

# Synthesising Computational Design Methods for a Human-Centred Design Framework

L. Urquhart <sup>1, $\boxtimes$ </sup>, A. Wodehouse <sup>1</sup> and B. Loudon <sup>2</sup>

<sup>1</sup> University of Strathclyde, United Kingdom, <sup>2</sup> Loud1Design, United Kingdom

🖂 lewis.urquhart@strath.ac.uk

#### Abstract

This paper presents models that identify two "cultures" of computational design practice. By reviewing the established culture of computational optimization efforts and contrasting it with the emerging work integrating human-factors into these optimizations, this paper argues that there are sets of key assumptions, outputs and tools that can be synthesized for a generalizable understanding of computational design. Furthermore, this synthesis facilitates the identification of key tools suited to computational design efforts seeking to integrate the complex data associated with human-factors.

Keywords: computational design methods, human-centred design, generative design

## 1. Introduction

While recent advances in computational design methods have yielded many interesting results, particularly in the field of architectural design, there remains significant limitations in terms of generalizable methods for specific human-centred design tasks (Cagan et al., 2005). Considering the two main subgroups of computational design - optimisation and generative methods - both have distinct operational outputs and applications and, as we will argue, are associated with distinct "cultures" and modes of working. Though there is significant overlap between these methods in the main, there is a lack of coherent understanding of how they can be synergised for a more focused adoption within design practice.

A major gap lies in trying to bridge the rift between human-factors - detailed extensively by studies in humancentred design (Giacomin, 2015), design semantics and design emotion (Demirbilek & Sener, 2010), and the fundamentals of optimisation and efficiency within the technical world of engineering mechanics. Computational methods have been used for some time with successful results within architectural design (see Caetano et al., 2020 for an overview) though there is less obvious output within industrial design possibly for reasons related to localised complexity and specific use-case requirements such as ergonomics.

This paper will seek to explore this issue in greater depth by examining the different cultures within the field of computational design and how they can be reformulated for a general human-centred design framework that can be useful for designers or researchers. Firstly, some background around the topic will be provided to deliver a foundation for the discussion and introduce the core concepts relating to computational design. Secondly, we will consider how the different forms of computational design can be distinguished; what the overlaps and distinctions are between the various methods along with exploring their applications. Thirdly, bringing these themes together, the discussion will shift to address how the distinctions between the computational methods introduces space in which generalizable methodological models can be developed in which computational methods can be formulated around "macro level" or "micro level" approaches that address distinct design concerns. The differentials between these models are examined next, whereby the key assumptions, outputs and tools that define

the approaches are made plain by making reference to the on-going PRIME-VR2 research project utilising these computational design methods for the development of bespoke therapy devices. Lastly, recommendations for the most effective human-centred computational design tools are explored with direct reference to available software tools.

# 2. Distinguishing forms of computational design

### 2.1. Overview and history

While "computational design" is a broad term it can be more strictly defined in relation to other terms: parametric design, generative design and algorithmic design. While there is some fluidity between these terms "computational design" can be treated as an umbrella term encompassing this range of methods. Here we will provide an overview of the different form of computational design taking *optimization* processes as our starting point.

Optimization has become one of the most widely used tools for engineers undertaking static or mechanical design work, allowing them to explore complex material and force loading relationships. Furthermore, the advent of advanced visual programming languages such as Rhino-Grasshopper and much better accessibility to additive manufacturing technologies has beckoned a new era of design optimization. Designers such as Neri Oxman, and the late Zaha Hadid have applied computational optimization methods within their respective industrial design and architectural projects (see Oxman, 2010; 2012 for instance) stimulating its overall uptake.

Computational design essentially begins with optimization operations i.e., how should material be laidout within a given space envelope? Bendsøe and Kikuchi's (1988) describe three categories of structural optimization a) sizing optimization where the basic design in terms of connectivity of elements b) shape optimization, where the optimization is engineered around a fixed topology - in the 2D case this means that a set of 2D areas or domains has fixed topology but changeable boundaries within the plane and c) topological optimization where only the domain loads and displacement constraints are specified and material may be freely assigned to each location in the design domain (2D or 3D), (see Figure 1).



Figure 1. a) Sizing optimization b) Shape optimization c) Topological optimization. From Bensoe and Sigmund (2004)

Sigmund and Maute's (2013) summaries are instructive for defining the varieties of spatial optimization tools and approaches, these are described in Table 1 below. Each method approaches the optimization in different ways though all are built around similar mathematical frameworks. Hybrid methods are becoming more widely applied such as the combination of level set and shape derivatives which can deliver more dynamic results. Many of these methods are utilised within the methods of generative design of which there is a significant overlap with optimization. Generative design applies these methods, but instead the optimization strategies are set up around novel constraints with the use of more complex form-finding algorithms. In essence, there is significant overlap between generative design and traditionally understood optimization strategies. The critical difference is that the optimizations strategies of a generative approach will usually explore a range of outcomes, with a less rigid solution space employing additional algorithmic power from shape grammar theory, neural network theory or metaheuristic genetic algorithms which mimic the processes of natural selection. The optimization tools that were principally

developed in order to explore distributions of material framed strictly within the context of engineering efficacy, spawned (somewhat unintentionally) a set of more broad-brush design tools that could be used to generate elaborate geometric designs such as the bridge formations shown in Figure 1.

#### Table 1. methods used for optimization and generative design

**Density based methods:** the process involves splitting a structure down into microscale voids and optimising material distribution (density) based on given design constraints. The method is highly developed and notable variants include the Simplified Isotropic Material with Penalization (SIMP) and Rational Approximation of Material Properties (RAMP) approaches (Bendsøe and Sigmund 1999)

**Evolutionary approaches:** finite element analysis is utilised to train optimization software in an evolutionary fashion to follow particular material distribution paths (Mattheck and Burkhardt 1990)

**Topological derivative methods:** applications of functional shape derivatives with respect to microscale changes in shape topology, such as adding small defects such as seeding points or infinitesimal holes (Sokolowski and Zochowski 1997)

**Level set methods:** the structure under optimization is implicitly represented by a moving boundary embedded in a scalar function (known as the "level set" function) of a higher dimensionality. The method is flexible in handling complex topological change (Wang et al. 2003)

**Phase field methods:** method developed as a way to represent the surface dynamics of phase transition phenomena such as solid-liquid transitions. By utilising the approach, perimeter control can be implemented enabling optimization (Bourdin and Chambolle 2003)

### 2.2. Applications and culture

Emerging work is using generative design methods for creative pursuits such as flexible wearable products and sculpture. While this is still a developing area of practice and, there are a number of interesting examples to which we can refer. Prominent designer and researcher Neri Oxman (2010; 2012) for instance has developed a set of tools utilising "digital morphogenesis" methods. These methods utilise a biological approach to form-finding, integrating biological processes of growth into algorithmic generation tools. Her prototype chaise lounge "Beast" (Figure 2a) is locally modulated for both structural support and corporeal aid through the adaption of material density, stiffness, and flexibility. It is also worth noting the overall aesthetic that is generated by generative design efforts; as well as the increased functional articulation, the aesthetic created by the fusion of organic and biological forms with modern production processes is notably striking (see Figure 2b, organic sculpture by Neri Oxman). This has been discussed directly in an article by Rain Noe (2019), writing for Core77 and has cited the creation of computationally optimized car tyres as a notable output of the culture.



Figure 2. "Beast" chaise lounge by Neri Oxman (a), generated organic sculpture by Neri Oxman (b) images from Wikimedia Commons

Other prominent areas of research are the production of prosthetics whereby generative methods have been employed to explore more interesting aesthetics that allow a user to feel more comfortable while retaining full functionality of the prosthetic. In this sense, computation is being utilised for another core human-factors dimension, that of aesthetic experience, product identity and design emotion (following Desmet & Hekkert, 2007). Some researchers have used generative design methods to develop more reliable prosthetics designs for amputees (Sansoni et al., 2015). This is still an experimental area of

medicine, and it is not yet hugely widespread, but research work in this area has expanded recently. Some interesting examples have included work from Rajput et al., (2021) who's approach aimed to create an optimised design for a lower-leg prosthetic utilising form finding optimization algorithms. The work resulted in an alternative design for a foot and calf prosthetic which has an integrated compliant mechanism to create the required localised flexibility. Similar principles have been explored by a range of researchers. Writing in a volume of Advanced Structured Materials, Hermida-Ochoa et al., (2021) have presented a strategy for creating personalised prosthetic components through anatomical scanning that are subsequently fabricated using 3D printing. Additionally, Beltrán-Fernández et al., (2021) utilised mechanical analysis to optimise the design of an orthosis for clubfoot. The analysis was able to identify key areas of stress and strain in the design and hence optimize the material distribution during the 3D printing fabrication process. A strategy similar to this is employed by Li and Tanaka (2018) who use Rhino-Grasshopper programming to produce bespoke orthotics designed to immobilise fractures in hands. The paper illustrates a proof-of-concept for using a Voronoi optimization approach for the creation of bespoke structures attuned around user anatomy.

We can see that the different research efforts have utilised a different array of computational tools with many relying on more traditionally understood optimization methods as opposed to methods that incorporate other human-factors. While this is perhaps indicative of the particular methodological constraints that computational tools present, it is a clear knowledge gap in which more study and analysis could prove valuable for research and practical innovation.

The key factor missing in these discussions is how this could be translated into a generalizable model for human-factors led computational design. While the overarching goals of the various projects are different, they are all interested in the interfacing between form and human ergonomics with the caveat that advanced additive manufacturing methods facilitate the production of their complex and ornate parts. Though they also use different methods to produce the products, there are clear areas in which an overarching approach can be defined.

The key question is how the panoply of computational design methods can be reined-in to focus their output on questions of human-factors in design. We have seen how optimization tools can be incredibly powerful in determining a broad sweep of functional design solutions usually with respect to material distribution. Additionally, we have also explored examples that use form building algorithms to create art in the form of sculpture through generative design methods. The intersection of these distinct cultures has been explored in emerging areas of research that seek to focus on factors such as ergonomics or the creation of distinct aesthetics. Conceptually, this is an evolution from the default culture of material-space optimizations and opens new space in which creative design work can operate. This sets the scene for the next section which will continue to evolve these ideas and establish a framework for human-centred computational design.

### 3. Towards a framework for human-centred computational design

When developing a variant framework to the computational design methods we have been examining, it is important to consider how such a process may differ to those more traditionally understood design methodologies and philosophies. Many well-known and widely used methodologies such as the British Design Council's "double diamond", Ulrich and Eppinger's methods (1994) or Pugh's earlier matrices-based methods (1990) all have a variety of benefits and draw backs for different design contexts. The double diamond for instance is high-level and generic providing the design team lots of freedoms within the approach. By contrast, Pugh's methodology is much more prescriptive and focuses the design work by applying sets of constraints around various elements such as materials and costs.

Computational design methods use the powers of algorithmic or mathematical logic to explore "design space". While this space is intentionally configured through the definition of constraints, many aspects of designer agency are removed in favour of a computational method that systematically interrogates the possible geometric formations that fit to the predefined constraints (Bensoe and Sigmund, 2004). In this respect, the process is fundamentally different to the default hylomorphic framing of form-emergence (see Ainsworth, 2016 for a summary). When trying then to define how to understand the overall processes of computational design for practical usage it is useful to subdivide the activities. By drawing an equivalence to the broad design space constraints set out during the first stages of an

optimization; we can term this the "macro" level of the process where the broad architecture of the design is set out. Following this, a "micro" level of the process somewhat equivalent to design detailing whereby the geometry is optimized around a set of ad hoc constraints (e.g., ergonomic requirements) is carried out. This macro-micro bilateral can function as a useful equivalence for the "two cultures" observation discussed earlier - where traditional optimization methods are more interested in the output at the macro-scale i.e., large structural changes that could say, save large amounts of material, where more modern methods integrating human-factors may require detailing at the micro-scale where the nuances of ergonomics and aesthetic experiences are established. A macro level approach may be best suited to the design issue at hand and this work is not explicitly arguing for always using micro level analysis may need to be initiated for complex human factors design problems to be fully solved as they will often lie beyond the bounds of the more linear problems of material distribution.

Shown below in Figure 3 is the methodological model that has been developed in which we will explore further and use as the foundation for exploring the differentials between the macro and micro levels of computational design thinking. This is the high-level version of the model but it will be used as a starting point for establishing our synthesis between the technical outputs of computational design and the human-factors outputs which we have examined in the previous sections. Narratively, the model follows the rough structure of a traditionally understood design methodology, starting with specification and ideation and ending in a product realisation allowing the reader to grasp the critical points in which computational methods are typically applied. Shown is how computational design thinking intersects with the traditional format for design work. The critical differences are seen as the solutions are being developed and the distinction between the macro solutions and the micro solutions which include a looping structure that integrates knowledge acquired from human-factors analysis and testing that is then fed back into the computational coding definitions. As a general rule, a micro level approach will always include a macro level phase before full realisation, but a macro level analysis may not always lead to a micro level output.





We can start with a more detailed overview of the methodology where the underlying concepts can be described in relation to computational design thinking:

- 1. **Specification/ideation stage:** The core requirements for the product are set out within the specifications which run in conjunction to initial ideation. This is perhaps the most well-aligned element to the traditional design methodologies.
- 2. **Conceptualisation stage:** The pre-computational phase in which the functionality of the concepts is explored in the abstract and the design space constraints are more properly established.
- 3. **Embodiment stage:** Computation stage in which the abstract understanding of form and functionality explored in the first two stages become refined and are built into an algorithmic

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definition. The algorithmic definition has a macro stage optimising the larger structural form features and a micro stage generating the detailed form features and in-built functionality.

4. **Realisation stage:** *Finalisation of design after computational design explorations. The design depending on the macro or micro strategy taken will be fully optimised around the specified constrains and any inputted data.* 

As shown the macro and micro computational activities can be more effectively deployed at certain design stages and may be deployed iteratively with the aim of achieving a unique design solution. The methods articulate with other practical design activities such as prototyping but the key computational activity is the coding of algorithms that facilitate the generation of the design solutions. Next, we can explore how the differentials and synergies between the macro and micro level strategies can be established in more detail.

### 3.1. Establishing a synthesis

While this paper has sought to argue that there are two distinct "cultures" of computational design effort, establishing a synthesis between these cultures is vital for understanding how computational approaches can be better presented as part of a more generalizable framework for human-centred design based innovation and indeed advancing efforts in traditional topology optimization practices.

To think further about the differentiations and possible synergies between a macro level approach with a more nuanced micro level approach, areas of the model shown in Figure 3 before can be explored in greater detail. To do this, some of the overarching process narrative has been removed and the critical steps leading to design solutions have been focused on. Critically, three important elements will be focused on that allow for the tracking of the utility of each approach for each context; *assumptions, outputs and tools*. These three elements facilitate both an analysis of function in terms of what the approaches are good for and what tools can be wielded to get particular outcomes, and furthermore cultural concerns around the assumptions required to initiate the computational design process itself - what the designer or engineer imagines the product creation process and the end product to be. Starting with macro level computational approaches, Figure 4 presents and analysis in terms of assumptions, outputs and tools.





This diagram illustrates how the macro level approaches are linear in their methodological process. Once the design constraints have been adequately defined, the algorithmic optimization packages available in the commercially available software listed within the available tools section can be applied. The critical assumptions for these kinds of approaches partition the design solution from direct human interaction at a subjective psycho-social level and instead focus on material optimization (e.g. space or density distributions) as the critical output. Many of the packages cited as key tools allow the user to define forces acting within the space envelope and define material specifications allowing the structure to be optimized with respect to a definite field of forces. This can now be compared to the micro level approaches which operationalise a range of different factors and allow for the creation of explicitly human-centred products.

Figure 5 maps the methodological model for micro level computation efforts. As shown, the process is much less linear and involves looped exchanges of bespoke data that has been established from empirical human factors analysis - this could be emotional responses to certain form elements (see Bar & Neta, 2006) or ergonomics and usability data derived from physical testing or data capture such as 3D scanning or motion capturing (Paoli et al, 2020 reviewed several relevant technologies). Crucially, this block of bespoke data fundamentally changes the "culture" of the operation as the critical assumption is that subjective psycho-social factors will play a role in how the end product will interact with the human world; the design outcome is not partitioned from direct human influence. The key outputs in this regard are bespoke forms that might be tailored around a specific features like anthropometric measurements or predictable emotive responses such as the negative associations most humans place on observed angularity (Bertamini et al., 2016). Notably, the tools cited here are more distinct, making reference to several Grasshopper plug-ins which facilitate these kinds of unique design explorations. The flexibility of Grasshopper makes it an excellent candidate tool for designers wanting to explore the integration of human-factors data into a computational design exploration.



Figure 5. Analysis of micro level computational design methods in terms of assumptions outputs and tools

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So how can this be used by design practitioners? The models we have set out in this paper are not directly prescriptive but does invite further expansion by allowing for the meaningful distillation of the synergies and differences between the two "cultures" of computational design. These can now be outlined but drawing comparisons between the models presented at Figures 4 and 5.

1) Key assumption synergies: the creation of a "unique" form for the design solution. For the macro level this is a by-product of the specific material and weight constraints, the micro level may be specifically guided by the articulations between materials, functionalities and human interaction concerns. 2) Key output synergies: material savings and functionality optimization with a given space envelope. Both macro level and micro level approaches are engaged with the problem of material-space arrangements and how best to optimize with respect to particular constraints to achieve the desired functionality. While different assumptions are at play in the processes in general, these particular outputs align closely. 3) Rhino-Grasshopper visual programming language. The programming language facilitates a wide-array of analysis and design generation tools and allows for both macro and micro level computation efforts. In terms of human-centred design and human factors analytics, Grasshopper is an excellent tool and has been explored within many contexts to create interesting design generation workflows that integrate human-factors data (Abualigah & Diabat, 2020). Furthermore, for a human-factors and computation integration focus, Grasshopper presents a very promising architecture in which to define a generalizable framework for approaching these design problems.

We can explore PRIME-VR2's research into bespoke therapy devices (see https://prime-vr2.eu/) to illustrate how the macro and micro level can be used to explore and generate different design outcomes. Firstly, Figure 6 illustrates how a macro level analysis can inform the design of componentry for the "spine" component of the bespoke device. Using Abaqus FEA, the spine can be analysed with respect to likely motions and input forces allowing for the optimization of the overall structure for most effective mechanical performance.



Figure 6. Macro level analysis for optimization of spine component

Micro level strategies integrating ergonomic data and human needs intelligence has also been used for PRIME-VR2. Shown below (Figure 7) is an excerpt from the Grasshopper algorithmic build that generates the wrist strap component that conforms around the user's wrist. The key distinction here is that the form is *generated* around a discrete set of constraints that are not limited to force inputs and material distribution as in Figure 7. Intelligence around ergonomics, device functionality and aesthetics has also been introduced to achieve the results.



Figure 7. Micro level methods for generation of wrist strap component

## 4. Conclusions

This paper has been theoretical in nature and has proposed a set of arguments that differentiate two "cultures" of computational design efforts. One culture - the "macro"- focuses on technical engineering problems of material and space optimization where a definite outcome is desirable based on a set of defined constraints. By contrast, the "micro" culture focuses on the integration of complex human interaction problems and may also explore the subjective realms of psychological experience as an input to the algorithmic solvers.

These arguments were developed by reviewing a number of examples within the research literature and also by looking at prominent examples within design practice that have integrated complex human-factors data like anthropometrics for innovative generative solutions. A number of models were presented that set out this differentiation and identified the macro cultures with a more linear approach that is less iterative in algorithmic solving due to the design space being smaller. The micro level culture that is required for human-centred computational design presents different challenges and will often utilise completely bespoke data and physical testing to build in the design constraints and improve the solutions iteratively. The intrinsic complexity and subjectivity of human-factors data means that the process is somewhat less linear than the traditional material distribution problems.

By comparing these models and exploring a set of practical examples from the PRIME-VR2 research project, several synergies between the approaches were identified where alignments between key assumptions, outputs and tools were clear. Notably, Rhino-Grasshopper was identified as a critical tool for a human-centred design focus due to its flexibility in the integration of many kinds of data types. This synthesis furthermore allows for a better theoretical understanding of the different computational design cultures and may be applied by researchers and practitioners to more effectively steer their thinking on computational design problems.

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