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ASTEROID COMPOSITIONAL TYPES AND THEIR DISTRIBUTIONS

B. ZELLNER and E. BOWELL

A sample of 359 minor planets with available colorimetric, spectrophotometric, thermal-radiometric, and/or polarimetric data are classified into broadly defined compositional types \underline{C} (carbonaceous), \underline{S} (silicaceous), \underline{M} (metal-rich), \underline{E} (metal-free; enstatite?), \underline{O} (ordinary-chondritic?), \underline{T} (Trojan; unidentified composition), and \underline{U} (unclassifiable; none of the above).

The small asteroids in Mars- or earth-crossing orbits are almost invariably of type S or O. For the main belt between 2.2 and 3.5 AU., distributions of the various types over diameter and orbital parameters are derived with corrections for observational selection bias. For 560 main-belt asteroids with diameters >50 km, 76% are of type C, 16% of type S, 5% M, and 3% of other types. The S objects become progressively less common with distance. The shapes of the diameter-frequency relations for primitive (C) and evolved (S + M) types are statistically indistinguishable, both showing a change of slope at 160-km diameter.

While large asteroids avoid the Kirkwood gaps more strongly than small ones, we find no significant gap-related anomalies in the relative frequencies of compositional types. Thus most of the observational basis for models in which primitive and evolved asteroids respond differently to collisional evolution has been removed.

INTRODUCTION

In recent years several observational techniques have been applied to large numbers of asteroids for remote sensing of their surface properties. Infrared radiometry at thermal wavelengths measures the diameter and, together with the visual magnitude, the geometric albedo (Hansen 1976; Morrison and Chapman 1976; Morrison 1977; and reviews in this volume by D. Morrison and O. Hansen). Optical polarimetry gives indications of surface structure and albedo and hence also permits the computation of diameters (Zellner and Gradie 1976a; A. Dollfus in this volume). Narrow-band spectrophotometry at visible and near-infrared wavelengths gives the most direct information on surface mineralogy (Johnson and Fanale 1973; McCord and Chapman 1975a,b; McCord and Gaffey in this volume). Broad-band or UBV photometry (Zellner et al. 1975, 1976; Bowell 1977) generally permits recognition of the major types identified by more sophisticated techniques and can be pushed to substantially fainter magnitude limits.

Diversity is a fundamental characteristic of the asteroid population.
While individual asteroids seem to have remarkably uniform surfaces, hardly any

two well-observed objects are optically indistinguishable, and as many as 34 distinct types of reflection spectra have been identified by McCord and Chapman. Nevertheless, five or six broad but distinct classes appear in the results from all compositionally sensitive techniques. The prevalence of the \underline{S} ("silicaceous") and \underline{C} ("carbonaceous") types, together accounting for more than 90% of the asteroid population, was first recognized by Chapman on the basis of colors and by Zellner on the basis of polarimetric parameters and is beautifully demonstrated in the albedo histogram by Morrison in this volume.

The distinctness of the major groups throughout the asteroid population as seen by independent techniques strongly suggests to us that the groupings have a high degree of physical significance as well as practical utility. The broad classification scheme permits the examination of distributions over diameter, heliocentric distance, etc. in ways not statistically possible for minutely specified compositional species. An asteroid observed by only one technique, such as UBV photometry, can usually be classified with confidence or else recognized as an unusual object. Finally, let us emphasize that these groups are based entirely on observational parameters, and their validity is not compromised if interpretations in terms of meteoritic analogues, etc. must be modified.

Our purpose in this paper is to classify as large a sample of asteroids as currently available observations permit and to derive distributions of the various types over diameter and orbital parameters with correction for observational selection biases. Our preliminary results are examined in more detail by Bowell et al. (1977). Such an analysis was first attempted by Chapman et al. (1975), who concluded that: (1) most asteroids can be classified \underline{C} or \underline{S} , with a sprinkling of the other types; (2) the frequency of type \underline{S} with respect to type \underline{C} generally decreases with distance outward through the main belt; (3) \underline{M} asteroids tend to fall near the Kirkwood gaps, and \underline{C} objects to avoid the gaps widely; and (4) different diameter-frequency relations, suggestive of different collisional evolution histories, are found for the \underline{C} and \underline{S} populations. Now, with a sample of asteroids more than three times larger than that available to Chapman et al. we can confirm the first two statements. The third appears to be false, however; and the fourth must be substantially modified.

TYPES AND DIAMETERS

The major types can be displayed in a variety of ways using spectroscopic, radiometric, or polarimetric data. We are limited by space requirements to Figure 1, which separates out the groups as well as any two-dimensional plot.

The moderate albedos and reddish curving spectra of the S asteroids are attributable to a mixture of free metal and transition-metal ions in a silicate lattice (Gaffey 1974; McCord and Gaffey 1974). Near-infrared absorption bands characteristic of pyroxene and/or olivine silicates are often but not invariably present. Although good matches with laboratory reflection spectra have proven difficult, the S asteroids will no doubt be ultimately identified with various stony-iron meteorites or iron-rich ordinary chondrites.

The low albedos and rather flat spectra of the \underline{C} asteroids are almost certainly due to an admixture of carbon, while a characteristic drop-off in the ultraviolet implies the presence of ferrosilicates as well. These objects are probably the parent bodies of at least some carbonaceous chondrites.

A third major type is provided by the M ("metallic") objects with albedos similar to those of the S group but flatter, featureless reflection spectra characteristic of free metal as in the nickel-iron meteorites and enstatite chondrites. A class \underline{O} , as yet poorly defined, has higher albedos (up to 0.26) and spectra similar to certain metal-poor ordinary chondrites. Three \underline{E} objects have been identified with quite high albedos (≥ 0.3) and colorless spectra strongly suggestive of the metal-free enstatite achondrites (Zellner 1975; Morrison et al. 1977). Observations of several Trojans, here denoted as class

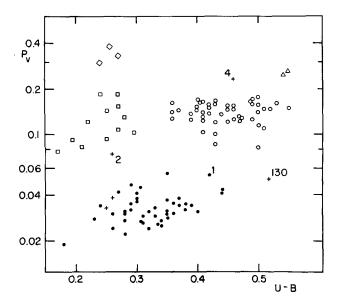


FIGURE 1. Albedo versus ultraviolet minus blue color index for 43 C asteroids (filled circles), 47 of type S (open circles), tvelve of type M (open boxes), three of type E (open diamonds), two of type O (open triangles), and five of other types (+). Geometric albedos are on the radiometric scale, as listed by D. Morrison in this volume.

T, have revealed quite low albedos and unique spectra not corresponding to any identified meteorite or mineral assemblage.

A small fraction of the observed asteroids belongs to none of the above types and is designated by the symbol \underline{U} ("unclassifiable"). They are either unique or belong to types yet to be described. The \underline{U} asteroids include some of the very largest objects; 4 Vesta has a unique basaltic surface (McCord et al. 1970; Larson and Fink 1975), while 2 Pallas has a rare combination of optical properties and 1 Ceres itself is a rather unusual C asteroid.

There is no observational evidence that any asteroid has a surface of variegated albedo or composition. Recent polarization observations of 433 Eros (Zellner and Gradie 1976b) showed the albedo to be constant over rotation and aspect to one part in forty, and narrow- and broad-band colors did not vary measurably with rotation (e.g., Pieters et al. 1976; Millis et al. 1976).

Table I gives compositional types chosen by us for 336 main-belt asteroids, twelve Mars-crossers, two Hildas, and nine Trojans. The data base consists of observational parameters in the TRIAD computer file $^{\rm I}$ and further preliminary results by several observers. By rough count we have 100 asteroids with polarimetric data, 126 with reflection spectra, 165 with radiometric diameters, and 300 with UBV colors.

The type assignments range in quality from quite secure to highly provisional. We used classification criteria very similar to, but slightly looser than, those tabulated by Bowell et al. (1977). That is, we did not exclude an

The <u>Tucson Revised Index of Asteroid Data</u> contains all reliable physical information for minor planets and is maintained at the University of Arizona by B. Zellner. Contributors and their areas of responsibility are: D. Bender, orbital elements; E. Bowell, UBV colors; C. Chapman, spectrophotometric parameters; T. Gehrels, magnitudes and lightcurve parameters; T. McCord, digital reflection spectra; D. Morrison, radiometric parameters; and B. Zellner, polarimetric parameters.

Table I. Compositional Types and Diameters

No.	Туре	D1 am	No.	Туре	D1 am	No.	Туре	Diam	No.	Туре	Diam	No.	Туре	Diam	No.	Туре	D1 am
1 2 3 4 5	ง ร บ ร	1003 608 247 538 117	66 67 68 69 70	S S U C	26 62 126 151	145 146 148 149 150	C	176 135 106 16 109	293 295 306 308 313	င s S U	59 27 43 138	478 481 497 498 505	8 C C C	75 102 31 71 91	801 804 825 830 853	C S S C	34 162 12 43 29
6 7 8 9 10	\$ \$ \$ C	201 209 151 151 450	71 72 76 77 78	S C C S C	115 96 144 65 140	151 152 153 154 156	s c c	41 64 164 191 104	321 324 326 335 336	C C U M	52 246 82 34	508 509 510 511 516	C M C M	126 60 34 323 63	863 887 888 911 924	0 S S T C	35 4.5 36 155 78
11 12 13 14 15	\$ \$ \$ \$	150 126 224 158 272	79 80 81 82 83	S U C S C	76 83 112 65	159 162 163 164 166	C C C C U	140 95 26 102	337 338 342 344 345	8 M C C	55 60 53 145 89	524 532 537 540 545	c \$ c s	61 130 103 13 115	932 946 963 969 976	C C S U M	56 47 9.2 43
16 17 18 19 20	M S C S	250 109 150 215 131	84 85 86 87 88	C C M C	90 1 47 108 119 210	170 172 173 176 177	U S C C C	67 142 119 68	349 350 351 354 356	0 0 8 S C	144 123 45 153 150	550 554 558 560 563	S M C S	41 103 64 43 51	977 1001 1011 1036 1043	C M S S	68 38 7.2 35
21 22 23 24 25	M S C S	115 177 111 211 72	89 90 91 92 93	\$ C C	155 124 104 244 168	178 179 181 182 183	\$ \$ \$ \$	39 72 82 48 33	357 360 362 363 364	с с с s	105 130 90 95 32	569 579 584 588 591	С S T И	54 26 55 110 23	1048 1052 1058 1087 1140	\$ \$ C	20 12 13 58 26
26 27 28 29 30	\$ \$ \$ \$	93 108 123 195 91	94 95 97 100 102	C C M S C	188 167 95 80 85	185 186 189 192 194	C M S C	169 49 41 94 191	365 367 370 372 377	C S I I	99 20 53	596 602 617 618 623	C C C C	134 137 148 126 35	1143 1171 1172 1173 1178	С Т	124 65 131 88 24
31 32 34 36 37	C S C C S	334 93 114 96 95	103 104 105 106 107	s c c c	90 122 125 166 211	195 196 200 203 204	c S c c S	92 161 123 92 50	381 384 386 387 388	C C S M	126 38 191 112 66	624 631 639 654 658	T S S C S	182 49 72 116 24	1212 1263 1266 1268 1287	I C C	69 24 79 91 19
39 40 41 42 43	\$ C \$	163 100 204 97 82	108 109 110 111 113	s c c s	61 75 120 143 47	206 208 209 210 211	C S M C C	101 42 67 77 166	389 393 395 397 402	<i>S C S S</i>	81 129 49 50 46	660 661 674 675 676	s s s c	40 36 102 74 71	1291 1314 1329 1362 1401	S	26 8.5 24 58 10
44 45 46 47 48	C C C	82 226 133 135 248	114 115 116 117 119	c s s c s	122 93 86 137 57	213 214 216 219 221	C M M S U	90 44 128 37	404 409 410 415 416	C C C S	86 211 1 34 75 76	679 680 694 702 704	S I C C U	73 88 205 350	1437 1500 1504 1547 1566	S S U	126 7.0 13
49 51 52 53 54	С С С С	176 151 289 97 180	120 122 123 124 125	C S S	173 139 47 67 58	224 230 236 238 241	M S C C	71 121 <i>65</i> 1 54 <i>179</i>	426 432 433 434 435	C S S E	104 55 23 11	705 714 735 737 739	r S C S C	16 68 54 105	1567 1580 1583 1620 1627	C T S	72 6 109 3.4 7.0
55 56 57 58 60	M C S C	75 146 109 99 51	126 129 130 131 135	<i>S</i> M U <i>M</i> M	40 115 173 35 78	247 250 258 264 268	C M S S C	142 107 65 63 106	441 444 446 451 454	M C C C C	66 141 40 276 85	744 747 755 776 778	บ C M C บ	205 37 147	1636 1681 1685 1694 1707	3 U C	10 14 3.2 17 8.8
61 62 63 64 65	S C S E C	87 105 91 56 309	137 139 140 141 144	00000	143 163 103 133 130	270 275 276 281 284	\$ C C S C	51 94 107 13 53	455 462 471 472 476	C S S C	93 37 143 45 106	779 782 785 790 796	C S M C I	108 15 49 176	1864 6004 6004 76A4	N S	2.2 15

Notes to Table I. Compositional types are italicized where observations by one technique only are available. Italicized diameters refer to objects for which albedos have not been derived from radiometric or polarimetric observations but only assumed according to the type. (See text). The last three entries signify unnumbered objects 1960 OA, 1960 UA, and 1976 AA.

object from a likely class if some measured parameter fell just outside the nominal class boundaries.

We use the class designation \underline{I} (indeterminate) in a few cases where the only available parameters fall in ambiguous color or albedo domains and no real choice is possible. The designation \underline{U} , by contrast, is used for objects known to fall outside the domains of all recognized (\underline{C} , \underline{S} , \underline{M} , \underline{E} , \underline{O} , \underline{T}) classes in one or more parameters.

Diameters in Table I are taken from Morrison (this volume), where radiometric, polarimetric, or combined results of weight 2 or higher are available. In other cases the diameters are computed from

$$2 \log (D/2) = 5.642 - 0.4V(1,0) - \log p_v$$

Absolute visual magnitudes V(1,0) were computed from the blue magnitudes listed by Gehrels and Gehrels (1977) and B-V colors either known or estimated according to the type. For the geometric albedo p_V , we used adopted values of 0.14 for type \underline{S} , 0.12 for type \underline{M} , 0.037 for type \underline{C} , and 0.23 for type \underline{O} . As demonstrated by Morrison, the mean albedo is probably more reliable in a particular case than a low-weight polarimetric or radiometric value.

We emphasize that the diameters used here are all based on the radiometric albedo scale, which gives somewhat lower albedos and larger dimensions than the polarimetric calibration. We ourselves have confidence in the polarimetric values, at least for albedos greater than 0.06, but we use the radiometric scale for convenience and ease of comparison with other results. The following analysis depends rather critically on the choice of relative albedos, but only weakly on the absolute values.

THE MAIN BELT: BIAS-CORRECTED DISTRIBUTIONS

The sample of main-belt asteroids classified in Table I is complete to mean opposition apparent magnitude B(a,0) = 12; it is 65% complete to magnitude 14 and has significant sampling to the limit of completeness of the numbered asteroids at about magnitude 15.5

The selection in favor of bright objects in observational programs is a bias against asteroids which are small, distant, and of low albedo. For evaluation and correction of the selection effects, we assume that the bias is, over broad distance zones, a function of the mean opposition apparent magnitude only. This assumption is a slight oversimplification since some survey programs contained deliberate attempts to sample objects from particular Hirayama familes, etc., and other more subtle selection effects. Since the compositional type is unknown before observation, however, the true bias effects cannot depend on the type; for this reason the "indeterminate" classifications of Table I are kept in the sample. Results with slightly modified assumptions are examined by Bowell et al. (1977).

Thus bias factors are computed at any apparent magnitude as the ratio of the count for the whole numbered population to the count for the classified sample. For the normalization we used 1330 numbered main-belt objects with $B(a,0) \le 16$ from the tabulation of Gehrels and Gehrels (1977). Modest corrections for incompleteness of the numbered sample were applied beyond magnitude 15.

While Figure 2 illustrates the process for the whole main belt, the actual computations were made separately in three distance zones, and the resulting (smoothed) bias factors are also plotted. For example, asteroid 342 Endymion with B(a,0)=14.31 in zone 2 has bias factor 4.67, and it is entered with this weight for the summation of bias-corrected distributions. We feel confident of the results for apparent magnitudes up to about 14.7 or weights up to 10. The statistics are ragged at the faint end, and also at the bright end because of the small numbers of asteroids actually present.

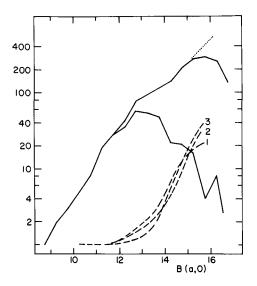


FIGURE 2. Total number of main-belt asteroids (upper solid line) and classified main-belt agteroids (lower solid curve) per 0 m 5 interval in mean opposition apparent magnitude B(a,0). The dotted line indicates correction for incompleteness of the catalogued asteroid population beyond apparent magnitude 15. Dashed curves are bias factors, computed as the (smoothed) ratio of the two solid curves, but in three distance zones: (1) 2.19 \leq a \leq 2.50; (2) 2.50 \leq a \leq 2.83, (3) 2.83 \leq a \leq 3.49.

FREQUENCIES OF THE COMPOSITIONAL TYPES

In the outer parts of the main belt, \underline{C} asteroids with diameters smaller than 50 km have apparent magnitudes fainter than the completeness limit of the numbered population and hence beyond reach of the bias analysis. Similar limits for types \underline{S} and \underline{M} are on the order of 25 km. For the entire main belt and diameters above $\overline{50}$ km we have observed 141 \underline{C} objects, and the bias weights add up to 422. For type \underline{S} the corresponding numbers are 73 and 91, and for type \underline{M} , 19 and 25. Thus the corrected frequency ratios are:

C:
$$(C + S + M) = 0.78$$

S: $(C + S + M) = 0.17$.
M: $(C + S + M) = 0.05$.

For types \underline{E} , \underline{O} , \underline{U} , and \underline{I} no rigorous bias analysis is possible since the statistics are poor and reliable diameters are often missing. With diameters probably greater than 50 km we have nine \underline{U} asteroids, two \underline{E} 's, and a single 0, for which the total bias weights add up to 14; and four asteroids classified \underline{I} with total weight 10, of which half are probably of type \underline{C} and half \underline{M} . Finally, it is probable that one or two of the asteroids classified \underline{M} on the basis of UBV colors alone are actually of type \underline{E} and \underline{U} .

Thus we estimate that the main belt contains 562 asteroids with D > 50 km, of which 76% \pm 6% are of type C, 16% \pm 2% of type S, 5% \pm 1% of type M, and 3% \pm 1% of other types. If the adopted relative albedos of the principal types are correct, these proportions should not be in error by more than the indicated statistical uncertainties.

DISTRIBUTIONS OVER DIAMETER

Figure 3 gives bias-corrected results for the diameter-frequency relation of types \underline{C} , \underline{S} , and \underline{M} . We note that, relative to the \underline{C} distribution, the \underline{S} objects become slightly less numerous at smaller diameters, and the \underline{M} objects more numerous. However, consider Figure 4, in which we have plotted the same distribution for type \underline{C} and the combined distribution for types \underline{S} and \underline{M} . According to current ideas of their chemistry and origin, the two curves may be loosely described as representing "primitive" and "evolved" objects.

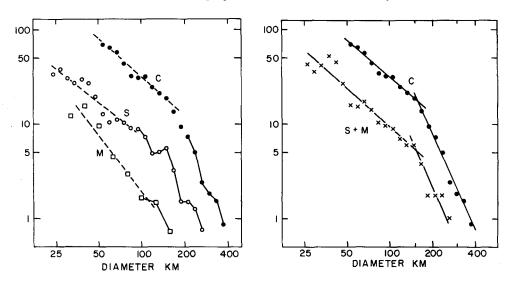


FIGURE 3. Bias-corrected number of asteroids of types \underline{C} (filled circles), \underline{S} (Open circles), and \underline{M} (Open boxes) in intervals of 0.05 in log diameter. Connected points represent diameter ranges over which the sampling is essentially complete. The data are somewhat smoothed in regions of poor statistics.

FIGURE 4. As in Figure 3, but for types \underline{C} (filled circles) and the sum of types S and M (x).

Within statistical noise limits the diameter-frequency functions for types \underline{C} and \underline{S} + \underline{M} are parallel both showing a break or change in slope at about $\overline{160}$ km. At all diameters the C objects are more numerous than types \underline{S} + \underline{M} by a factor of 3.5. The break at 160 km produces the well-known slope change in the magnitude-frequency relation at about absolute magnitude 9 (e.g., van Houten 1971). For small objects the slope is 1.3, and for diameters greater than 160 km it is 3.4

Thus the "silicate bump" or excess of evolved asteroids near 160 km first seen by Chapman et al. (1975) is present in absolute numbers, but no longer confined to type S. The conclusion reached two years ago evidently arose from insufficient observations of small C objects. The interpretations advanced by Chapman (1974,1976) and Chapman and Davis (1975) in terms of high collisional fragmentation strengths for stony-iron cores must be re-evaluated.

DISTRIBUTIONS OVER HELIOCENTRIC DISTANCES

For distributions of the C, S, and M types over orbital semi-major axis we

divided the main belt into eleven distance zones of roughly equal depth, five containing major Kirkwood gaps and six with no major gaps. For all types we found that the gap zones tend to fill in and become relatively better populated toward smaller diameters. This remarkable effect, that large asteroids avoid the Kirkwood gap regions more strongly than small ones, seems to have gone previously unnoticed but is easily demonstrated for the whole numbered population.

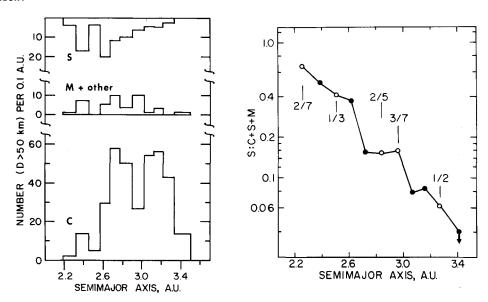


FIGURE 5. Bias-corrected distributions of \underline{C} , \underline{S} , and other compositional types over orbital semi-major axis, for diameters >50 km. Distance zones containing Kirkwood gaps are shaded.

FIGURE 6. Ratio of bias-corrected counts as a function of orbital semi-major axis, for S asteroids, and the sum of types C, S, and M for all diameters >50 km. Open circles are used for distance zones containing major Kirkwood gaps, and fractions indicate the ratio of sidereal periods with respect to Jupiter.

Bias-corrected type abundances as functions of semi-major axis are plotted in Figure 5. Figure 6 clearly shows the general decrease of the relative frequency of type \underline{S} with distance noted by Chapman et al. (1975); \underline{S} asteroids tend to fall in the inner and central parts of the belt, \underline{C} objects in the central and outer parts, and M and other types most frequently in the central regions.

Contrary to earlier conclusions, we see no significant depletion of type C relative to S, M, or U in the Kirkwood gap zones. In Table II we have reconstructed Table 4 of Chapman (1976). His conclusion that the relative frequency of S asteroids is greatly enhanced near the Kirkwood gaps was an artifact of the size effect noted above. That is, he used no specific diameter cut-off and hence was comparing small S asteroids with large C objects.

Chapman et al. (1975) noted an unusual distribution of types near the cluster of Kirkwood gaps around 2.9 A.U. Our data show one marked peculiarity in this region, namely, an excess of large (>80 km) $\underline{\text{M}}$ asteroids and a deficiency of smaller ones relative to type $\underline{\text{S}}$. The statistics are poor, however, comprising four $\underline{\text{M}}$ objects in each diameter range. Analogous effects are not seen in other gap zones.

TABLE II												
DISTRIBUTIONS	OF	TYPES	WITH	RESPECT	TO	KIRKWOOD	GAPS					

Asteroid	Fraction with of Kirkwoo		Fraction far from Kirkwood Gaps			
Туре	Chapman	This Paper*	Chapman	This Paper*		
<u>C</u>	11%	38%	89%	62%		
<u>s</u>	36%	34%	64%	66%		
<u>M</u>	1 710	37%	1.00	63%		
Other	31%	35%	69%	65%		

^{*}Diameter >50 km

In summary, the new analysis has removed most of the observational basis for models in which \underline{C} and \underline{S} asteroids respond differently to collisional fragmentation, both with respect to the diameter-frequency relations and with respect to the Kirkwood gaps.

THE OUTLIERS: MARS-CROSSERS, HUNGARIAS, HILDAS, AND TROJANS

Figure 7 illustrates the run of broad-band color with heliocentric distance

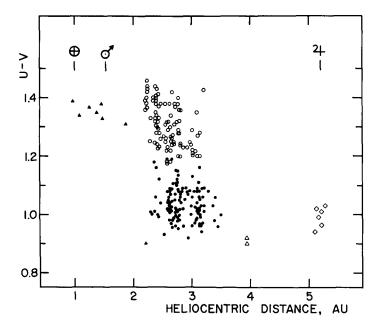


FIGURE 7. U-V color index for main-belt C (filled circles) and S (open circles) asteroids, Hildas (open triangles), Trojans (open diamonds), and Mars-crossers (filled triangles). Main-belt objects of types other than C or S are omitted for clarity. Adapted from Zellner et al. (1976).

for the whole minor planet domain. This overall view shows the main belt to be a transition zone between predominantly reddish colors due to ferrosilicate compositions and the more neutral tones of carbon-bearing materials. As may be seen in Figure 6, the proportion of carbonaceous objects increases exponentially with a distance scale length of less than 0.5 A.U.

The dozen small objects in our sample in Mars- or Earth-approaching orbits (433, 887, 1011, 1036, 1566, 1580, 1620, 1627, 1685, 1864, 1960UA, and 1976AA) were all observed by special efforts during favorable apparitions so that no meaningful bias analysis is possible. With a single proven exception, however, all of them have optical properties of types \underline{S} or \underline{O} ; and these are among the prime candidates for the parent or "carrier" bodies that supply us with the common stony meteorites (e.g., Levin et al. 1976). The anomaly is 1580 Betulia, a dark, neutrally colored 6-km body which is formally classifiable as type \underline{C} , but which may be an extinct cometary nucleus (Lebofsky et al. 1977).

Of the Hungaria family of small asteroids just inside the main belt at 1.9 A.U., only the largest, 434 Hungaria itself at 12-km diameter, has been observed. Surprisingly, it turns out to be one of the rare \underline{E} type (Morrison et al. 1977). Two Hilda asteroids (1212 and 1268) at the two-thirds resonance with Jupiter near 4 A.U. have been observed, by UBV photometry only. The colors are quite similar and suggestive of dark objects, but a composition distinct from the main-belt C asteroids is not yet excluded.

For the distant Trojans near the equilateral Lagrangian points of Jupiter, initial results indicated low albedos characteristic of carbonaceous material, but with reflection spectra quite unlike anything in the main belt (McCord and Chapman 1975b; Cruikshank 1976; Zellner et al. 1976). Recent observations, however, show a normal C-type spectrum for 1173 Anchises (Chapman, personal communication). Thus the view of the Trojan clouds as a separate, homogeneous population may have to be abandoned.

FUTURE WORK

Brighter than apparent magnitude 14, roughly 130 objects remain unobserved by the classification techniques. Further survey work will lead to better definition of the various compositional types, especially those for which few members are known at present. It is also probable that distinct new types will be recognized. Closer examination of known \underline{E} , \underline{O} , and \underline{U} objects may give critical insight into geochemical processes and relationships with meteorites.

It is within our power but clearly unnecessary to classify more than 1500 of the numbered asteroids. For statistical purposes, further survey work in the main belt will be most profitable at apparent magnitudes near 15. In Table I we have 36 objects with 14.5 \leq B(a,0) \leq 15.5, with bias factors ranging up to 30. In one observing season we could double or triple this sample, thus reducing the bias factors to 10 or so and greatly increasing our confidence level for the 30-to-60-km diameter range. At magnitude 16 we reach the unexplored fragmental tail of the size-frequency distribution, but the numbered asteroid population is incomplete, and evaluation of bias factors would require supporting work of the type undertaken for the Palomar-Leiden Survey.

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DISCUSSION

ARNOLD: Do the Hirayama families have compositional significance?

ZELLNER: The general rule seems to be heterogeneity among family members. However some of the dynamically best-proven families have no bright members or only one bright member, and are essentially unexplored.

WILLIAMS: It was stated that asteroid families are heterogeneous in composition. The results we have seen are on a few of the less well determined families and restricted to the few brightest members of the families. To conclusively determine whether families have a single composition, or a few compositional types, or are completely heterogeneous will require observing members of the best defined families (such as Eos or Koronis) and to go to faint members of these families.

80, 986.

SCHOBER: I would like to know, what you are really thinking about the existence of the E-type group of asteroids? Are the three objects only an exception, not be assigned to any other group?

ZELLNER: The three identified E asteroids, 44 Nysa, 64 Angelina, and 434 Hungaria, have uniquely high albedos and uniquely flat spectra, hence a high degree of recognizability. That does not imply a unique mineral, or course.

WASSON: You stated that the general change from S to C type asteroids with increasing distance seemed inconsistent with my hypothesis that the parent bodies of some mteorites formed at locations outside the asteroid belt, but as a result of planetary perturbations, now be present in asteroidal orbits. This represents a misunderstanding of my picture. The bulk of material in the asteroid belt probably formed in that region. The exotic materials are probably much rarer, but as a result of the Mars perturbations necessary for capture into asteroidal orbits, have a much higher probability of perturbation into earth crossing orbits that would allow them to fall as meteorites.

ANDERS: You said that all Mars crossers were S or O objects. How certain is this for Icarus? In two respects (spherical shape, eccentricity) it looks like an extinct cometary nucleus, and at least I find it hard to believe that a cometary nucleus should have S or O (i.e., ordinary chondrite) composition.

JOHNSON: Icarus vas observed by Tom Gehrel's group at UBVRI. The low value of the I reflectance indicates that this object is similar to other Apollos, such as Toro and has a chondritic type composition - not like Betulia for instance.

ZELLNER: Icarus came by before we really knew what we were doing, and it is somewhat difficult to fit it into the current picture. However it is certainly S- or O-like, and certainly not carbonaceous.

WASSON: It appears that in attempting to associate asteroid properties with meteorite categories you have assumed that all or most asteroidal materials can be found in terrestrial meteorite museums. It is important to bear in mind that our terrestrial selection of meteorites is biased and incomplete. Many intermediate types must exist, and some of these may be important constituents of asteroids.

ZELLNER: No such assumption is necessary. The optical types of asteroids would still be seen even if we had no meteorites to study. Classification of asteroids and identification with meteorites are two separate steps.

KELLER: You suggested that 1580 Betulia might be an extinct cometary nucleus. What is its diameter?

ZELLNER: The polarimetry indicates a C-like object with a diameter near 6 km; radar results from Arecibo give about 7 km. Thermal radiometry by L. Lebofsky, analyzed with the usual asteroid models, gives about 3 km.

We have never seen that kind of anomaly before. Unless some mistake has been made, the thermal properties must be very strange. But let me emphasize that these are highly preliminary results.

WETHERILL: I would just like to clarify the earlier answer regarding the minimum distance of 1580 Betulia from the sun. As a consequence of the free oscillations of its elements, as calculated by Williams, on a time-scale of

 ${\sim}10^4$ years this object repeatedly becomes not only earth-crossing but Venus-crossing as well.

WEISSMAN: On the problem of finding extinct cometary nuclei there is an object, periodic comet Arend- Rigaux, which is widely recognized as a comet about to become extinct. It will have a favorable opposition in February, 1978 and efforts should be made to observe it at that time, employing modern asteroid study techniques. Another similar object, Neujmin I, will make a favorable opposition in 1983.