \times N$) for different versions of the following general regression model:

$$E_{i,t}(\pi_{t+h}) = \beta_1 E_{i,t}(u_{t+h}) + \beta_2 E_{i,t-1}(\pi_{t+h}) + \beta_3 \text{Anchor}_{i,t,h} + \beta_4 \text{Anchor}_{i,t,h} \times E_{i,t}(u_{t+h}) + \beta_5 \text{Anchor}_{i,t,h} \times E_{i,t-1}(\pi_{t+h}) + \mu_i + \gamma_t + \varepsilon_{i,t}$$

where $E_{i,t}(\pi_{t+h})$ represents inflation expectations made in period t by forecaster i for a horizon of h -years-ahead, $E_{i,t}(u_{t+h})$ denotes the corresponding unemployment expectations, $E_{i,t-1}(\pi_{t+h})$ gives inflation expectations made in the previous quarter, and $\text{Anchor}_{i,t,h}$ is a proxy measuring the individual degree of anchoring of inflation expectations. μ_i , γ_t , and $\varepsilon_{i,t}$ characterize time-invariant forecaster-specific fixed effects, time fixed effects, and idiosyncratic errors, respectively. This general regression model has been restricted to a pooled regression model with (Lagged) and without lagged inflation expectations (Basic), to a fixed-effects (FE) model with and without time fixed effects and the anchoring measure (FE+). In addition, we have also estimated the model applying the Arellano and Bond (1991) GMM estimator (AB) and an iterative Cochrane and Orcutt (1949) estimator (CO). The same model has also been estimated for aggregated time-series data using cross-sectional means across forecasters:

$$\bar{E}_t(\pi_{t+h}) = \beta_0 + \beta_1 \bar{E}_t(u_{t+h}) + \beta_2 \bar{E}_{t-1}(\pi_{t+h}) + \beta_3 \overline{\text{Anchor}}_{t,h} + \beta_4 \overline{\text{Anchor}}_{t,h} \times \bar{E}_t(u_{t+h}) + \beta_5 \overline{\text{Anchor}}_{t,h} \times \bar{E}_{t-1}(\pi_{t+h}) + \varepsilon_t.$$

Table 3. Phillips curve expectations regression results for $h = 5$

	Individual-level panel data							Aggregated time-series data			
	Basic	Lagged	FE	FE	FE+	AB	CO	Basic	Lagged	Anchor	CO
$E_{i,t}(u_{t+h})$	-0.0160	-0.0088	-0.0095	-0.0124	-0.0044	-0.0227	-0.0025	-0.0135	-0.0113	-0.0170	-0.0176
SE	(0.0132)	(0.0037)	(0.0043)	(0.0094)	(0.0059)	(0.0290)	(0.0062)	(0.0157)	(0.0053)	(0.0085)	(0.0068)
p -value	[0.2280]	[0.0183]	[0.0292]	[0.1907]	[0.4557]	[0.4354]	[0.6827]	[0.3926]	[0.0342]	[0.0489]	[0.0118]
$E_{i,t-1}(\pi_{t+h})$		0.8289	0.7624	0.7058	0.5936	0.7774	0.5509		0.9374	0.8839	0.8141
SE		(0.0474)	(0.0489)	(0.0542)	(0.0206)	(0.2368)	(0.0214)		(0.0556)	(0.0593)	(0.0634)
p -value		[0.0000]	[0.0000]	[0.0000]	[0.0000]	[0.0010]	[0.0000]		[0.0000]	[0.0000]	[0.0000]
Intercept	2.0243	0.3961						1.9999	0.2113	0.3590	0.4968
SE	(0.1106)	(0.0769)						(0.1134)	(0.1006)	(0.1175)	(0.1388)
p -value	[0.0000]	[0.0000]						[0.0000]	[0.0386]	[0.0030]	[0.0006]
$\text{Anchor}_{i,t,h}$					0.7326		0.7558			0.0604	0.2742
SE					(0.1030)		(0.1060)			(0.7383)	(0.9082)
p -value					[0.0000]		[0.0000]			[0.9350]	[0.7635]
$\text{Anchor}_{i,t,h} \times E_{i,t}(u_{t+h})$					0.0252		0.0257			0.1269	0.1492
SE					(0.0094)		(0.0097)			(0.0778)	(0.0755)
p -value					[0.0078]		[0.0078]			[0.1067]	[0.0515]
$\text{Anchor}_{i,t,h} \times E_{i,t-1}(\pi_{t+h})$					-0.4707		-0.4846			-0.5440	-0.7397
SE					(0.0402)		(0.0416)			(0.4725)	(0.3908)
p -value					[0.0000]		[0.0000]			[0.2530]	[0.0620]

Table 3. Continued.

	Individual-level panel data							Aggregated time-series data			
	Basic	Lagged	FE	FE	FE+	AB	CO	Basic	Lagged	Anchor	CO
Forecasters FE	No	No	Yes	Yes	Yes	Yes	Yes	No	No	No	No
Time FE	No	No	No	Yes	Yes	Yes	Yes	No	No	No	No
\bar{R}^2	0.0039	0.7051	0.7143	0.7322	0.7101	0.8917	0.7139	0.0017	0.8477	0.8521	0.7937
$T \times N$	3030	2454	2454	2454	1267	2454	1267	91	88	88	88

Note: The table reports coefficient estimates, heteroskedasticity and autocorrelation robust (HAC) standard errors (SE) according to Arellano (1987), p -values, the adjusted R^2 (\bar{R}^2) and the number of observations ($T \times N$) for different versions of the following general regression model:

$$E_{i,t}(\pi_{t+h}) = \beta_1 E_{i,t}(u_{t+h}) + \beta_2 E_{i,t-1}(\pi_{t+h}) + \beta_3 \text{Anchor}_{i,t,h} + \beta_4 \text{Anchor}_{i,t,h} \times E_{i,t}(u_{t+h}) + \beta_5 \text{Anchor}_{i,t,h} \times E_{i,t-1}(\pi_{t+h}) + \mu_i + \gamma_t + \varepsilon_{i,t}$$

where $E_{i,t}(\pi_{t+h})$ represents inflation expectations made in period t by forecaster i for a horizon of h -years-ahead, $E_{i,t}(u_{t+h})$ denotes the corresponding unemployment expectations, $E_{i,t-1}(\pi_{t+h})$ gives inflation expectations made in the previous quarter, and $\text{Anchor}_{i,t,h}$ is a proxy measuring the individual degree of anchoring of inflation expectations. μ_i , γ_t , and $\varepsilon_{i,t}$ characterize time-invariant forecaster-specific fixed effects, time-fixed effects, and idiosyncratic errors, respectively. This general regression model has been restricted to a pooled regression model with (Lagged) and without lagged inflation expectations (Basic), to a fixed effects (FE) model with and without time-fixed effects, and the anchoring measure (FE+). In addition, we have also estimated the model applying the Arellano and Bond (1991) GMM estimator (AB) and an iterative Cochrane and Orcutt (1949) estimator (CO). The same model has also been estimated for aggregated time-series data using cross-sectional means across forecasters:

$$\bar{E}_t(\pi_{t+h}) = \beta_0 + \beta_1 \bar{E}_t(u_{t+h}) + \beta_2 \bar{E}_{t-1}(\pi_{t+h}) + \beta_3 \bar{\text{Anchor}}_{t,h} + \beta_4 \bar{\text{Anchor}}_{t,h} \times \bar{E}_t(u_{t+h}) + \beta_5 \bar{\text{Anchor}}_{t,h} \times \bar{E}_{t-1}(\pi_{t+h}) + \varepsilon_t.$$

to an increase in inflation expectations. In addition, we also see that the Phillips curve coefficient lowers in magnitude and becomes insignificant. For the corresponding interaction term, we also observe that it even switches the sign. The coefficient of lagged inflation expectations also decreases itself and decreases further when taken the corresponding interaction term into account. This is also plausible as a higher degree of anchoring stabilizes inflation expectations and therefore reduces its persistence. The results achieved from the iterative Cochrane and Orcutt (1949) estimation are nearly identical.

The time-series regression models on the aggregated level basically confirm the findings discussed above; however, in this case, the Phillips curve coefficient remains statistically significant at least at the 5% level even after controlling for the degree of anchoring. The coefficient ranges between -0.05 and -0.1 . A similar conclusion is achieved when considering the findings for the forecast horizon $h = 2$ provided in Table 2. The results basically confirm the findings discussed above for $h = 1$; however, the Phillips curve coefficient is statistically significant at least at the 5% level in all specifications ranging between -0.06 and -0.17 . This clearly changes when considering the medium-run horizon ($h = 5$) provided in Table 3. In this case, the Phillips curve coefficient is quite low in magnitude and insignificant for most of the panel data specification. Only the time-series models provide some evidence for the existence of the expectation-based Phillips curve relationship over a longer forecast horizon.

Overall, for lower forecast horizons (i.e., one- and two-years-ahead), we find evidence for a low but mostly significant Phillips curve coefficient confirming that professional forecasters make forecasts for inflation and unemployment, which are roughly in line with the traditional Phillips curve concept. We also observe that a large part of the variation is explained by past inflation expectations and time-fixed effects while forecaster-specific fixed effects do not add much explanatory power. The consideration of the anchoring measure indicates some nonlinearity in the relationship. For an average degree of anchoring (i.e., $\text{Anchor}_{i,t,h} = 0$), there is a small but negative Phillips curve relationship between expectations for inflation and unemployment. This association is also statistically significant at a 1% level for $h = 2$. For a lower degree of anchoring (i.e., $\text{Anchor}_{i,t,h} < 0$), this negative connection becomes much stronger while it disappears for a higher degree of anchoring (i.e., $\text{Anchor}_{i,t,h} > 0$). The latter might be explained by fact that a high degree of anchoring results in stable inflation expectations close to the inflation target of the ECB of 2%, which are detached from unemployment expectations. This argument is also in line with our observation that unemployment expectations show a much stronger variation compared to inflation expectations within the sample period (see Figure 5). This might also explain why the Phillips curve relationship mostly disappears for medium-run forecasts (i.e., for five-years-ahead forecasts).

4.2 Expectation-based accelerationist Phillips Curve

As an additional robustness check, in Table 4, we have also considered the case of an expectations-based accelerationist Phillips curve version (Blanchard, 2016; Hazell et al. 2022). Compared to equation (11), we basically assume a high persistence of inflation expectations and therefore set the β_2 coefficient equal to unity:

$$E_{i,t}(\pi_{t+h}) - E_{i,t-1}(\pi_{t+h}) = \beta_1 E_{i,t}(u_{t+h}) + \mu_i + \gamma_t + \varepsilon_{i,t}. \quad (17)$$

However, either the adjusted R^2 s are extremely low or the Phillips curve coefficient is insignificant. The latter is especially true after controlling for time-fixed effects, which explain most of the variation in the change of inflation expectations. We see this as evidence against the expectations-based accelerationist Phillips curve version.

Table 4. Accelerationist Phillips curve expectations regression results

	Basic	FE	FE	Basic TS
$E_{i,t}(u_{t+h})$	-0.0256	-0.0284	-0.0168	-0.0307
SE	(0.0053)	(0.0057)	(0.0247)	(0.0252)
p -value	[0.0000]	[0.0000]	[0.4979]	[0.2255]
Intercept	0.2559			0.3042
$h = 1$ SE	(0.0522)			(0.2499)
p -value	[0.0000]			[0.2265]
Forecasters FE	No	Yes	Yes	No
Time FE	No	No	Yes	No
\bar{R}^2	0.0076	0.0047	0.2391	0.0199
$T \times N$	2992	2992	2992	96
$E_{i,t}(u_{t+h})$	-0.0227	-0.0273	-0.0194	-0.0206
SE	(0.0049)	(0.0054)	(0.0203)	(0.0315)
p -value	[0.0000]	[0.0000]	[0.3373]	[0.5145]
Intercept	0.2097			0.1917
$h = 2$ SE	(0.0477)			(0.3094)
p -value	[0.0000]			[0.5369]
Forecasters FE	No	Yes	Yes	No
Time FE	No	No	Yes	No
\bar{R}^2	0.0046	0.0024	0.3963	-0.0037
$T \times N$	2895	2895	2895	96
$E_{i,t}(u_{t+h})$	-0.0077	-0.0083	-0.0049	-0.0112
SE	(0.0035)	(0.0042)	(0.0089)	(0.0055)
p -value	[0.0301]	[0.0512]	[0.5850]	[0.0438]
Intercept	0.0625			0.0917
$h = 5$ SE	(0.0288)			(0.0452)
p -value	[0.0301]			[0.0455]
Forecasters FE	No	Yes	Yes	No
Time FE	No	No	Yes	No
\bar{R}^2	0.0028	-0.0074	0.0201	0.0426
$T \times N$	2454	2454	2454	88

Note: The table reports coefficient estimates, heteroskedasticity and autocorrelation robust (HAC) standard errors (SE) according to Arellano (1987), p -values, the adjusted R^2 (\bar{R}^2) and the number of observations ($T \times N$) for different versions of the following general regression model:

$$E_{i,t}(\pi_{t+h}) - E_{i,t-1}(\pi_{t+h}) = \beta_1 E_{i,t}(u_{t+h}) + \mu_i + \gamma_t + \varepsilon_{i,t}$$

where $E_{i,t}(\pi_{t+h}) - E_{i,t-1}(\pi_{t+h})$ represents the change in inflation expectations between $t - 1$ and t by forecaster i for a horizon of h -years-ahead, and $E_{i,t}(u_{t+h})$ denotes the corresponding unemployment expectations. μ_i , γ_t , and $\varepsilon_{i,t}$ characterize time-invariant forecaster-specific fixed effects, time-fixed effects, and idiosyncratic errors, respectively. This general regression model has also been restricted to a pooled regression model (Basic) and to a fixed effects (FE) model with and without time fixed effects. The same model has also been estimated for aggregated time-series data (Basic TS) using cross-sectional means across forecasters:

$$\bar{E}_t(\pi_{t+h}) - \bar{E}_{t-1}(\pi_{t+h}) = \beta_0 + \beta_1 \bar{E}_t(u_{t+h}) + \varepsilon_t.$$

4.3 Heterogeneity across forecasters and over time

We also study the heterogeneity of the Phillips curve relationship across individual forecasters by using time-series regressions of inflation expectations on their lag and unemployment expectations. Figure 7 displays the corresponding Phillips curve coefficients together with their robust standard errors for each of the three forecast horizons ($h = 1, 2, 5$). It can be seen that the degree of heterogeneity of the individual forecasters' coefficient estimates is relatively low. This is in line with our previous finding in the fixed effects regression framework that forecaster-specific effects do not add much to the explanatory power. Most of the coefficients are low but negative corresponding to the concept of the Phillips curve. For the expectations over short-run horizons ($h = 1, 2$) the corresponding coefficient is negative for more than 90% of forecasters. Over the longer forecast horizon it is still negative for more than 70% of forecasters. The red colored points represent coefficients that are significantly different from zero at a 5% level. This is the case for more than 30% of forecasters for $h = 1, 2$ and for around 12% for $h = 5$.¹¹ Overall, we also find evidence in favor of the Phillips curve relationship between expectations considered on an individual level but again the association becomes smaller for a higher forecast horizon.

The world economy has been hit by several major shocks over the recent decades, which results in the necessity to allow for time-variation in the expectation building mechanism and the relationship between inflation and unemployment. Figure 8 also plots a time-varying Phillips curve coefficient together with the corresponding adjusted R^2 relying on a rolling-window fixed effects regression using a window size of 20 quarters, which corresponds to five years. Again the red colored dots refer to periods, in which the coefficient is significantly different from zero. Overall, we see a large variation in the relationship over time when referring to both the Phillips curve coefficient or the explanatory power of the variation in inflation expectations measured by the adjusted R^2 . This finding is in line with the importance of time-fixed effects already discussed above (see Section 4.1). For shorter forecast horizons ($h = 1, 2$) the most significant Phillips curve association is observed around the global financial crisis (i.e., between 2006 and 2009) and the period characterized by ultra-low interest rates (i.e., between 2014 and 2020). For the longer forecast horizon ($h = 5$), we find a long period of a pretty stable and significant Phillips curve relationship between 2012 and 2017. However, the association is the highest for the most recent high inflation period. This is also indicated by a substantial increase of the adjusted R^2 to a level around 0.8 observed for each forecast horizon. This seems plausible as in this period the degree of anchoring of inflation expectations has started to deteriorate as seen in Figures 1 and 4.

4.4 Phillips Curve-based uncertainty relationship

In the following, we also discuss estimation results carried out for the relationship between the forecasters' uncertainties regarding inflation and unemployment based on the Phillips curve concept. We are focusing on the co-movement between two different categories of uncertainty while the previous literature often focuses on cross-country spillovers of different uncertainty measures (Klößner and Sekkel, 2014; Caggiano et al. 2020; Thiem, 2020; Beckmann et al. 2023). The corresponding findings are summarized in Tables 5 to 7 for the three forecast horizons ($h = 1, 2, 5$). Across all different specifications, there is a positive connection between inflation and unemployment uncertainty, which is highly significant and robust across the forecast horizons. Accounting for the anchoring measure even strengthens the relationship between uncertainties regarding the two macro variables. More than 50% of the variation in inflation uncertainty is explained by unemployment uncertainty when referring to the adjusted R^2 .

This shows that the uncertainties regarding both macro variables move together in line with the Phillips curve framework. This is particular relevant in the most recent high inflation period. On the one hand, uncertainty regarding the length and strength of the high inflation period also raises uncertainty regarding future unemployment. On the other hand, uncertainty regarding

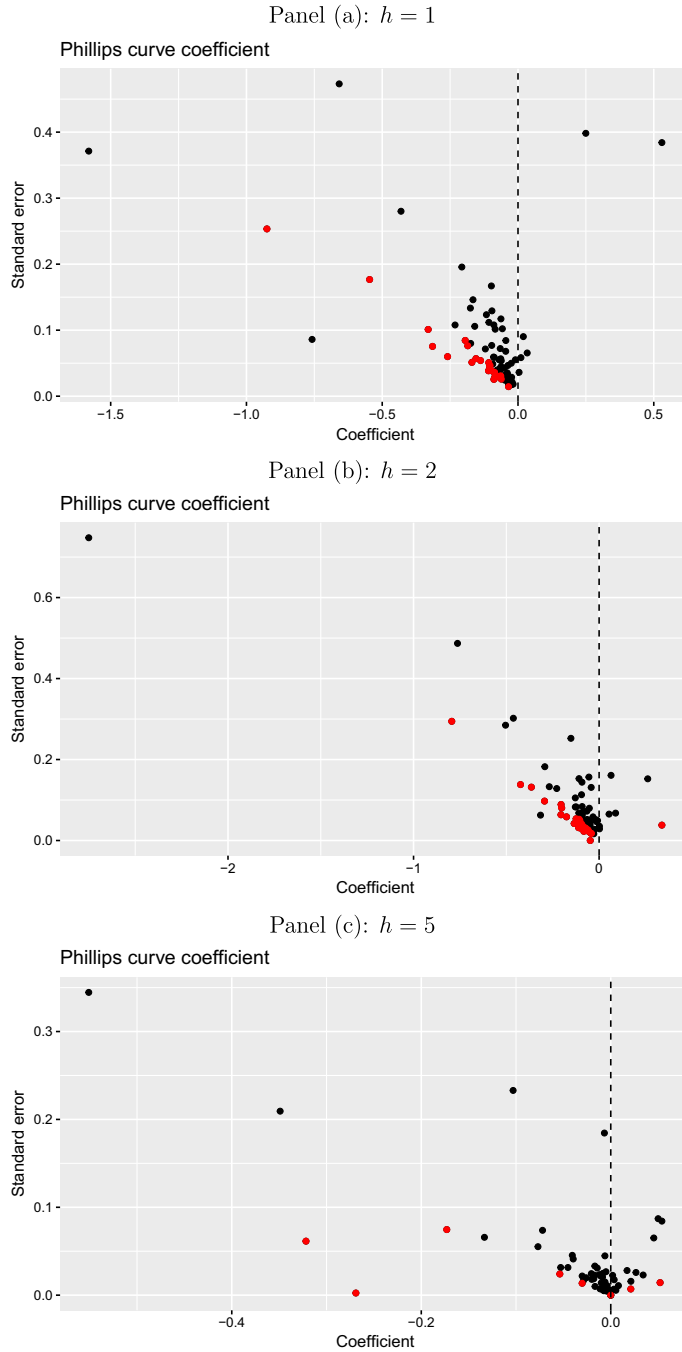


Figure 7. Individual Phillips curve expectations coefficients. The plots illustrate the estimated Phillips curve expectations coefficients and their standard errors from a regression of inflation expectations on unemployment expectations and lagged inflation expectations for the Euro Area on an individual forecaster level for different horizons h (one-year-ahead, two-years-ahead, and five-years-ahead) for the period from 1999Q1 to 2023Q1 taken from the ECB Survey of Professional Forecasters. The red colored points refer to coefficients, which are significantly different from zero at a 5% level.

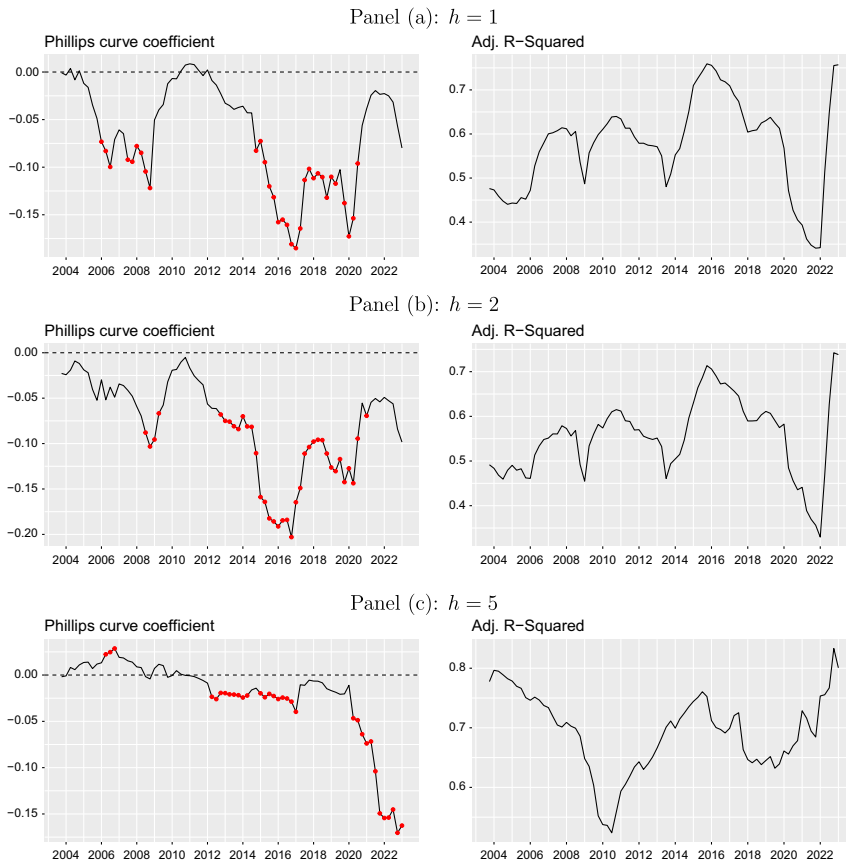


Figure 8. Time-varying Phillips curve expectations coefficients. The plots illustrate the Phillips curve expectations coefficients and corresponding adjusted R^2 s estimated by rolling-window fixed effects regressions of inflation expectations on unemployment expectations and lagged inflation expectations for the Euro Area using panel data for different horizons h (one-year-ahead, two-years-ahead, and five-years-ahead) for the period from 1999Q1 to 2023Q1 taken from the ECB Survey of Professional Forecasters. The red colored points refer to coefficients, which are significantly different from zero at a 5% level. The window size is 20 quarters (= five years).

unemployment due to a potential recession forced by higher energy prices or by a tightening of monetary policy also favors a higher uncertainty regarding future inflation.

The finding of a significantly positive relationship between uncertainty regarding inflation and unemployment is also confirmed on an individual forecaster level (see Figure 9) and when allowing the coefficient to change over time (see Figure 10). Especially, the latter underlines the robustness of this finding even further.

5. Summary and concluding remarks

The present study contributes to the existing literature by studying the expectation formation mechanism of professional forecasters. In doing so, we reassess whether forecasters form their expectations regarding future inflation and unemployment consistent with the concept of the Phillips curve. The contribution of our study to this specific strand of the literature is threefold. First, we do not solely focus on point forecasts but also take into account information of individual forecasts for the entire distribution. Second, we explicitly address the role of anchoring of

Table 5. Phillips curve uncertainty regression results for $h = 1$

	Individual-level panel data							Aggregated time-series data			
	Basic	Lagged	FE	FE	FE+	AB	CO	Basic	Lagged	Anchor	CO
$\sigma_{i,t}(u_{t+h})$	0.6658	0.2135	0.2339	0.2195	0.2110	0.2005	0.2094	0.7894	0.2868	0.2653	0.4695
SE	(0.0328)	(0.0199)	(0.0214)	(0.0202)	(0.0156)	(0.0443)	(0.0155)	(0.0788)	(0.0722)	(0.0685)	(0.0725)
p -value	[0.0000]	[0.0000]	[0.0000]	[0.0000]	[0.0000]	[0.0000]	[0.0000]	[0.0000]	[0.0001]	[0.0002]	[0.0000]
$\sigma_{i,t-1}(\pi_{t+h})$		0.7219	0.6259	0.5896	0.4635	0.0945	0.4685		0.6663	0.5559	-0.1974
SE		(0.0271)	(0.0368)	(0.0364)	(0.0194)	(0.0464)	(0.0194)		(0.0780)	(0.0768)	(0.0827)
p -value		[0.0000]	[0.0000]	[0.0000]	[0.0000]	[0.0418]	[0.0000]		[0.0000]	[0.0000]	[0.0191]
Intercept	0.1799	0.0386						0.1166	0.0297	0.1033	0.4678
SE	(0.0157)	(0.0064)						(0.0379)	(0.0162)	(0.0250)	(0.0862)
p -value	[0.0000]	[0.0000]						[0.0027]	[0.0702]	[0.0001]	[0.0000]
Anchor $_{i,t,h}$					-0.0029		-0.0028			-0.1925	-0.1806
SE					(0.0118)		(0.0117)			(0.0638)	(0.0614)
p -value					[0.8038]		[0.8112]			[0.0033]	[0.0041]
Anchor $_{i,t,h} \times \sigma_{i,t}(u_{t+h})$					0.0926		0.0918			0.1092	0.2392
SE					(0.0222)		(0.0221)			(0.1453)	(0.1327)
p -value					[0.0000]		[0.0000]			[0.4544]	[0.0748]
Anchor $_{i,t,h} \times \sigma_{i,t-1}(\pi_{t+h})$					-0.2656		-0.2642			0.1187	-0.0102
SE					(0.0220)		(0.0220)			(0.1131)	(0.1295)
p -value					[0.0000]		[0.0000]			[0.2967]	[0.9377]

Table 5. Continued.

	Individual-level panel data							Aggregated time-series data			
	Basic	Lagged	FE	FE	FE+	AB	CO	Basic	Lagged	Anchor	CO
Forecasters FE	No	No	Yes	Yes	Yes	Yes	Yes	No	No	No	No
Time FE	No	No	No	Yes	Yes	Yes	Yes	No	No	No	No
\bar{R}^2	0.5691	0.8095	0.8189	0.8266	0.8565	0.9440	0.8747	0.8628	0.9420	0.9508	0.4825
$T \times N$	3566	2992	2992	2992	1674	2992	1674	97	96	96	96

Note: The table reports coefficient estimates, heteroskedasticity and autocorrelation robust (HAC), standard errors (SE) according to Arellano (1987), p -values, the adjusted R^2 (\bar{R}^2), and the number of observations ($T \times N$) for different versions of the following general regression model:

$$\sigma_{i,t}(\pi_{t+h}) = \beta_1 \sigma_{i,t}(u_{t+h}) + \beta_2 \sigma_{i,t-1}(\pi_{t+h}) + \beta_3 \text{Anchor}_{i,t,h} + \beta_4 \text{Anchor}_{i,t,h} \times \sigma_{i,t}(u_{t+h}) + \beta_5 \text{Anchor}_{i,t,h} \times \sigma_{i,t-1}(\pi_{t+h}) + \mu_i + \gamma_t + \varepsilon_{i,t}$$

where $\sigma_{i,t}(\pi_{t+h})$ represents inflation uncertainty proxied by the standard deviation of density forecasts made in period t by forecaster i for a horizon of h -years-ahead, $\sigma_{i,t}(u_{t+h})$ denotes the correspondingly computed unemployment uncertainty, $\sigma_{i,t-1}(\pi_{t+h})$ gives inflation uncertainty based on the previous quarters density forecast, and $\text{Anchor}_{i,t,h}$ is a proxy measuring the individual degree of anchoring of inflation expectations. μ_i , γ_t , and $\varepsilon_{i,t}$ characterize time-invariant forecaster-specific fixed effects, time fixed effects, and idiosyncratic errors, respectively. This general regression model has been restricted to a pooled regression model with (Lagged) and without lagged inflation expectations (Basic), to a fixed effects (FE) model with and without time fixed effects and the anchoring measure (FE+). In addition, we have also estimated the model applying the Arellano and Bond (1991) GMM estimator (AB) and an iterative Cochrane and Orcutt (1949) estimator (CO). The same model has also been estimated for aggregated time-series data using cross-sectional means across forecasters:

$$\bar{\sigma}_t(\pi_{t+h}) = \beta_0 + \beta_1 \bar{\sigma}_t(u_{t+h}) + \beta_2 \bar{\sigma}_{t-1}(\pi_{t+h}) + \beta_3 \overline{\text{Anchor}}_{t,h} + \beta_4 \overline{\text{Anchor}}_{t,h} \times \bar{\sigma}_t(u_{t+h}) + \beta_5 \overline{\text{Anchor}}_{t,h} \times \bar{\sigma}_{t-1}(\pi_{t+h}) + \varepsilon_t.$$

Table 6. Phillips curve uncertainty regression results for $h = 2$

	Individual-level panel data							Aggregated time-series data			
	Basic	Lagged	FE	FE	FE+	AB	CO	Basic	Lagged	Anchor	CO
$\sigma_{i,t}(u_{t+h})$	0.6767	0.2853	0.2990	0.2648	0.2453	0.2248	0.2644	0.7576	0.4607	0.5398	0.5900
SE	(0.0282)	(0.0213)	(0.0242)	(0.0248)	(0.0174)	(0.0800)	(0.0180)	(0.0613)	(0.1007)	(0.0426)	(0.0441)
p -value	[0.0000]	[0.0000]	[0.0000]	[0.0000]	[0.0000]	[0.0050]	[0.0000]	[0.0000]	[0.0000]	[0.0000]	[0.0000]
$\sigma_{i,t-1}(\pi_{t+h})$		0.6318	0.5123	0.5069	0.4102	0.9519	0.3505		0.4520	0.3510	-0.0548
SE		(0.0260)	(0.0311)	(0.0314)	(0.0200)	(0.1550)	(0.0204)		(0.1254)	(0.0902)	(0.0638)
p -value		[0.0000]	[0.0000]	[0.0000]	[0.0000]	[0.0000]	[0.0000]		[0.0005]	[0.0002]	[0.3929]
Intercept	0.1787	0.0489						0.1344	0.0513	0.0652	0.3557
SE	(0.0146)	(0.0062)						(0.0306)	(0.0401)	(0.0447)	(0.1068)
p -value	[0.0000]	[0.0000]						[0.0000]	[0.2038]	[0.1479]	[0.0013]
Anchor $_{i,t,h}$					-0.0491		-0.0528			-0.0111	-0.1328
SE					(0.0140)		(0.0143)			(0.1043)	(0.0738)
p -value					[0.0005]		[0.0002]			[0.9153]	[0.0753]
Anchor $_{i,t,h} \times \sigma_{i,t}(u_{t+h})$					-0.3116		-0.3176			0.7345	0.3273
SE					(0.0337)		(0.0333)			(0.1723)	(0.1430)
p -value					[0.0000]		[0.0000]			[0.0000]	[0.0245]
Anchor $_{i,t,h} \times \sigma_{i,t-1}(\pi_{t+h})$					0.2028		0.2056			-0.7122	-0.1289
SE					(0.0272)		(0.0259)			(0.2101)	(0.1366)
p -value					[0.0000]		[0.0000]			[0.0010]	[0.3478]

Table 6. Continued.

	Individual-level panel data							Aggregated time-series data			
	Basic	Lagged	FE	FE	FE+	AB	CO	Basic	Lagged	Anchor	CO
Forecasters FE	No	No	Yes	Yes	Yes	Yes	Yes	No	No	No	No
Time FE	No	No	No	Yes	Yes	Yes	Yes	No	No	No	No
\bar{R}^2	0.5774	0.7787	0.7936	0.8077	0.8453	0.8276	0.8326	0.8465	0.9014	0.9240	0.6987
$T \times N$	3487	2895	2895	2895	1570	2895	1570	97	96	96	96

Note: The table reports coefficient estimates, heteroskedasticity and autocorrelation robust (HAC) standard errors (SE) according to Arellano (1987), p -values, the adjusted R^2 (\bar{R}^2), and the number of observations ($T \times N$) for different versions of the following general regression model:

$$\sigma_{i,t}(\pi_{t+h}) = \beta_1 \sigma_{i,t}(u_{t+h}) + \beta_2 \sigma_{i,t-1}(\pi_{t+h}) + \beta_3 \text{Anchor}_{i,t,h} + \beta_4 \text{Anchor}_{i,t,h} \times \sigma_{i,t}(u_{t+h}) + \beta_5 \text{Anchor}_{i,t,h} \times \sigma_{i,t-1}(\pi_{t+h}) + \mu_i + \gamma_t + \varepsilon_{i,t}$$

where $\sigma_{i,t}(\pi_{t+h})$ represents inflation uncertainty proxied by the standard deviation of density forecasts made in period t by forecaster i for a horizon of h -years-ahead, $\sigma_{i,t}(u_{t+h})$ denotes the correspondingly computed unemployment uncertainty, $\sigma_{i,t-1}(\pi_{t+h})$ gives inflation uncertainty based on the previous quarters density forecast, and $\text{Anchor}_{i,t,h}$ is a proxy measuring the individual degree of anchoring of inflation expectations. μ_i , γ_t , and $\varepsilon_{i,t}$ characterize time-invariant forecaster-specific fixed effects, time fixed effects, and idiosyncratic errors, respectively. This general regression model has been restricted to a pooled regression model with (Lagged) and without lagged inflation expectations (Basic), to a fixed-effects (FE) model with and without time fixed effects and the anchoring measure (FE+). In addition, we have also estimated the model applying the Arellano and Bond (1991) GMM estimator (AB) and an iterative Cochrane and Orcutt (1949) estimator (CO). The same model has also been estimated for aggregated time-series data using cross-sectional means across forecasters:

$$\bar{\sigma}_t(\pi_{t+h}) = \beta_0 + \beta_1 \bar{\sigma}_t(u_{t+h}) + \beta_2 \bar{\sigma}_{t-1}(\pi_{t+h}) + \beta_3 \overline{\text{Anchor}}_{t,h} + \beta_4 \overline{\text{Anchor}}_{t,h} \times \bar{\sigma}_t(u_{t+h}) + \beta_5 \overline{\text{Anchor}}_{t,h} \times \bar{\sigma}_{t-1}(\pi_{t+h}) + \varepsilon_t.$$

Table 7. Phillips curve uncertainty regression results for $h = 5$

	Individual-level panel data							Aggregated time-series data			
	Basic	Lagged	FE	FE	FE+	AB	CO	Basic	Lagged	Anchor	CO
$\sigma_{i,t}(u_{t+h})$	0.6443	0.1860	0.2056	0.2035	0.1781	-0.0017	0.1896	0.6980	0.2555	0.2240	0.1337
SE	(0.0303)	(0.0185)	(0.0265)	(0.0251)	(0.0150)	(0.0444)	(0.0156)	(0.0533)	(0.0628)	(0.0517)	(0.0511)
p -value	[0.0000]	[0.0000]	[0.0000]	[0.0000]	[0.0000]	[0.9700]	[0.0000]	[0.0000]	[0.0001]	[0.0000]	[0.0105]
$\sigma_{i,t-1}(\pi_{t+h})$		0.7623	0.6406	0.6194	0.5855	-0.0096	0.5483		0.6528	0.6276	0.7608
SE		(0.0225)	(0.0424)	(0.0404)	(0.0201)	(0.1179)	(0.0209)		(0.0914)	(0.0789)	(0.0610)
p -value		[0.0000]	[0.0000]	[0.0000]	[0.0000]	[0.9350]	[0.0000]		[0.0000]	[0.0000]	[0.0000]
Intercept	0.1653	0.0193						0.1193	0.0348	0.0786	0.0609
SE	(0.0209)	(0.0049)						(0.0361)	(0.0226)	(0.0294)	(0.0330)
p -value	[0.0000]	[0.0001]						[0.0014]	[0.1264]	[0.0090]	[0.0686]
Anchor $_{i,t,h}$					-0.0199		-0.0179			-0.1187	-0.1051
SE					(0.0184)		(0.0191)			(0.1449)	(0.1775)
p -value					[0.2798]		[0.3484]			[0.4151]	[0.5556]
Anchor $_{i,t,h} \times \sigma_{i,t}(u_{t+h})$					0.0927		0.0864			1.0089	1.0510
SE					(0.0405)		(0.0414)			(0.3728)	(0.4147)
p -value					[0.0222]		[0.0370]			[0.0083]	[0.0132]
Anchor $_{i,t,h} \times \sigma_{i,t-1}(\pi_{t+h})$					-0.2280		-0.2383			-1.0635	-1.1236
SE					(0.0459)		(0.0469)			(0.4918)	(0.5625)
p -value					[0.0000]		[0.0000]			[0.0335]	[0.0491]

Table 7. Continued.

	Individual-level panel data							Aggregated time-series data			
	Basic	Lagged	FE	FE	FE+	AB	CO	Basic	Lagged	Anchor	CO
Forecasters FE	No	No	Yes	Yes	Yes	Yes	Yes	No	No	No	No
Time FE	No	No	No	Yes	Yes	Yes	Yes	No	No	No	No
\bar{R}^2	0.6021	0.8652	0.8746	0.8769	0.8734	0.9666	0.8723	0.8141	0.9051	0.9091	0.9476
$T \times N$	3030	2454	2454	2454	1267	2454	1267	91	88	88	88

Note: The table reports coefficient estimates, heteroskedasticity and autocorrelation robust (HAC) standard errors (SE) according to Arellano (1987), p -values, the adjusted R^2 (\bar{R}^2), and the number of observations ($T \times N$) for different versions of the following general regression model:

$$\sigma_{i,t}(\pi_{t+h}) = \beta_1 \sigma_{i,t}(u_{t+h}) + \beta_2 \sigma_{i,t-1}(\pi_{t+h}) + \beta_3 \text{Anchor}_{i,t,h} + \beta_4 \text{Anchor}_{i,t,h} \times \sigma_{i,t}(u_{t+h}) + \beta_5 \text{Anchor}_{i,t,h} \times \sigma_{i,t-1}(\pi_{t+h}) + \mu_i + \gamma_t + \varepsilon_{i,t}$$

where $\sigma_{i,t}(\pi_{t+h})$ represents inflation uncertainty proxied by the standard deviation of density forecasts made in period t by forecaster i for a horizon of h -years-ahead, $\sigma_{i,t}(u_{t+h})$ denotes the correspondingly computed unemployment uncertainty, $\sigma_{i,t-1}(\pi_{t+h})$ gives inflation uncertainty based on the previous quarters density forecast, and $\text{Anchor}_{i,t,h}$ is a proxy measuring the individual degree of anchoring of inflation expectations. μ_i , γ_t , and $\varepsilon_{i,t}$ characterize time-invariant forecaster-specific fixed effects, time-fixed effects, and idiosyncratic errors, respectively. This general regression model has been restricted to a pooled regression model with (Lagged) and without lagged inflation expectations (Basic), to a fixed-effects (FE) model with and without time-fixed effects and the anchoring measure (FE+). In addition, we have also estimated the model applying the Arellano and Bond (1991) GMM estimator (AB) and an iterative Cochrane and Orcutt (1949) estimator (CO). The same model has also been estimated for aggregated time-series data using cross-sectional means across forecasters:

$$\bar{\sigma}_t(\pi_{t+h}) = \beta_0 + \beta_1 \bar{\sigma}_t(u_{t+h}) + \beta_2 \bar{\sigma}_{t-1}(\pi_{t+h}) + \beta_3 \bar{\text{Anchor}}_{t,h} + \beta_4 \bar{\text{Anchor}}_{t,h} \times \bar{\sigma}_t(u_{t+h}) + \beta_5 \bar{\text{Anchor}}_{t,h} \times \bar{\sigma}_{t-1}(\pi_{t+h}) + \varepsilon_t.$$

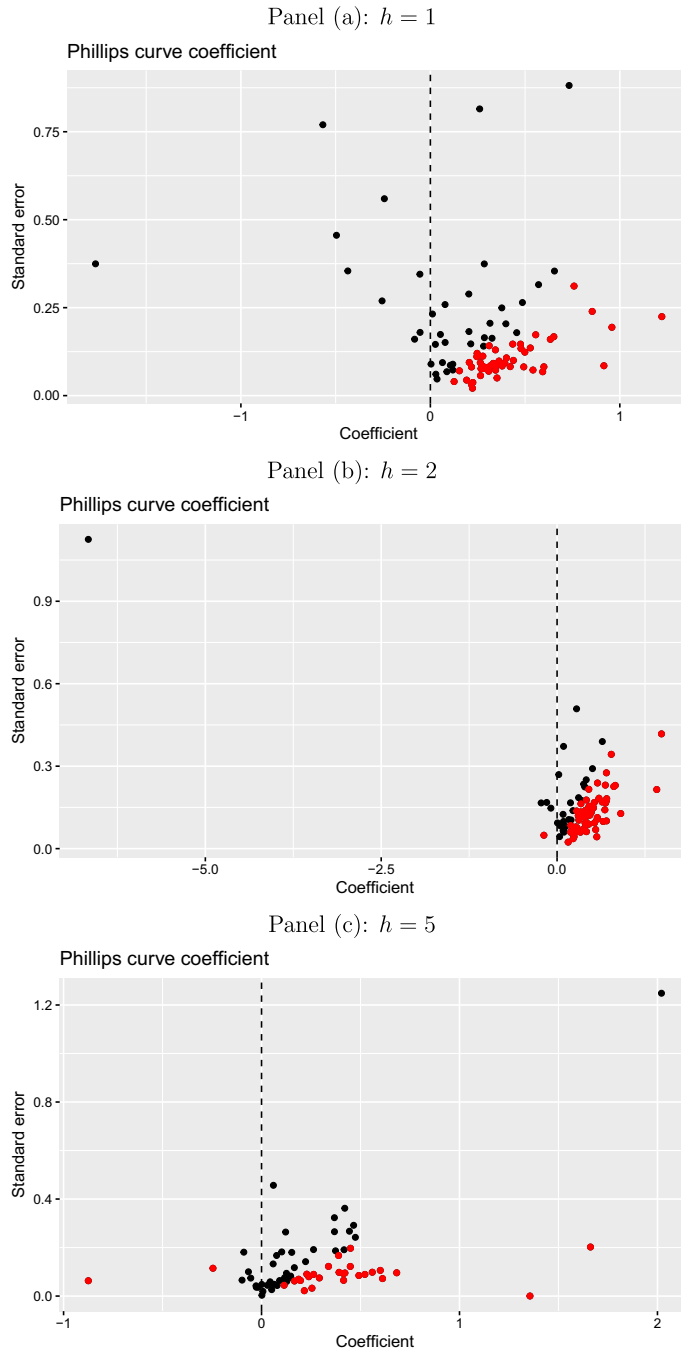


Figure 9. Individual Phillips curve uncertainty coefficients. The plots illustrate the estimated Phillips curve uncertainty coefficients and their standard errors from a regression of inflation uncertainty on unemployment uncertainty and lagged inflation uncertainty for the Euro Area on an individual forecaster level for different horizons h (one-year-ahead, two-years-ahead, and five-years-ahead) for the period from 1999Q1 to 2023Q1 taken from the ECB Survey of Professional Forecasters. The red colored points refer to coefficients, which are significantly different from zero at a 5% level.

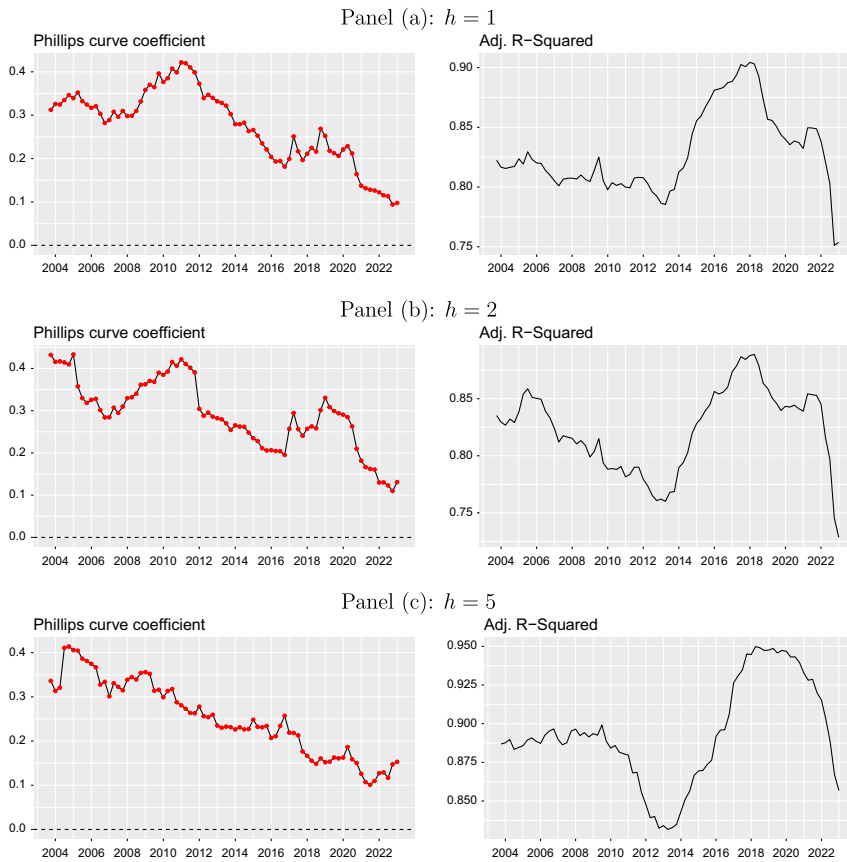


Figure 10. Time-varying Phillips curve uncertainty coefficients. The plots illustrate the Phillips curve uncertainty coefficients and corresponding adjusted R^2 s estimated by rolling-window fixed-effects regressions of inflation uncertainty on unemployment uncertainty and lagged inflation uncertainty for the Euro Area using panel data for different horizons h (one-year-ahead, two-years-ahead, and five-years-ahead) for the period from 1999Q1 to 2023Q1 taken from the ECB Survey of Professional Forecasters. The red colored points refer to coefficients, which are significantly different from zero at a 5% level. The window size is 20 quarters (= five years).

inflation expectations for the estimation of an expectations-based Phillips curve relationship while using a novel anchoring measure. Third, we assess a Phillips curve-based link between uncertainty regarding inflation and unemployment.

Our main empirical findings are also threefold. First, our results indicate that professional forecasters generally rely on the concept of the Phillips curve for lower forecast horizons (i.e., one- and two-years-ahead). However, this relationship mostly disappears for medium-run forecasts (i.e., for five-years-ahead forecasts). Second, the consideration of the anchoring measure indicates some nonlinearity in the relationship. For an average degree of anchoring, there is a small but negative Phillips curve relationship between expectations for future inflation and unemployment. For a low degree of anchoring this negative connection becomes much stronger while it disappears for a high degree of anchoring. The latter might be explained by fact that a high degree of anchoring results in stable inflation expectations close to the inflation target of the ECB of 2%, which are detached from unemployment expectations. Third, we also find that the uncertainties regarding future inflation and unemployment move together in line with the Phillips curve framework. This is particular relevant in the most recent high inflation period. On the one hand, uncertainty regarding the length and strength of the high inflation period also raises uncertainty regarding

future unemployment. On the other hand, uncertainty regarding unemployment due to a potential recession forced by higher energy prices or by a tightening of monetary policy also favors a higher uncertainty regarding future inflation.

The connection between uncertainties regarding future inflation and unemployment offers further insights for policymakers and contributes to the literature concerning uncertainty spillovers across countries and across different macro variables. In this context, the consideration of ex ante measures of uncertainty derived from density forecasts for different other macro variables offers an avenue for future research. In addition, the nonlinearity in the Phillips curve could also be studied even further by taking into account whether a de-anchoring of inflation expectations refers to inflation expectations lying above or below the inflation target of the central bank.

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Competing interest. The author declares that he has no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

Notes

1 More precisely, the inverse relationship found by Phillips (1958) was between unemployment and the change in wages, which is closely connected to inflation.

2 In the strict sense, anchored inflation expectations refer to a situation when market participants expect the future inflation rate to correspond to a reference point or anchor. It can be seen as an indication for the credibility of monetary policy, if inflation expectations are anchored at the inflation target of the central bank. This concept differs from the notion of static or myopic expectations. In the latter case, market participants do not expect any changes and expect the same inflation rate for the future as is currently observed. Static expectations assume that expectations do not take into account any new information or changes in economic conditions, while anchored expectations allow for adjustment to new information. In the present paper, we assess the degree of anchoring of inflation expectations based on different characteristics, which roughly refer to the deviation of expectations from the target of the central bank, their stability, and their probabilistic distribution.

3 According to Friedman (1968) and Phelps (1968), the relationship in general does not exist between inflation and unemployment but between the deviation of inflation from its expectations and the deviation of the unemployment rate from the so-called natural level of unemployment.

4 They refer to forecasts for the next year as medium-term forecasts. In the present study, two-years-ahead forecasts are still considered as short-run forecasts. We refer to medium-run forecasts in case of five-years-ahead forecasts.

5 See Glas (2020) for an in-depth discussion of this issue.

6 Inflation expectations can also be derived from inflation swaps, which would provide a measure based on market data. The benefit is that such a measure would be available on a much higher frequency. However, we rely on survey data as it offers the potential to derive an individual measure for each forecaster, which would not be possible based on market data.

7 Previous studies formally testing the anchoring of inflation expectations have often assessed whether inflation expectations react to new information. For instance, using data from Consensus Economics Buono and Formai (2018) find for the Euro Area that inflation expectations have been de-anchored since the global financial crisis and also after 2014. Grishchenko et al. (2019) use data from both Consensus Economics and the ECB-SPF and argue that overall inflation expectations have been better anchored in the Euro Area than in the US throughout their sample from 1999 to 2016 but also argue in favor of a mild de-anchoring. The present study does not test the (de-)anchoring of inflation expectations formally, but it uses an individual measure proxying the degree of anchoring to check for a potential nonlinearity in the expectation-based Phillips curve.

8 This overlap arises as inflation is measured as the annual percentage change of the harmonized consumer price index, but forecasts are provided on a quarterly frequency. In addition, we also use heteroskedasticity and autocorrelation robust (HAC) standard errors according to Arellano (1987).

9 This seems reasonable although Figure 4 illustrates that on average inflation expectations have been widely anchored across forecasters. However, for a few individual forecasters, we also observe a de-anchoring in some periods of time.

10 According to Coibion and Gorodnichenko (2015b), the absence of disinflation during the Great Recession can be attributed to a rise in households' inflation expectations due to a simultaneous increase in oil prices. Therefore, it would have also been reasonable to include oil prices into the regression model. In equation (11), oil prices are considered as a global factor that is captured by time-fixed effects. Another related idea would be to also include oil price expectations, which has been considered due to the fact that oil price expectations are also included in the ECB-SPF (Czudaj, 2022, 2023a). However,

they are solely available as fixed horizon forecasts for the current and the next three quarters, and therefore, unfortunately do not match the forecast horizons for inflation and unemployment forecasts exactly.

11 In some cases, the coefficients turn out to be insignificant due to relatively large standard errors, which arise as a result of a lower number of observations as some forecasters have not participated in many waves of the survey.

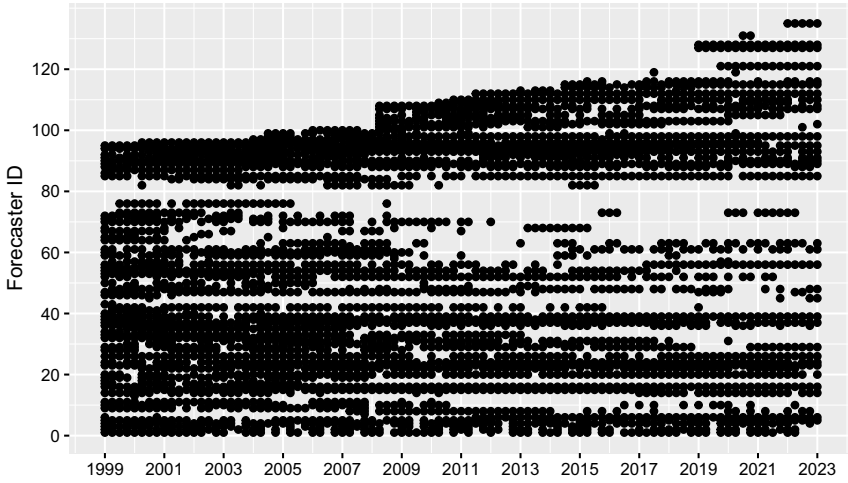
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Appendix A

Panel (a): Coverage of individual forecasters



Panel (b): Number of forecasters

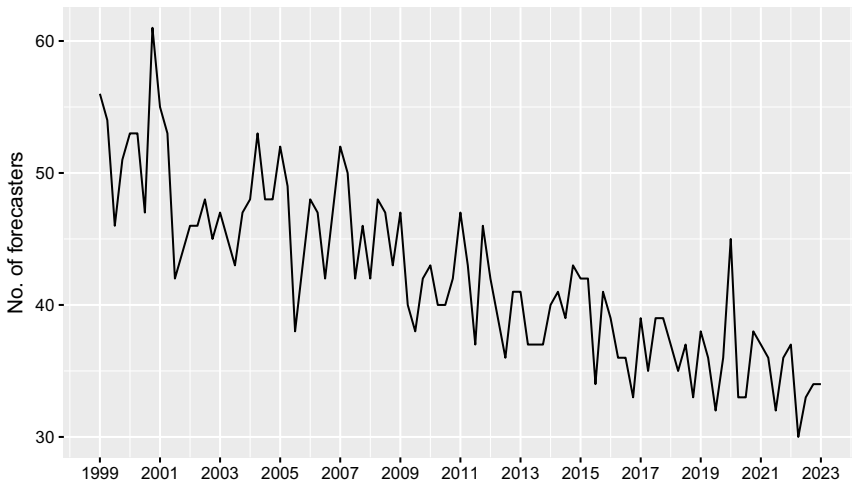


Figure A1. Coverage of forecasters. The plot shows the coverage of each individual forecaster across the different waves in the ECB Survey of Professional Forecasters (Panel (a)) and the number of participating forecasters per wave (Panel (b)) for the period from 1999Q1 to 2023Q1.

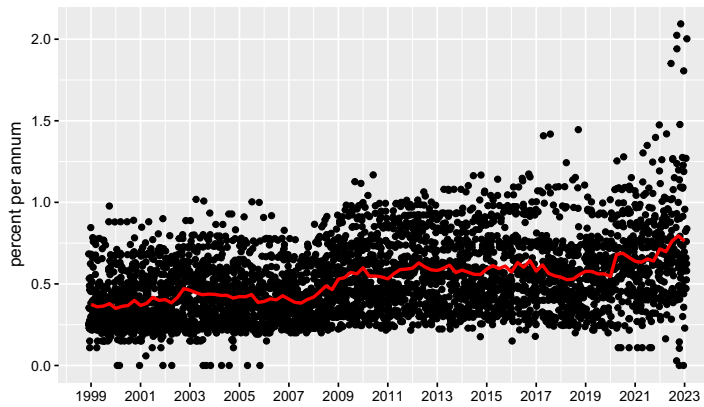
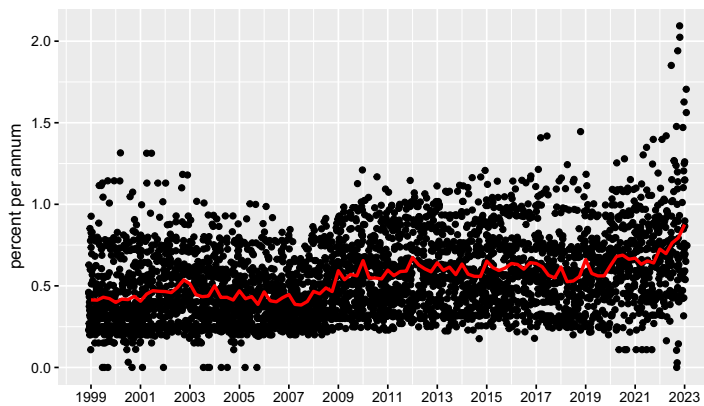
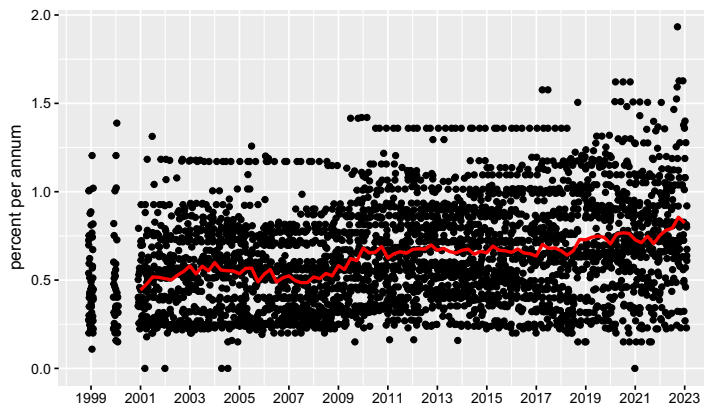
Panel (a): $h = 1$ Panel (b): $h = 2$ Panel (c): $h = 5$ 

Figure A2. Forecasters' uncertainty for inflation forecasts. The black points represent standard deviations derived from individual quarterly density forecasts for the inflation rate in the Euro Area (in percent per annum) for different horizons h (one-year-ahead, two-years-ahead, and five-years-ahead) for the period from 1999Q1 to 2023Q1 taken from the ECB Survey of Professional Forecasters. The red lines provide the corresponding cross-sectional means of standard deviations across forecasters for each point in time.

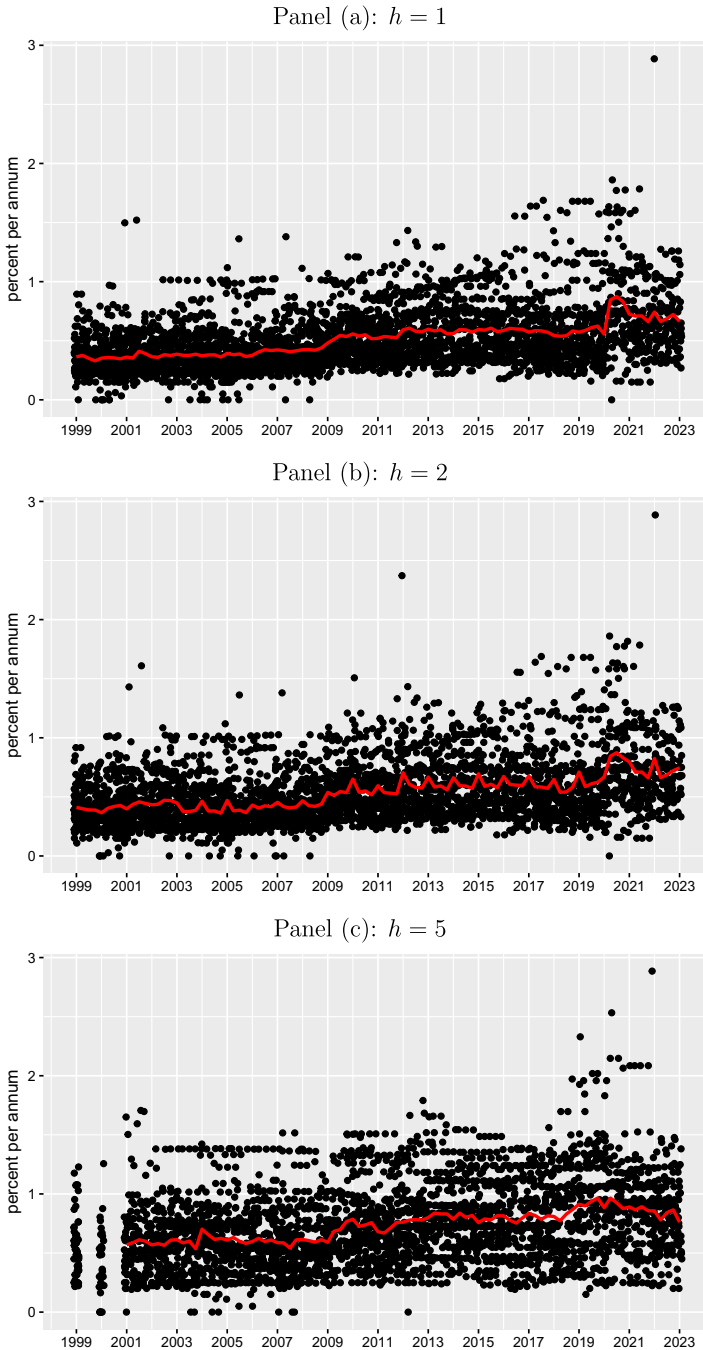


Figure A3. Forecasters' uncertainty for unemployment forecasts. The black points represent standard deviations derived from individual quarterly density forecasts for the unemployment rate in the Euro Area (in percent per annum) for different horizons h (one-year-ahead, two-years-ahead, and five-years-ahead) for the period from 1999Q1 to 2023Q1 taken from the ECB Survey of Professional Forecasters. The red lines provide the corresponding cross-sectional means of standard deviations across forecasters for each point in time.

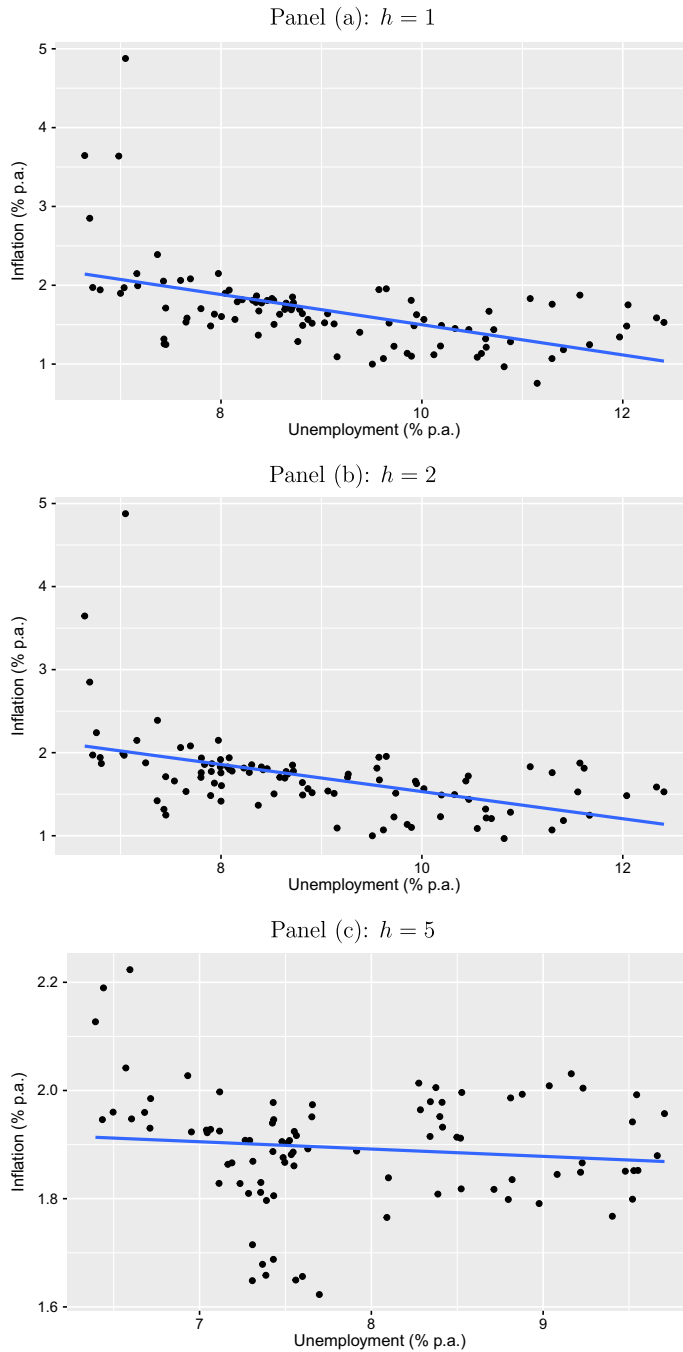


Figure A4. Phillips curve expectations relationship. The plots illustrate the relationship between inflation expectations and unemployment expectations for the Euro Area on an aggregated level for different horizons h (one-year-ahead, two-years-ahead, and five-years-ahead) for the period from 1999Q1 to 2023Q1 taken from the ECB Survey of Professional Forecasters. Each point refers to the cross-sectional mean across forecasters at each period.

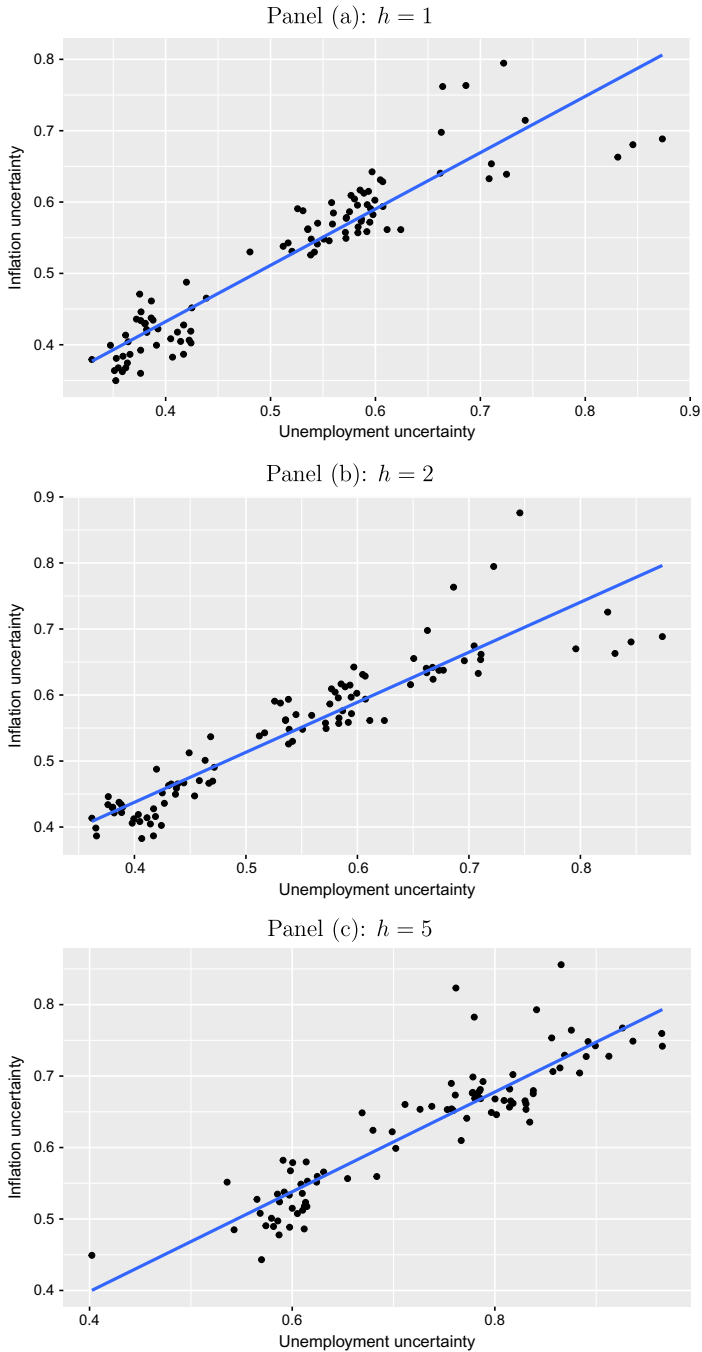


Figure A5. Phillips curve uncertainty relationship. The plots illustrate the relationship between inflation uncertainty and unemployment uncertainty for the Euro Area on an aggregated level for different horizons h (one-year-ahead, two-years-ahead, and five-years-ahead) for the period from 1999Q1 to 2023Q1 taken from the ECB Survey of Professional Forecasters. Uncertainty is proxied by the standard deviation of each forecasters density forecast. Each point refers to the cross-sectional mean across forecasters at each period.

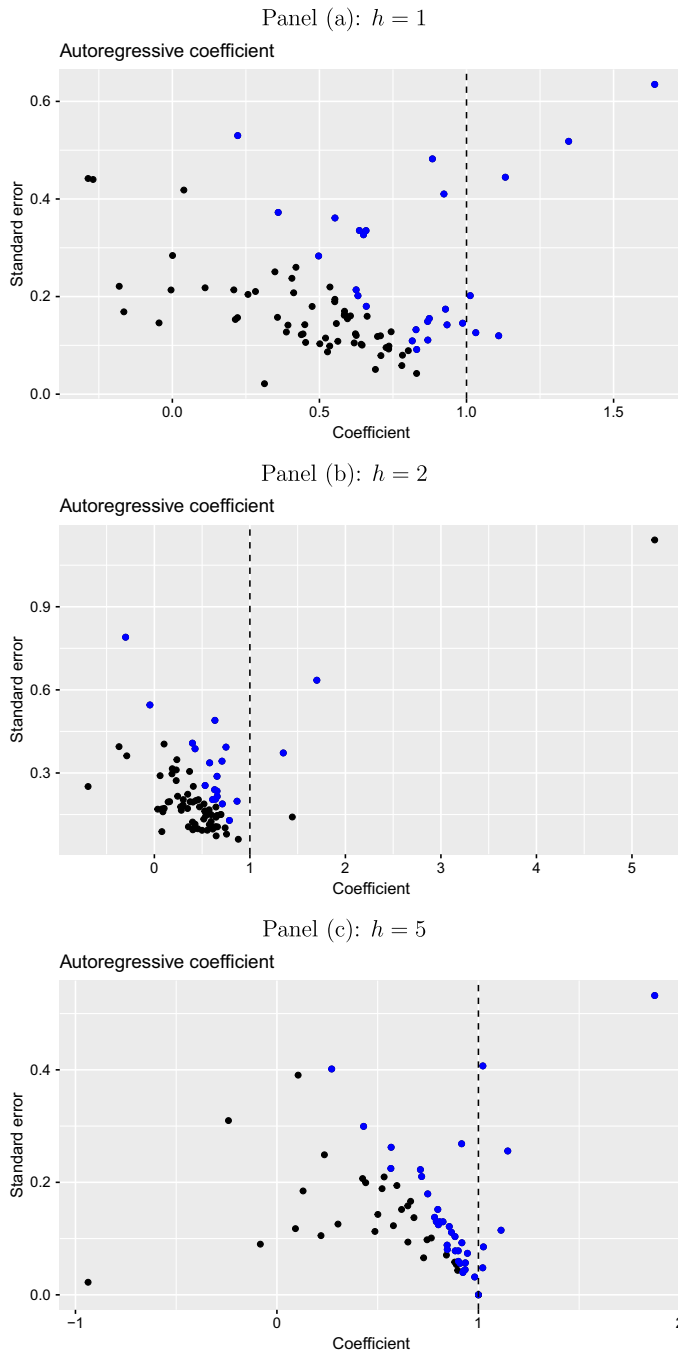


Figure A6. Individual autoregressive expectations coefficients. The plots illustrate the estimated autoregressive expectations coefficients and their standard errors from a regression of inflation expectations on unemployment expectations and lagged inflation expectations for the Euro Area on an individual forecaster level for different horizons h (one-year-ahead, two-years-ahead, and five-years-ahead) for the period from 1999Q1 to 2023Q1 taken from the ECB Survey of Professional Forecasters. The blue colored points refer to coefficients, which are not significantly different from unity at a 5% level.

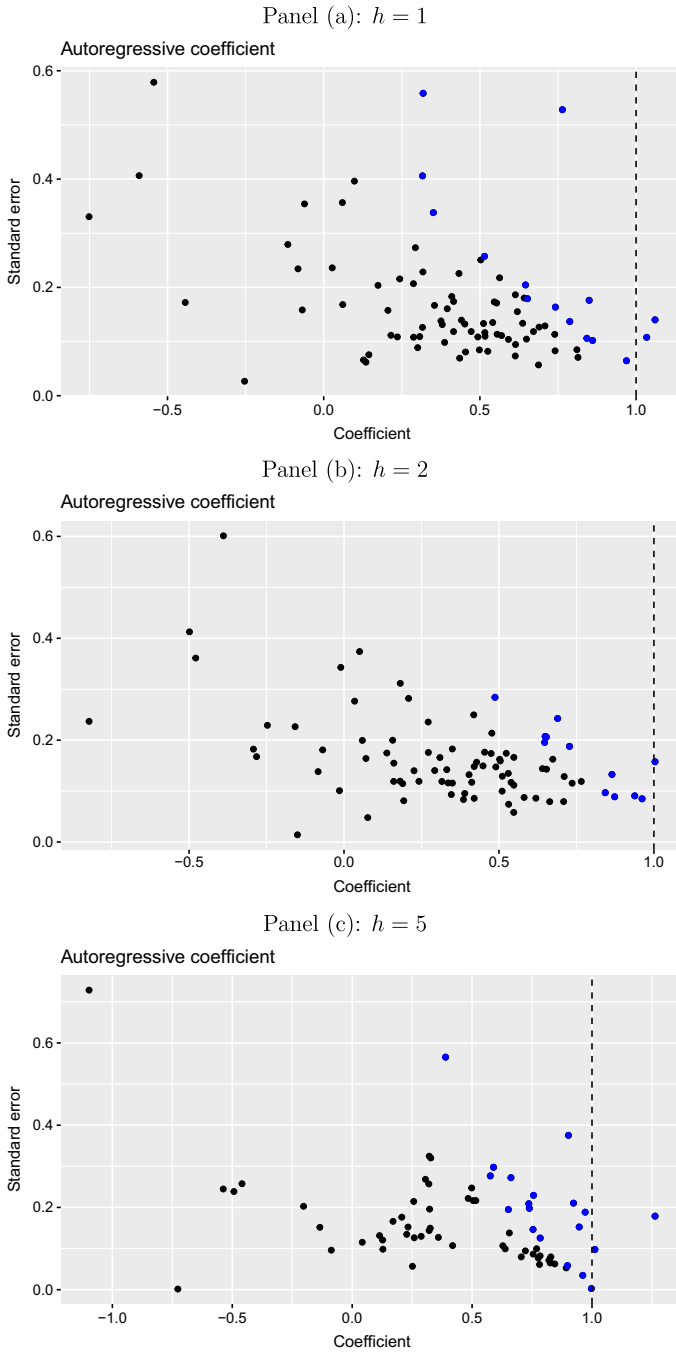


Figure A7. Individual autoregressive uncertainty coefficients. The plots illustrate the estimated autoregressive uncertainty coefficients and their standard errors from a regression of inflation uncertainty on unemployment uncertainty and lagged inflation uncertainty for the Euro Area on an individual forecaster level for different horizons h (one-year-ahead, two-years-ahead, and five-years-ahead) for the period from 1999Q1 to 2023Q1 taken from the ECB Survey of Professional Forecasters. The blue colored points refer to coefficients, which are not significantly different from unity at a 5% level.

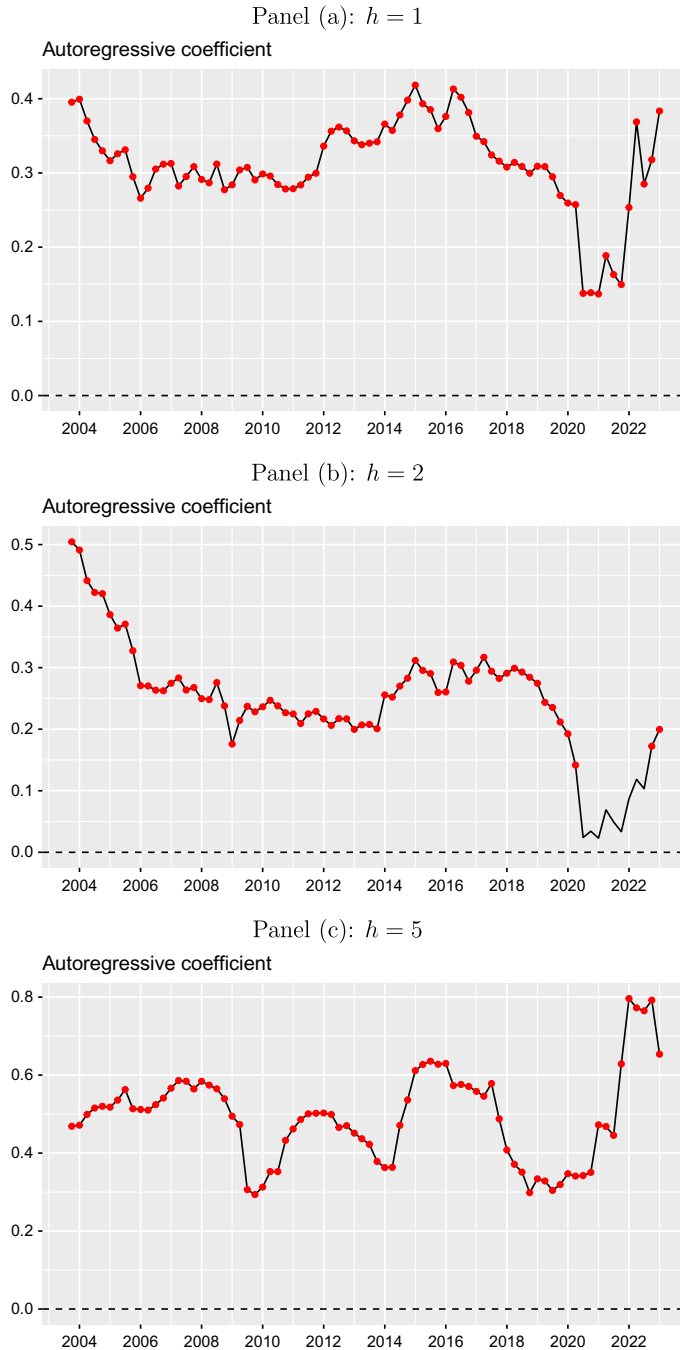


Figure A8. Time-varying autoregressive expectations coefficients. The plots illustrate the autoregressive expectations coefficients estimated by rolling-window fixed-effects regressions of inflation expectations on unemployment expectations and lagged inflation expectations for the Euro Area using panel data for different horizons h (one-year-ahead, two-years-ahead, and five-years-ahead) for the period from 1999Q1 to 2023Q1 taken from the ECB Survey of Professional Forecasters. The red colored points refer to coefficients, which are significantly different from zero at a 5% level. The window size is 20 quarters (= five years).

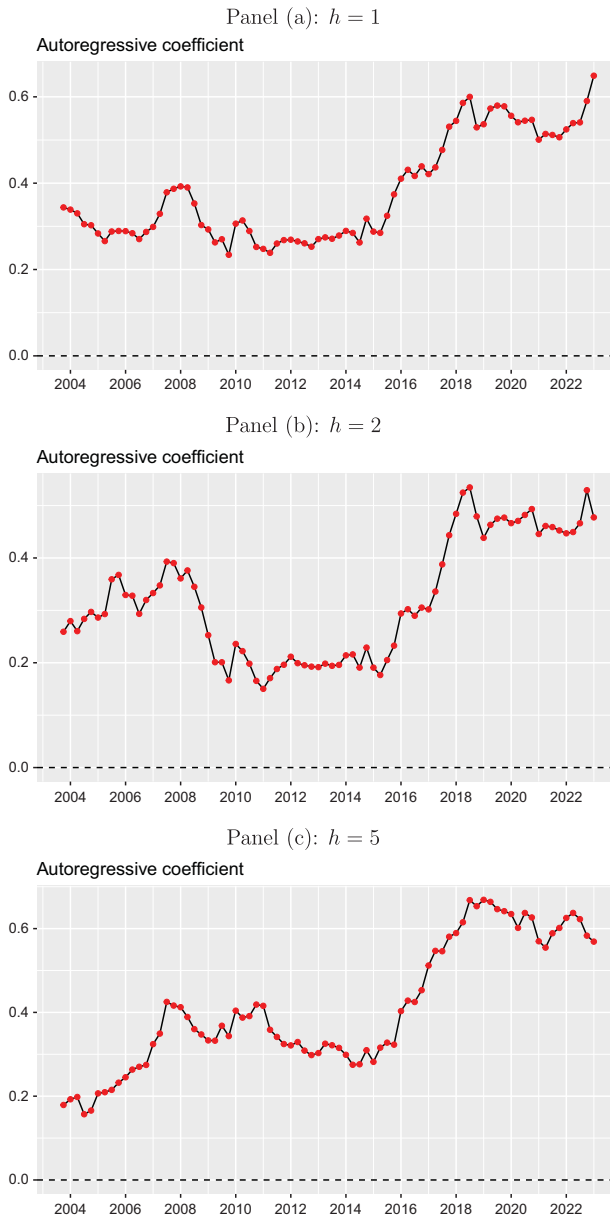


Figure A9. Time-varying autoregressive uncertainty coefficients. The plots illustrate the autoregressive uncertainty coefficients estimated by rolling-window fixed effects regressions of inflation uncertainty on unemployment uncertainty and lagged inflation uncertainty for the Euro Area using panel data for different horizons h (one-year-ahead, two-years-ahead, and five-years-ahead) for the period from 1999Q1 to 2023Q1 taken from the ECB Survey of Professional Forecasters. The red colored points refer to coefficients, which are significantly different from zero at a 5% level. The window size is 20 quarters (= five years).