50 MHz helicopter-borne radar data for determination of glacier thermal regime in the central Chilean Andes

Guisella GACITÚA,1,2 José A. URIBE,1 Ryan WILSON,1 Thomas LORIAUX,1 Jorge HERNÁNDEZ,1 Andrés RIVERA1,3

1Glaciology Laboratory, Centro de Estudios Científicos (CECs), Valdivia, Chile
2Universidad de Magallanes, Punta Arenas, Chile
3Department of Geography, Universidad de Chile, Santiago, Chile
Correspondence: Guisella Gacitúa <guisella.gacitu@umag.cl>

ABSTRACT. Despite their importance as freshwater reservoirs for downstream river systems, few glaciers in central Chile have been comprehensively surveyed. This study presents ground-penetrating radar (GPR) and field-based observations for characterizing the englacial and basal conditions of Glaciar Olivares Alfa (33°11’S, 70°13’W), central Chilean Andes. Using a 50 MHz radar mounted onto a helicopter platform, data were collected covering large portions of the glacier accumulation and ablation zones. The radar data revealed boundaries of a temperate-ice layer at the base of the eastern body of Glaciar Olivares Alfa which appears to be covered by colder ice that extends throughout large parts of the glacier. The thickness of the temperate ice layer is highly variable across the glacier, being on average 40% of the total ice thickness. Radar data analyses reveal regions of cold ice at the bottom/base of the glacier and also patterns of highly saturated sediments beneath the glacier. Using GPR data, this study represents the most exhaustive analysis of glacier ice structure performed in the central Chilean Andes. The results will enable improved estimations of the glacier’s mass balance and ice dynamics, helping us to understand its further development and its impact on water availability.

KEYWORDS: aerogeophysical measurements, applied glaciology, basal ice, glacial geomorphology

INTRODUCTION
Santiago de Chile (33°S), with ~6.7 million inhabitants, is located at the foot of the central Andes, in the Maipo river basin. Glacier inventories compiled for the Maipo basin estimate an approximate ice area coverage of 420 km², contributing up to 67% of river flow during dry seasons (Peña and Nazarala, 1987; percentage is under dispute at present). Over recent decades, glaciers in central Chile (32–41°S) have shown significant frontal retreat and accelerated areal reduction, presumably as a response to atmospheric warming and a reduction in precipitation (Casassa, 1995; Rivera and others, 2002, 2006; DGA, 2011). Glacier inventory data from this region yield a negative glacier area variation of 8% for the period 1955–2000. Moreover, predictions show a possible increase in air temperature by a rate of 0.25°C decade⁻¹ (Falvey and Garreaud, 2009), hence further glacier changes are expected to occur in response.

Early observations by Lliboutry (1956) gave rise to the notion that glaciers in the central Chilean Andes were mainly cold and highly dependent on climatic fluctuations. More recently, glacier monitoring programmes, initiated to estimate mass-energy-balance components (DGA, 2012; CECs, 2013), have suggested that some glaciers in central Chile may, in fact, be characterized as polythermal, containing perennial temperate and cold ice structures (Blatter and Hutter, 1991). To date, there has been no attempt to clearly identify or quantify the distribution of cold and warm ice structures for any glacier in central Chile.

The complexity of polythermal glacier structures has been increasingly recognized through the use of geophysical techniques (Irvine-Fynn and others, 2011). Widely used for measuring ice thickness and mapping glacial bedrock and stratigraphy (Plewes and Hubbard, 2001; Dowdeswell and Evans, 2004; Bingham and Siegert, 2007), ground-penetrating radar (GPR) systems have been deployed to survey the thermal properties of ice masses. Air, ice, water and other heterogeneities (e.g. rock, volcanic dust) all have contrasting dielectric permittivities that yield distinct responses in radar returns (Annan and others, 1975). Hence, to a first order, it is possible to distinguish between cold ice (below ~5°C), which is relatively transparent for radar propagation, and warm ice, whose water inclusions scatter radar signals. As a result, reflections can be analysed to distinguish englacial ice conditions and to identify water-/air-filled cavities or channels by observing the intensity of the return (Jacobel and Raymond, 1984; Moorman and Michel, 2000; MacGregor and others, 2012).

Over the last two decades, analyses of bed reflection power (BRP) have been conducted for several major ice sheets, especially in Greenland and Antarctica, with the aim of determining subglacial conditions and assessing their potential impacts on ice dynamics (Bentley and others, 1998; Gades and others, 2000; Oswald and Gogineni, 2008; Jacobel and Welch, 2009; Ashmore and others, 2014). This technique is mostly applicable where the ice-bed boundary is relatively flat, a characteristic which reduces the complex scattering of radar returns by the bed topography. Besides analysing major ice sheets, radar BRP has also been successfully applied to a number of valley glaciers (Capland and Sharp, 2001; Pattyn and others, 2003, 2009; Matsuoka and others, 2007; Wilson and others, 2013). In all cases, the biggest issue to be overcome in attaining accurate values of BRP is to account correctly for englacial attenuation of the radar signal. Englacial,
attenuation can be estimated through the implementation of empirical- and modelling-based approaches. In the former, attenuation coefficients are derived empirically from travel-time versus reflection intensity relationships. In the latter, englacial temperature modelling is used, calibrated by englacial borehole temperature measurements (whenever possible) (Wilson and others, 2013).

Here we present the results of signal analyses of 50 MHz GPR data acquired from a helicopter-borne system across the highly elevated Glaciar Olivares Alfa, central Chilean Andes. The aim of these analyses is to identify the supraglacial, englacial and subglacial characteristics of this glacier through in situ observations and theoretical approaches. Consequently, we were able to use the data to delineate the boundary between warm and cold ice and determine the drainage networks. Considering the potential attenuation, given the two-layered thermal regimes of the ice, we obtained the distribution of the reflective patterns, featuring the potential occurrence of water streams, dams and pools.

Site location

Within the main Maipo basin, the largest glaciers are located in the upper Olivares sub-basin, which experienced a 25% reduction in ice area between 1955 and 2000 (Marangunic, 1979; Valdivia, 1984; DGA, 2011). Located at an elevation ranging from 4240 to 4830 m a.s.l., Glaciar Olivares Alfa (33°11′S, 70°13′W) has an approximate area of 3.91 km² and flows from south to north. Figure 1 shows the position of ten mass balance stakes, installed as part of an ongoing monitoring programme, and whose movements provide the ice-velocity validation data used in this study. Field-based observations of the mass-balance stake network made between December 2012 and January 2014 reveal an overall negative trend (−162.5 cm w.e. d⁻¹). During the observation period, a maximum ablation rate of 2.41 cm w.e. d⁻¹ was measured at stake 3 between December 2013 and January 2014, while the maximum accumulation rate of 0.72 cm w.e. d⁻¹ was measured at stake 1 between May and June 2013. Ice surface velocity at Olivares Alfa throughout

Fig. 1. Location map of Glaciar Olivares Alfa. The red lines depict transects of the radar data used in the analyses. Black points show the position of installed mass-balance control stakes (numbered 1–10).
the observation period was shown to be particularly low (average of 2.75 m a\(^{-1}\)) (CECs, 2013). Figure 1 also shows the radar tracks acquired in May 2013.

**Surface topography data**

In December 2012, a high-precision lidar system, CAMS (CECs Airborne Mapping System), was used on board a helicopter to acquire data for Olivares Alfa and other surrounding glaciers in the upper Olivares sub-basin. The airborne system included a RIEGL laser scanner (LMS-Q240-60) combined with a dual-frequency GPS (Javad Lexon GD) and an inertial measurement unit (iMAR iNAV-FMS), providing surface elevation data with an estimated vertical accuracy of ±0.3 m maximum.

The resulting lidar point cloud measurements were calibrated with known surface contour points. Subsequently, the filtered cloud points (with a density 1.07 points m\(^{-2}\)) were converted into a digital elevation model (DEM) using an interpolation method (triangulated irregular network, TIN), yielding a cell size resolution of 2 m. ‘Flow accumulation patterns’ were detected from the DEM to simulate the hydraulic drainage network (using the tools available in ArcGIS 9.3).

**Radar data acquisition**

Radar data were acquired for this study using a helicopter-borne system, consisting of a hanging dual bow-tie dipole antenna, designed and modelled to operate at a central frequency of 50 MHz. The system consists of a high-voltage (2.4 kV) impulse transmitter generator, a signal receiver, a geodetic GPS for precise georeferencing of data and a laser altimeter for altitude control of the antenna above the ice. The radar signal is captured by a 14-bit analogue-to-digital converter, at a sampling frequency of 400 MHz. During the survey, the maximum pulse repetition frequency (PRF) of the transmitter was used (4 kHz) together with the minimum allowable stacking (256 traces). This system configuration related to the power consumption and the internal power dissipation of the transmitter, as well as to the data transfer capacity. The configuration used was considered optimum for this radar system as it produced the maximum trace rate (15.6 traces s\(^{-1}\)) with a high PRF, suitable for high-speed helicopter surveys (20 m s\(^{-1}\)).

Data were acquired at the beginning of the 2013 (austral) winter season, prior to any major precipitation events. The total flight track, which was ~33.17 km in length and consisted of 22 111 data points, was divided into sections of longitudinal and transverse profiles across an ice surface that was mostly smooth with moderate slopes on the margins. Taking into account only point measurements that reached the ice bottom, the antenna height was, on average, 51 m (standard deviation of 32 m) above the ice surface. The distance between traces ranged from 1.5 to 2 m according to the helicopter speed. Figure 1 shows the GPR data points (in red) for which bedrock was detected and that were subsequently used in this study (16 467 traces). Gaps in the red line denote the lack of bedrock detection below the ice.

**Radar data analyses**

Prior to analysis, the radar data were (1) horizontally rearranged using the geodetic GPS information collected during flight; (2) corrected vertically to zero time (by determining the direct wave from transmitter to receiver); and (3) cut to 2402 ns (two-way travel time), ensuring that the maximum ice depth was detected within this range. A vertical time increment of 2.5 ns was used during data collection, which resulted in a radargram of 961 points of vertical representation.

Glacier surface and bedrock layers were identified within the resulting radargram using a semi-automatic procedure. During this procedure the user picked two points from a continuous reflector (indicative of a visible layer in the radargram), made a linear interpolation between the selected points and then corrected the result to the position of the nearest maximum reflector point in the trace. Due to the complex subglacial topography detected and the multiple-echoes received, the picked layers were often further edited to avoid potential error.

In addition to the glacier surface and bedrock layers, sections of scattering were identified along the radar profile that depict englacial transitions in the ice structure. These transitions were assumed to define the boundary between cold and temperate ice. When distinguishing these transitions, scattering produced by surface features was excluded. The power of each picked horizon was computed individually using Eqn (1) for the different sections of interest.

\[
P = \frac{1}{n_2 - n_1 + 1} \sum_{n=n_1}^{n_2} s_n^2
\]

where \(s_n\) is the amplitude (V) of the signal, and \(n_1\) and \(n_2\) are the starting and ending sample numbers of the calculation window.

**Surface, bedrock and internal reflection power (SRP, BRP and IRP)**

Considering only the geometrical spreading loss, which is a function of radar wave travel path length, SRP is a measure of the reflected power from the ice surface (mainly a function of the antenna height). SRP was computed for at least one pulse period length (of each trace) with respect to the picked sample \(s_n\). The moving window limits used were 8 samples above and 15 samples below \(s_n\) and represented 60 ns (~5 m).

The layer identified as bedrock in the radargram was used to compute the power reflection produced at the bottom of the ice (BRP). As was done for SRP, a same-size moving window was used with respect to the sample picked that had the highest amplitude reflected. Lastly, the englacial transitions between cold and temperate ice were also delineated in the radargrams. The reflected power through the temperate ice thickness (IRP) was calculated for the section of each trace that presented a scattered signal return (associated with attenuation due to changes in the ice conditions). The moving window length varied according to the thickness of the scattered region and neglected reflections that might be coming from the surface (SRP) or directly from the bedrock (BRP).

**Ice-thickness variation correction**

The radar signal amplitude is reduced by the path length mainly due to geometrical spreading and signal absorption within the ice. The relationship between measured BRP (Eqn (1)) and BRP corrected for ice absorption (BRP\(_{\text{est}}\)) is given by

\[
\text{BRP}_{\text{R}} = \frac{\text{BRP}_{\text{R}}}{\text{BRP}_{\text{est}}} - 1
\]

BRP\(_{\text{R}}\) is the residual BRP, the variations of which are not
related to changes in the amount of energy transmitted into the ice (Gades, 1998). In order to obtain \( B_{\text{est}} \), some authors have used empirical methods, where the measured \( B_{\text{est}} \) values from a given area are plotted against ice thickness and a best-fit curve is used as a representative model (usually an exponential fit) (Gades, 1998; Gades and others, 2000; Copland and Sharp, 2001; Pattyn and others, 2009). In contrast, other authors have estimated \( B_{\text{est}} \) theoretically by using the radar equation for which parameters are known (Bentley and others, 1998; Peters and others, 2005). The empirical approach assumes that \( B_{\text{est}} \) is largely a factor of geometrical spreading, an assumption which breaks down in complex settings, such as valley glaciers characterized by heterogeneous media. Indeed, for this study, while a good exponential fit was found between the ice and/or englacial water is assumed to depress \( B_{\text{est}} \) after applying the correction for losses and is proportional to the reflectivity of the base. This relationship with temperature depends on the wavelength \( \lambda \) in the ice and the loss tangent \( \tan(\delta) \), which relates to the dielectric losses within ice due to absorption of the electromagnetic radar waves and their dissipation as heat (Evans, 1965; Matzler, 1987).

\[
L_g = e^{-\pi \tan(\delta) / \lambda}
\]

To obtain the antenna-height variation for SRP (\( \text{SRP}_{\text{est}} \)), the general expression (Eqn (3)) was simplified for airwave travel:

\[
\text{SRP}_{\text{est}} = P_{\text{in}} G L_g
\]

The following expression was then deduced to estimate \( B_{\text{est}} \):

\[
B_{\text{est}} = P_{\text{in}} G L_g T_{ai}^2 L_i^2 R_{ib}
\]

\( L_g \) is a function of the wavelength \( \lambda \) in air and \( \varepsilon_i \) is the relative dielectric permittivity of the ice:

\[
L_g = \frac{(G\lambda)^2}{[8\pi(h_a + h_i)]^2}
\]

Experimental studies have shown that \( L_i \) decreases sharply when temperatures are just below the melting point. This relationship with temperature depends on the wavelength \( \lambda \) in the ice and the loss tangent \( \tan(\delta) \), which relates to the dielectric losses within ice due to absorption of the electromagnetic radar waves and their dissipation as heat (Evans, 1965; Matzler, 1987).

\[
L_i = e^{-2\pi \left[ \tan(\delta) / \lambda \right]}
\]

RESULTS

Radar-detected ice thickness for Glaciar Olivares Alfa reached a maximum of \(~130\) m, with a mean of \(56\) m.
Aside from those acquired from the western branches of the glacier, the radargrams show a clear transition from highly transparent ice to ice that significantly scatters the radar signal. This transition is taken to indicate the englacial thermal boundary between cold ice and underlying temperate ice, existing at the pressure-melting point. The identification of these boundaries became more laborious at the margins and near the surface of the glacier. In such areas the seasonal supraglacial channels eventually also develop into englacial conduits that reach the underlying temperate region and the glacier bedrock. The supraglacial channels result in highly noisy sections in the radargrams. In addition, when the distance between the antenna and the surface was <50 m, multiples of the radar direct wave masked the surface reflection, hindering the detection of features from the near subsurface (‘fake reflector’ in Fig. 2).

Figure 3a and b show longitudinal (L1–L2) and transverse (T1–T2) radargrams relative to ice-flow direction, respectively, together with the corresponding SRP, IRP and BRP results and the reflection coefficient measured from the ice–bedrock interface $R_{i b}$. Figure 4a shows the resulting total ice thickness map using a natural neighbour interpolation and a two-dimensional average filter for smoothing the raster surface. Ice thickness was spatially interpolated to a raster cell size of 20 m assuming a minimum depth of 5 m at the margins.

The regions of scattered radar returns, visible in Figures 2 and 3, indicative of temperate ice, reach a maximum thickness of ~70 m above the bedrock, with a mean of 24 m. Using the same process applied to interpolate the total ice thickness (Fig. 4a), the spatial distribution of the temperate ice thickness across the glacier was also interpolated.
The temperate ice thickness was found to be highly variable, becoming thinner above the equilibrium line (4600 m a.s.l.). In relation to the total ice thickness, the temperate ice bulk represents, on average, 40%.

As described earlier, the magnitude of the basal reflection is a function of both the physical condition of the bed (i.e. wet versus dry) and the englacial conditions, the latter being ruled by the temperature of the ice through which the radar signal has passed (i.e. predominantly warm, cold or mixed). Therefore, we estimated the reflection power assuming losses for the temperate ice (near the melting point) and the cold ice at –5°C (MacGregor and others, 2007; Conway and others, 2009). The radar equation (Eqn (7)) was then evaluated for the dielectric attenuation (\(\tan(\delta)\)) at –1°C (\(\tan(\delta) = 0.006\)) and at –5°C (\(\tan(\delta) = 0.0038\)) (Evans, 1965). In terms of reflection anomalies, there are two instances when BRP\(_R\) is expected to be around or below 0: (1) Eqn (2) has correctly accounted for englacial attenuation of the signal, or (2) there is low reflectivity from the base. Here BRP\(_R\) was <0 for 83.7% of the detected data points, with smaller values being predominantly situated outside of the englacial layer of the identified temperate ice (Fig. 4b).

The spatial distribution of high positive BRP\(_R\) values corresponds well with the identified temperate ice layer, suggesting the presence of a substantial amount of water at the base of the glacier. Positive BRP\(_R\) values are particularly prominent for temperate ice regions located close to the glacier terminus, where englacial and subglacial drainage networks are likely to be more developed (Fig. 5b).

In order to interpret BRP\(_R\), it is necessary to observe the processes of the signal through the media above. The energy reflected from the surface quantifies the signal attenuation purely related to the geometrical spreading. The qualitative analyses of the reflected power from internal features help

**DISCUSSION**

Data acquired using a 50 MHz airborne radar system allowed for the identification of distinct temperate and cold ice layers within Glaciar Olivares Alfa. The presence of these layers confirms earlier notions of this glacier being polythermal; however, there was no quantification of the temperate ice. Following the classification of the thermal regimes of polythermal glaciers carried out by Irvine-Fynn and others (2011), Olivares Alfa is shown to correspond to the glacier type for which temperate ice is distributed as a function of ice thickness and/or geothermal heat flux (resembling glaciers located in the High Arctic).

Although the transition from cold ice to temperate ice at the pressure-melting point is considered to be gradual (Moorman and Michel, 2000), in the radargrams the delineation of the transition between non-scattered signal zones (cold ice) and scattered signal zones (temperate ice) gives a reasonable method for identifying their spatial distribution. Due to the strong dependency of the dielectric attenuation on ice temperature along the propagation path (Matsuoka and others, 2010), this two-layered thermal regime was considered for estimating the power reflected from the bedrock (BRP). In order to interpret BRP, it is necessary to observe the processes of the signal through the media above. The energy reflected from the surface quantifies the signal attenuation purely related to the geometrical spreading. The qualitative analyses of the reflected power from internal features help

![Fig. 4. Spatial distribution of ice thickness (cell size 20 m). (a) Total ice thickness from surface to bedrock; T1–T2 and L1–L2 indicate respectively the transversal and longitudinal sections shown in Figure 3. (b) Spatial distribution of the reflective layer thickness interpreted as temperate basal ice (dashed line in (a)).](https://doi.org/10.3189/2015AoG70A953)
us to understand the reflection patterns generated by the effect of englacial heterogeneity on the propagated energy above the bedrock. In this regard, from Figure 3 it can be seen that IRP increases substantially at the margins of the glacier (shallower ice) where the ice contains multiple englacial events originated by surface roughness (Fig. 5a). Therefore, BRP measurements and further inferences of basal conditions at these locations may be less reliable due to potential underestimation of the attenuation.

The relationship between directly measured power and estimated power was used as an indicator of unexpected reflectors, interpreted as saturated material at the glacier base or as liquid water. Highly reflective patterns, suggesting the latter, were mostly found for areas underlain by the temperate ice and it is likely that the water source for these is mostly supraglacial. Measurements were made at the end of the melt season when runoff had stopped (average air temperature –10 ± 3.03°C) and refreezing had likely begun. Therefore, the highly reflective radar patterns detected may be the result of the presence of late-season meltwater which, having made its way to the glacier bed, has become trapped behind a thermal dam (Skidmore and Sharp, 1999) and/or in overdeepenings.

Early research suggests that ‘cold ice’ is effectively attached to the bedrock and that, given the low temperatures, englacial hydraulic connections are not supported (Blatter and Hutter, 1991; Paterson, 1994). However, recent studies of polythermal glaciers (which contain cold ice) have demonstrated that drainage networks between supraglacial streams and englacial conduits can develop within cold ice which eventually outflow to the base (Gulley and others, 2009; Irvine-Fynn and others, 2011). Such observations could help explain the existence of the patterns of radar reflectivity found outside of the temperate ice identified. It could also be the case that a thin layer of temperate ice exists at the base which was not detected by the radar.

The resulting basal reflectivity patterns and the interpreted dielectric values (which contrast the ice bed) show localized zones of saturation (Fig. 6). This saturation suggests that Glaciar Olivares Alfa might be hydrologically configured by a small number of large channels (instead of widespread small conduits) which efficiently transport meltwater out of the glacier. This type of hydrological configuration is characterized by channels that change size depending on the amount of discharge (Björnsson, 1998; Bennett and Glasser, 2011). At the same time this hydrological configuration also influences ice motion by reducing basal traction (Rippin and others, 2005). Such influences may explain the relatively low surface velocities observed at Glaciar Olivares Alfa. Between December 2012 and August 2013, ice velocities, measured at stake locations on the glacier surface (see Fig. 1) ranged from 0.9 to 5.1 m a⁻¹,

Fig. 5. Drainage network models. (a) Surface drainage derived from 2 m cell DEM (December 2012). (b) Basal drainage network system derived from the bedrock map interpolation (20 m cell size). Red delineations show overdeepenings of the terrain.

Fig. 6. Patterns of positive BRP and spatial distribution of the dielectric permittivity values at the base. Values are scaled for a distinctive representation of a frozen base (yellow) and saturated materials (blue). Background image shows the basal drainage network modelled from Figure 5b. Dashed line delineates the layer in Figure 4b.
which is ‘slow’ compared to other nearby glaciers. Surface velocity at Olivares Beta, for example, which is located ~4 km to the north of Olivares Alfa, was observed to range from 2.3 to 12.8 m a\(^{-1}\) over the same period (CECs, 2013).

The GPR data analyses made for this study give us an overall idea of the basal conditions of the glacier; however, the method applied cannot guarantee accuracy on the detection of accumulated water. The restrictions are mostly attributed to the system resolution (i.e. the water layer is too thin to be detected) and to the underestimation of the englacial attenuation. Anyway, the methodology used provides a fairly representative approach to the subglacial characteristics of Glaciar Olivares Alfa.

CONCLUSIONS

A 50 MHz airborne radar system was used to survey the polythermal Glaciar Olivares Alfa. This survey represents a unique GPR dataset for the central Chilean Andes glaciers, allowing the characterization of englacial and subglacial features. Radar data revealed that Olivares Alfa consists of a two-layered thermal structure, with temperate ice lying at the base, covered almost entirely by cold ice. The underlying temperate ice is connected to the surface by englacial conduits through which subglacial meltwater can drain. Overall, the distribution of the warm ice suggests that the temperate layer identified developed as a result of ice thickness and the geothermal heat flux.

Although the temperate ice covers a large part of the base of the glacier, reflectivity patterns do not correlate to the whole area covered but only to localized areas where accumulated water was detected. However, saturated materials are more widely spread and near the lower front. These findings might be restricted by the limitations of the radar system, specifically when detecting thin layers of water and due to potential underestimation of the englacial attenuation. However, the GPR method described is shown to successfully characterize both the basal conditions and the polythermal conditions, variables which are poorly studied and are important when estimating mass balance and ice dynamics.

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