A distributed surface energy-balance model for complex topography and its application to Storglaciären, Sweden

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ABSTRACT. A grid-based surface energy-balance mass-balance model has been developed to simulate snow- and ice melt in mountainous regions with an hourly resolution. The model is applied to Storglaciären, a valley glacier in Sweden, using a 30 m resolution digital elevation model. Emphasis is directed towards computing the radiation components. These are modelled individually, considering the effects of slope angle, aspect and effective horizon. A new parameterization for snow albedo is suggested, modifying the albedo of the preceding hour as a function of time after snowfall, air temperature and cloudiness. The model is used to provide the meltwater input for discharge modelling and to assess the influence of the individual components on melt. Results are validated by means of observed melt rates, patterns of snow-line retreat and proglacial discharge. In general, simulations are in good agreement with observations. In particular, the diurnal and seasonal fluctuations of discharge are simulated remarkably well.

1. INTRODUCTION

In recent years there has been increasing interest in predictive tools for spatially distributed estimates of melt rates (Kirnbauer and others, 1994), further promoted by increased availability of remote-sensing data. Although, for many purposes, melt rates are obtained by simple empirical temperature index methods (Hock, 2003), more physically based energy-balance models generally better take into account the large spatial and temporal variability in melt rates typically encountered in a valley glacier environment. However, few studies have attempted to extend the surface energy balance at the point scale (for summary see Ohmura and others, 1992; Hock, 2005) to a larger spatial unit (e.g. on a catchment scale). Distributed models for snow-covered basins have been presented by, for example, Blöschl and others (1991), Ohta (1994), Ujihashi and others (1994) and Fierz and others (1997), while models developed for valley glaciers have been suggested by Escher-Vetter (1985), Funk (1985), Arnold and others (1996), Hock and Noetzli (1997), Brock and others (2000b), Escher-Vetter (2000) and Klok and Oerlemans (2002). However, these show one or a combination of the following shortcomings: albedo is prescribed rather than simulated; longwave incoming and outgoing radiation are assumed constant in space; the direct and diffuse components of solar radiation are not calculated individually; or the surface temperature is assumed to be constantly at melting point. Hence, part of the spatial and temporal variability of energy-balance components is neglected.

This paper presents a fully distributed surface energybalance model and its application to Storglaciären, Sweden, for two melt seasons. The model calculates the components of the surface energy balance for every hour and each gridcell, based on meteorological data collected at one point on the glacier. Direct and diffuse radiation are treated individually, considering topographic effects. Sky and terrain radiation are also considered separately for computation of both the diffuse and longwave irradiance. Albedo and surface temperatures are generated internally by the model. The bulk method is applied for calculating the turbulent fluxes. Results are validated by means of observations of discharge, melt rates and snow-line retreat.

2. PHYSICAL SETTING AND DATA INPUT

Storglaciären is located in northern Sweden ($67^{\circ}55'$ N, $18^{\circ}35'$ E), has an area of 3 km² and ranges in elevation from ~1120 to ~1730 m (Fig. 1). The drainage basin of the glacier is 70% glacierized. The glacier holds the longest continuous and detailed mass-balance record in the world (Holmlund and Jansson, 1999). The mass balance was positive in 1993 (1.00 m), and negative in 1994 (-0.37 m), although summer balances were relatively similar (-1.25 m in 1993 and -1.43 m in 1994).

During the 1993 and 1994 melt seasons, up to five automatic weather stations were operated on the glacier (Hock and Holmgren, 1996). The air-temperature, humidity, wind-speed, global radiation, reflected shortwave radiation and net all-wave radiation data collected at station B (Fig. 1), located at 1370 m a.s.l. close to the equilibrium line, were used to force the model. However, the data of all meteorological stations on the glacier were analyzed to investigate their spatial variability, as air temperature, relative humidity, wind speed and precipitation have to be extrapolated to each gridcell. As an example, scattergrams of air-temperature, humidity and wind-speed data at stations A and B are given in Figure 2.

Air temperature correlated well between stations, with generally higher temperatures at lower elevations. An average lapse rate of $0.55 \text{ K} (100 \text{ m})^{-1}$ was obtained from all the data available and applied in the model, although lapse rates on glaciers have been found to vary in time (Braun and Hock, 2004). We investigated this simplification by running the model using a variable lapse rate as measured every hour during the sub-periods of simultaneous



Fig. 1. Drainage basin of Storglaciären with 25 m contour lines. N and S refer to the sites of the water-stage recording stations at the glacial streams Nordjåkk and Sydjåkk. The black dots mark the positions of the ablation stakes in 1994, only slightly differing from those in 1993. The circles labelled A–E denote the sites of five micrometeorological stations on the glacier.

temperature measurements on the glacier. Model results differed only negligibly. We also explored the possibility of expressing a temporally variable lapse rate as a simple function of air temperature, but we did not detect any significant relationship. Thus, we adopt a constant lapse rate, allowing the model to be forced by data from only one weather station. Relative humidity varied relatively little among stations and was therefore assumed to be equal over the entire grid. As expected, wind speed displayed the largest scatter. Westerly winds dominated, coinciding with the down-glacier direction. During high wind-speed conditions, wind speed at the station in the accumulation area (station C) tended to be lower than at the meteorological stations at lower altitudes, probably due to the proximity of a precipitous rock wall and resulting shielding effects. For low wind speeds ($<3 \text{ m s}^{-1}$), especially combined with high air temperatures, an increase in wind speed towards the southern margin (station E) and in particular towards the glacier tongue (station A) was observed (Fig. 2). Despite these apparent systematic variations and considering the large scatter among stations, the data available are considered too sparse to derive a general scheme to quantitatively assess the spatial distribution of wind speed. Thus, wind speed measured at station B was assumed representative for the entire area calculated.

Measured precipitation was increased by 35% to account for the gauge undercatch error and then extrapolated assuming a 10% increase with elevation for the catchment (Hieltala, 1989). Besides the meteorological data, the model requires a digital elevation model (DEM) sufficiently large to allow for the computation of topographic shading of the area of interest and raster maps containing slope and aspect angles of each gridcell. The DEM was based on the 1:20 000 map by Holmlund and Schytt (1987). In order to distinguish between firn and ice albedo after the retreat of the snow-line, the model also needs a raster map indicating for each glaciated gridcell whether the surface below the winter snow cover is firn or ice. The boundary is approximated from the previous year's snow-line.

3. SURFACE ENERGY-BALANCE MODEL

For every hour and each gridcell the energy at the surface available for melt $Q_{\rm M}$ is calculated from

$$(I + D_{s} + D_{t})(1 - \alpha) + L_{s}^{\downarrow} + L_{t}^{\downarrow} + L \uparrow + Q_{H}$$
$$+ Q_{E} + Q_{G} + Q_{R} + Q_{M} = 0, \quad (1)$$

where I is direct solar radiation, expressed in terms of the beam radiation received on the horizontal, D_s and D_t are diffuse sky and diffuse terrain radiation, respectively, α is the albedo, L_{s}^{\downarrow} and L_{t}^{\downarrow} are longwave sky and terrain irradiance, respectively, $L \uparrow$ is longwave outgoing radiation, $Q_{\rm H}$ is the sensible-heat flux, $Q_{\rm E}$ is the latent-heat flux, $Q_{\rm G}$ is the ground heat flux in the ice or snow and $Q_{\rm R}$ is the energy supplied by rain. Energy fluxes directed towards the surface are taken positive, those away from the surface negative. The effects of subsurface melting are not considered. The energy available for melt, $Q_{\rm M}$ (W m⁻²), is converted into meltwater equivalent $M \pmod{h^{-1}}$. The effects of Q_L on the mass balance and on the water available for runoff are included: *M* provides the input for the runoff modelling. *M* corrected for the mass transfer by sublimation or resublimation, henceforth referred to as *ablation*, will be compared to mass-balance data.

3.1. Global radiation

Highly sophisticated models have been proposed for spectral solar radiation in complex terrain (Dozier, 1980), but their use is restricted to clear-sky conditions and they require various atmospheric parameters as input. We apply a simpler method using global radiation data at one point and



Fig. 2. Air temperature (°C), relative humidity (%) and wind speed ($m s^{-1}$) of station A (1250 m a.s.l.) on the glacier tongue vs station B (1370 m a.s.l.) close to the equilibrium line (Fig. 1), using hourly means of the 1994 melt season.

applicable under all weather conditions. Measured global radiation is separated into the direct and diffuse components, which are then extrapolated individually to each gridcell considering terrain effects. The separation is based on the ratio of measured global radiation G to top-of-atmosphere radiation I_{TOA} . With increasing cloudiness, G/I_{TOA} tends to decrease, whilst the diffuse portion D/G increases. In the case of a completely overcast sky with low, dark clouds, the ratio G/I_{TOA} is smallest and all global radiation is diffuse. Empirical relationships between D/G and the G/I_{ToA} have been suggested by, for example, Liu and Jordan (1960) and Collares-Pereira and Rabl (1979). These may vary with space and time as a function of atmospheric conditions and site characteristics such as elevation, surrounding topography and its reflecting characteristics. Therefore, in the present study, a new empirical relationship was established using data collected by the meteorological station of the Swedish Meteorological and Hydrological Institute in Kiruna, 60 km east of Storglaciären (67°50' N, 18°26' E; 408 m a.s.l.).

Hourly data of diffuse and global radiation for May– September 1987–96 were analyzed. The ratios D/G are plotted against G/I_{TOA} in Figure 3a. Top-of-atmosphere radiation I_{TOA} is calculated using standard methods (Sellers, 1965):

$$I_{\text{ToA}} = I_0 \left(\frac{R_{\text{m}}}{R}\right)^2 (\cos\phi\cos\delta\cos\omega + \sin\phi\sin\delta), \quad (2)$$

where $I_0 = 1368 \text{ W m}^{-2}$ is the solar constant (Fröhlich, 1993), *R* and *R*_m are the instantaneous and the mean sun–Earth distances, respectively, ϕ is the latitude, δ the solar declination and ω the solar hour angle.

The ratios considered are expected to lose accuracy with decreasing radiation amounts. Therefore, global radiation data or calculated top-of-atmosphere radiation less than $20 \text{ W} \text{ m}^{-2}$, or data when zenith angles exceeded 85°, were excluded from the dataset, leaving a total of about 22 000 data points. Figure 3a displays large scatter as the relationship is expected to vary with cloud type and zenith angle. Multiple regression techniques indicated that the effect of zenith angle was negligibly small. Therefore, the zenith angle was neglected, and daily means were applied in further analysis, thus also reducing the susceptibility of the involved ratios to errors, and hence the scatter in the correlation. A cubic polynomial function was fitted by the least-squares method to all daily data and to the data of each month individually (Fig. 3b and c), the latter in order to investigate the seasonal variation in the correlation. Whereas the functions for June-September hardly differ from each other, the function obtained for May yields ratios of D/G up to 0.1 higher for a given ratio of G/I_{ToA} . The difference is attributed to the presence of a snow cover in May, resulting in enhanced diffuse radiation due to reflection from adjacent slopes and backscattering of reflected global radiation. The function derived from all daily data reads:

$$\frac{D}{G} = \begin{cases} 0.15 & : x \ge 0.8\\ 0.929 + 1.134x - 5.111x^2 + 3.106x^3 & : 0.15 < x < 0.8\\ 1.0 & : x \le 0.15 \end{cases}$$
(3)

with D/G the ratio of total diffuse to global radiation and x the ratio of global to top-of-atmosphere radiation G/I_{ToA} . The limits of 0.15 and 0.8 were arbitrarily chosen from the plot (Fig. 3b).

The plausibility of the least-squares fit was evaluated by comparing it to the curve obtained by averaging the data



Fig. 3. Ratio of diffuse radiation to global radiation D/G vs the ratio of global radiation to top-of-atmosphere radiation G/I_{ToA} at Kiruna: (a) hourly data; (b) daily means and functions to describe the relationship; (c) least-squares fits for May–September based on daily means.

over defined classes of ratios G/I_{ToA} ('empirical function' in Fig. 3b). For each class the ratios G/I_{ToA} and the corresponding ratios D/G were averaged and plotted against each other. The class width was variable and adjusted to include 100 values for each class. The function thus obtained agreed well with the fitted function, indicating that the least-squares fit provides a reasonable description of the correlation (Fig. 3b). The least-squares fit is also in surprisingly good correspondence with the relationship derived from daily data of five different stations in the USA by Collares-Pereira and Rabl (1979).

For every hour between sunrise and sunset, Equation (3) together with measured global radiation is used to obtain the diffuse radiation at climate station B, which is then subtracted from global radiation to yield the direct solar radiation at this site, *I*_s. Topographic shading is calculated for every hour and for each gridcell from the path of the sun and the effective horizon. If the climate station is shaded by surrounding topography, any measured global radiation is assumed diffuse.

3.1.1. Direct solar radiation

Following Ohta (1994) and Fierz and others (1997) for every hour and each gridcell, direct radiation *I* is obtained from

$$I = \frac{I_{\rm s}}{I_{\rm sc}} I_{\rm c},\tag{4}$$

where the subscript s refers to the location of the climate station and c denotes clear-sky conditions. I_s is obtained from Equation (3), and $I_c = I_{sc}$ at the location of station B. The ratio I_s/I_{sc} accounts for the deviation from clear-sky conditions, expressing the reduction of potential clear-sky direct solar radiation mainly due to clouds. It approaches unity under clear-sky conditions and tends to decrease with increasing cloudiness as direct radiation I_s decreases. The ratio I_s/I_{sc} obtained at the climate station is assumed to be spatially constant. Potential direct solar radiation I_c is calculated for each gridcell taking into account the combined effects of slope and aspect angles of each gridcell (Garnier and Ohmura, 1968):

$$I_{\rm c} = I_0 \left(\frac{R_{\rm m}}{R}\right)^2 \psi_{\rm a}^{\frac{P}{P_0 \cos Z}} \times \left[\cos\beta\cos Z + \sin\beta\sin Z\cos(\varphi_{\rm sun} - \varphi_{\rm slope})\right], \quad (5)$$

where ψ_a is the atmospheric clear-sky transmissivity, *P* is the atmospheric pressure, P_0 is the mean atmospheric pressure at sea level, Z is the zenith angle, β is the gridcell slope angle, φ_{sun} is the solar azimuth angle and φ_{slope} is the slope azimuth angle. An average value of 0.75 was derived for clear-sky transmissivity from the measurements of global radiation and an assumed fraction of diffuse radiation of global radiation of 15% (Konzelmann and Ohmura, 1995). Variations in transmissivity ψ_a are not considered since values of I_c are subsequently scaled by measurements, and hence the resulting error is considered negligible. The P/P_0 ratio accounts for the effect of altitude on direct radiation, and $\cos Z$ in the exponent expresses the variation of the path length with sun altitude. If the gridcell calculated is topographically shaded, direct radiation is set to zero. Potential direct radiation is computed at 10 min intervals, and hourly means are applied in Equation (4).

If the climate station is shaded by surrounding topography, Equation (4) is not applicable since the ratio I_s/I_{sc} is no longer defined, as potential direct solar radiation at the climate station, I_{sc} , is zero. This case must be considered since the climate station is located on a valley glacier, and thus potentially subject to topographic shading, while other parts of the glacier may still be in the sunshine. For these gridcells the last ratio that could be obtained before the climate-station gridcell became shaded is applied. Thus, cloud conditions are assumed to remain constant until a new ratio I_s/I_{sc} can be determined at the climate station, usually the next morning. The error introduced by this assumption is considered small, as topographic shading of the climate station will only occur during times of low sun altitude, when direct radiation tends to be small.

3.1.2. Diffuse radiation

Diffuse radiation is assumed to be isotropic, although clearsky diffuse radiation is significantly anisotropic (Kondrat'ev, 1969). However, the error is considered negligible, because under clear-sky conditions the diffuse fraction of global radiation is small (10–20%) and under overcast conditions, when the diffuse component is dominant, the diffuse radiation is almost isotropic with the topographic screening by surrounding topography. Total diffuse radiation *D* is computed by means of a sky-view-factor relationship taking into account the fraction of the hemisphere that is obstructed by surrounding topography and by considering additional diffuse radiation reflected from adjacent slopes:

$$D = D_0 F + \alpha_{\rm m} G(1 - F), \tag{6}$$

where the first term refers to sky radiation and the second term to terrain radiation. D_0 is diffuse radiation from an unobstructed sky, α_m is the mean albedo of the surrounding terrain, *G* is global radiation and *F* is the sky-view factor defined by (Oke, 1987)

$$F = \frac{1}{2\pi} \int_0^{2\pi} \cos^2 \gamma \, \mathrm{d}\varphi, \tag{7}$$

where γ is the elevation angle of the horizon, which is integrated over the azimuth φ , here in steps of 15°. Values range between zero, indicating a completely obscured sky, and unity, referring to an unobscured sky. The expression includes the variation of radiant intensity with the direction of radiation. Equation (7) assumes a horizontal surface, although strictly speaking the angle between the normal to the inclined surface and the direction of radiation should be used. However, the error due to this assumption is considered small. As diffuse radiation at the climate station is already affected by surrounding topography, the diffuse radiation of an unobscured sky, D_0 , is calculated for the location of the climate station from Equation (6) and then assumed constant in space. The mean albedo $\alpha_{\rm m}$ will vary with time, mainly due to the progressive melt of the snow cover on the surrounding rock walls and on the glacier. Therefore, $\alpha_{\rm m}$ is obtained for every hour as the arithmetic mean of the modelled albedo of all gridcells of the entire drainage basin.

3.2. Albedo

Snow and ice albedo are treated individually. Among the large variety of albedo parameterizations (Brock and others, 2000a), a simple but widely used approach to account for the tendency of snow albedo to decrease with time is the formulation suggested by USACE (1956). Snow albedo is related to the number of days since the last significant snowfall. In the present study, this approach yielded large discrepancies between measured and modelled albedo, in particular during prolonged periods without snowfall (Fig. 4). In the present study, a new approach is suggested deriving hourly snow albedo from the albedo of the preceding hour. During snowfall, the preceding albedo is increased as a function of snowfall amounts. In the absence of snowfall, snow albedo is lowered as a function of the number of days after snowfall and air temperature. The former is taken as a surrogate to account for the effects of grain-size growth due to snow ripening and increasing impurity content with time. The lowering is assumed to be highest immediately after the snowfall event, decreasing exponentially with time. The inclusion of air temperature accounts for the acceleration of these processes as meltwater production is enhanced. Based on these considerations, the following empirical parameterization was derived:

$$\alpha_{t_2} = \begin{cases} \alpha_{t_1} - a_1 [\ln(T+1)] e^{(a_2 \sqrt{n_d})} &: n_d > 0 \text{ and } T > 0\\ \alpha_{t_1} - a_3 e^{(a_2 \sqrt{n_d})} &: n_d > 0 \text{ and } T < 0\\ \alpha_{t_1} + a_4 P_s &: n_d = 0 \end{cases}$$
(8)

where *T* is hourly air temperature (°C), P_s is snow precipitation (mm h⁻¹), n_d is the number of days since snowfall and a_1-a_4 are coefficients obtained by calibration.

To account for cloud effects, snow albedo obtained by Equation (8) is further modified using the ratio of measured

global radiation to top-of-atmosphere radiation G/I_{ToA} as an index for cloudiness. We incorporate the empirical relationship between the percentage change in albedo between two successive hourly measurements and the corresponding change in the ratio of G/I_{ToA} as derived from an investigation of detailed albedo measurements on Storglaciären (Jonsell and others, 2003), and snow albedo is obtained by

$$\alpha = \alpha_{t_2} + \alpha_{t_2} b[(G/I_{\text{TOA}})_{t_2} - (G/I_{\text{TOA}})_{t_1}]/100, \qquad (9)$$

where b = -20.7 and radiation is in W m⁻². In case of snowfall, albedo is delimited to a maximum of 0.9. Snow albedo turned out to drop too rapidly, when hours of snowfall and no snowfall alternated, as the terms subtracted in Equation (8) are largest directly after snowfall events. Therefore, if calculated albedo drops below the value calculated for the time-step before the last snowfall, albedo and n_d are set to their values immediately before the snowfall. Albedo will then continue to decrease at the same rate as if no snowfall had occurred. Hence, it is assumed that the new snow has melted.

A reduction in snow albedo when the snowpack becomes shallow is not included in the model. This common assumption was found to be unsubstantiated when tested with extensive field measurements on Haut Glacier d'Arolla, Switzerland (Brock and others, 2000a). In the firn area, when the winter snow has melted, the albedo is lowered once by 0.03 to account for the generally lower albedo of the previous year's summer surface. Firn albedo is then treated as snow albedo. The value of 0.03 was obtained on average from a few instantaneous albedo measurements with portable equipment over snow and firn surfaces in the firn area. The coefficients a_1-a_4 were fitted from the albedo measurements at station C in 1994 ($a_1 = 0.005$, $a_2 = -1.05$, $a_3 = 0.0005$, $a_4 = 0.02 \text{ h mm}^{-1}$). To avoid erroneous calibration due to possible effects of the zenith angle (Arendt, 1999) which are not accounted for in our parameterization, or due to measurement inaccuracies caused by surface slope effects (Jonsell and others, 2003), modelled hourly albedos were compiled into daily values from daily averaged global and shortwave reflected radiation prior to comparison with measured albedo. Measured and modelled daily snow albedo for station C in 1994 and station B in 1993 are compared in Figure 4. The model using Equations (8) and (9) performed significantly better than the routine by USACE (1956).

The albedos of ice at stations A and B varied little and did not show a significant decrease with time, as also found on other glaciers by Cutler and Munro (1996) and Brock and others (2000a). Any temporal variation in ice albedo is therefore neglected, and an albedo of 0.355 is assumed at the climate station, as obtained on average from the data available (Jonsell and others, 2003). To account for the tendency of debris to accumulate towards the glacier tongue, this value is extrapolated using an assumed increase of $3\% (100 \text{ m})^{-1}$ with increasing elevation, resulting in modelled ice albedo on Storglaciären of 0.33–0.38.

3.3. Longwave radiation

3.3.1. Longwave outgoing radiation Longwave outgoing radiation $L \uparrow$ is approximated by

$$L \uparrow = \varepsilon \sigma T^4, \tag{10}$$

where ε is the emissivity of the surface (assumed to be 1), σ is the Stefan–Boltzmann constant and *T* is the absolute



Fig. 4. Measured and simulated daily snow albedo at stations B and C using the parameterization defined by Equations (8) and (9) and the formulation by USACE (1956): $\alpha = a_0 + a_1 \exp(a_2 n_d)$, where $a_0 = 0.45$, $a_1 = 0.44$, $a_2 = -0.1$ and n_d is the number of days after snowfall.

temperature (K) of the emitting surface. The surface temperature is assumed to be zero if the energy available for melt is positive. If melt turns negative, the surface temperature is lowered iteratively by steps of 0.25 K until the computed melt for the time-step and the gridcell considered becomes zero (Escher-Vetter, 1985; Braithwaite and others, 1998). An iterative loop is needed because a lower surface temperature also affects outgoing longwave radiation, the turbulent heat fluxes and the heat transport supplied by rain.

3.3.2. Longwave incoming radiation

In complex topography, longwave sky radiation is reduced because part of the sky is obstructed, while additional radiation is received from surrounding slopes. Sky and terrain radiation are calculated individually. Longwave terrain irradiance L_t^{\downarrow} is calculated using the parameterization suggested by Plüss and Ohmura (1997):

$$L_{\rm t}^{\downarrow} = (1 - F)\pi (L_{\rm b} + aT_{\rm a} + bT_{\rm s}), \tag{11}$$

where *F* is the sky view factor (Equation (7)), *T*_a is the nearsurface air temperature (°C), *T*_s is the temperature of the emitting surface (°C) and *a* and *b* are constants $(a = 0.77 \text{ W m}^{-2} \text{ sr}^{-1}, b = 0.54 \text{ W m}^{-2} \text{ sr}^{-1})$. The constant $L_{b} = 100.2 \text{ W m}^{-2} \text{ sr}^{-1}$ is the emitted radiance of a 0°C black body. The parameterization was derived in a snowcovered alpine environment using a narrowband radiation model (LOWTRAN) and includes the effects of the air between the emitting surface and the receiving surface. Longwave sky irradiance L_{s}^{\downarrow} is obtained from

$$L_{\rm s}^{\downarrow} = L_0 F \tag{12}$$

with L_0 the sky irradiance from an unobstructed sky. L_0 is obtained for the location of the climate station involving two steps. First, longwave incoming radiation is determined as a residual in the radiation balance at the climate station using the measurements of net radiation, global radiation and reflected shortwave radiation and the computed value of outgoing longwave radiation. Radiation obtained in this way is the sum of sky and terrain radiation ($L_s^{\downarrow} + L_t^{\downarrow}$). Therefore, secondly, sky radiation from an unobscured sky, L_0 , is calculated from Equations (11) and (12) for the location of the climate station. This value is assumed invariant in space and used to compute sky radiation of the entire grid. Total longwave irradiance at each grid element is the sum of L_s^{\downarrow} and L_t^{\downarrow} .

Deriving longwave incoming radiation from the radiation measurements merits some comment. Halldin and Lindroth (1992) showed that a large variation can be expected by comparing different types of net radiometers. In the present study, a Funk-type net radiometer (Kondrat'ev, 1969) was used. Müller and Ohmura (1993) and Konzelmann and Ohmura (1995) showed that this type of instrument is subject to a substantial underestimation of net radiation at an increasing rate with rising global radiation. They suggested a correction formula relating the error to global radiation. Net radiation corrected in this way for sites in Greenland and Switzerland agreed well with net radiation derived from measurements of the individual radiation components. Therefore, the net radiation data after correction are considered sufficiently accurate to allow for the procedure adopted here.

3.4. Turbulent heat fluxes

The turbulent heat fluxes are calculated from the bulk aerodynamic method, assuming the sensible- and latentheat flux to be proportional to air temperature T_z , wind speed u_z and vapour pressure e_z at height z above the surface:

$$Q_{\rm H} = \rho c_{\rm p} \frac{k^2}{\left[\ln \left(\frac{z}{z_{0w}} \right) - \Psi_{\rm M} \left(\frac{z}{L} \right) \right] \left[\ln \left(\frac{z}{z_{0T}} \right) - \Psi_{\rm H} \left(\frac{z}{L} \right) \right]} u_z (T_z - T_0)$$
(13)

$$Q_{\rm E} = L_{\rm v} \frac{0.623\rho_0}{P_0} \frac{k^2}{\left[\ln\left(\frac{z}{z_{0w}}\right) - \Psi_{\rm M}\left(\frac{z}{L}\right)\right] \left[\ln\left(\frac{z}{z_{0e}}\right) - \Psi_{\rm E}\left(\frac{z}{L}\right)\right]} u_z(e_z - e_0),$$
(14)

where ρ is the air density, the subscript 0 refers to the mean atmospheric pressure at sea level, P_0 , c_p is the specific heat capacity of air, k is von Kármán's constant (0.4), T_0 is the surface temperature, e_0 is the vapour pressure of the surface, z_{0w} , z_{0T} and z_{0e} are the roughness lengths for logarithmic profiles of wind speed, temperature and water vapour, respectively, Ψ_M , Ψ_H and Ψ_E are the stability functions, L is the Monin–Obukhov length, and L_v is the latent heat of evaporation $(2.514 \times 10^6 \text{ J kg}^{-1})$ or sublimation (2.849 $\times 10^{6}$ J kg⁻¹) as appropriate. Which one is applied is controlled by the direction of the latent-heat flux and the surface temperature. If the latent-heat flux is positive, the surface is expected to experience condensation in case of a melting surface and resublimation (a phase change from vapour to ice) in case of subfreezing surface temperatures. For negative latent-heat fluxes, sublimation is assumed, no matter what the surface temperatures.

Based on Forrer and Rotach (1997), for the stable case we apply the non-linear stability functions by Beljaars and Holtslag (1991):

$$-\Psi_{\rm M} = \frac{az}{L} + b\left(\frac{z}{L} - \frac{c}{d}\right)\exp\left(-d\frac{z}{L}\right) + \frac{bc}{d}$$
(15)
$$-\Psi_{\rm H} = \left(1 + \frac{2az}{3L}\right)^{1.5} + b\left(\frac{z}{L} - \frac{c}{d}\right)\exp\left(-d\frac{z}{L}\right) + \frac{bc}{d} - 1.$$
(16)

We assume $\Psi_{\rm E} = \Psi_{\rm H}$. For the far less frequent unstable case we apply the commonly used Businger–Dyer expressions (see Paulson, 1970). The Monin–Obukhov length *L* is computed from

$$L = \frac{\rho c_{\rm p} u_*^3 T_z}{kg Q_{\rm H}} \tag{17}$$

$$u_* = \frac{ku_z}{\ln\left(\frac{z}{z_{0w}}\right) - \Psi_{\mathsf{M}}},\tag{18}$$

where u_* is the friction velocity and T_z is in Kelvin. Since the calculation of *L* requires a priori knowledge of Q_H and u_* , *L* is determined by iteration for the location of station B and for every time-step following the procedure outlined by Munro (1990). Stability functions determined in this way are then assumed spatially invariant across the glacier.

Detailed profile measurements of temperature, wind speed and water vapour were not available to determine the roughness length z_{0w} . Reported roughness lengths of ice and snow surfaces cover a range of orders of magnitude (for summary see Moore, 1983; Braithwaite, 1995) and are expected to vary in space and time (Holmgren, 1971; Greuell and Konzelmann, 1994; Plüss and Mazzoni, 1994). A general pattern as to whether or not z_{0w} values over ice are higher than over snow does not emerge in the literature. Hence, obtaining roughness lengths from the literature is problematic. On Storglaciären over ice, z_{0w} values of 2.7 mm (Hock and Holmgren, 1996) and 0.1 mm (Grainger and Lister, 1966) have been reported. Energy-balance studies have shown a large sensitivity of results to assumed roughness lengths (Morris, 1982; Harding and others, 1989; Hock and Holmgren, 1996). Based on these considerations, in our model the roughness lengths are treated as model parameters, and hence chosen to yield optimal agreement between simulations and observations considering both melt and discharge. The roughness lengths for ice and snow were assumed equal and also constant in time during both melt seasons ($z_{0w} = 10 \text{ mm}$). The roughness lengths of temperature and vapour pressure were assumed to be two orders of magnitude smaller than that of wind speed according to Holmgren (1971) and Ambach (1986). When interpreting relative contributions of energybalance components, it must be borne in mind that the procedure of tuning roughness lengths entails that any errors concerning components other than the turbulent heat fluxes are lumped into the roughness lengths, thus affecting modelled energy partitioning. Nevertheless, considering the uncertainties with respect to the computation of the turbulent fluxes in the glacier environment (Hock, 2005), and specifically to the specification of roughness lengths and the as yet infant stage of available attempts at their temporal and spatial extrapolation, the method adopted here is considered to suffice in place of a more sophisticated scheme, but should be subject to future model improvement as more datasets become available and new generally applicable parameterizations evolve. Determination of the roughness lengths (or exchange coefficients) from closure of the seasonal energy budget has been adopted by various authors (e.g. Oerlemans, 2000; Konya and others, 2004).

3.5. Ground heat flux and rain energy

A heat flux into the snow cover and the modelling of the formation of superimposed ice are neglected because snow temperature measurements at station B indicated that the winter cold content of the snow cover had been eliminated by the time the simulation began. On Storglaciären a heat transport into the ice is to be expected, because, although mostly temperate, a cold surface layer exists in the ablation area (Pettersson and others, 2003). Temperature-depth profiles in 1994 and during a micrometeorological experiment in the 1970s (Holmgren, unpublished information) indicated that the ice heat flux was approximately 0-5 W m⁻² after the ice had been exposed (Hock and Holmgren, 1996). The amount is small but, because the direction of the flux is constant, neglect of the flux would introduce a systematic error. Therefore, for any ice-exposed gridcell, the ground heat flux is crudely approximated by assuming that it drops from $5 \text{ W} \text{ m}^{-2}$ to $0 \text{ W} \text{ m}^{-2}$ between 1 July and 1 September, with linear interpolation in between. The model neglects the heat energy required to warm the surface up to melting point following periods of negative energy balance. However, the cooling process is not restricted to the surface but rather extends over a volume, whereas during the reverse process it is sufficient to raise the temperature of the surface to 0°C for melt to occur. Subsurface layers are then effectively heated by the latent heat released from the refreezing of percolating surface meltwater. Consequently, the processes of cooling and warming-up of the surface are asymmetrical, and only part of the integrated negative energy balance needs to be compensated for before melt will occur.

The energy supplied by rain $Q_{\rm R}$ is calculated by

$$Q_{\rm R} = \rho_{\rm w} c_{\rm w} R (T_{\rm r} - T_{\rm s}), \qquad (19)$$

where ρ_w is the density of water, c_w is the specific heat of water (4.18 kJ kg⁻¹ K⁻¹), *R* is the rainfall rate and T_r and T_s are the temperatures of rain (assumed to be equal to air temperature) and the surface, respectively. T_r becomes equal to T_s before rain leaves the glacier surface.

3.6. Accumulation

Any snow precipitation is accumulated as a snow cover on the glacier. The aggregational state of each precipitation is determined according to a fixed air-temperature divider of 1.5°C (Rohrer, 1989). A mixture of rain and snow is assumed for a transition zone ranging from 1 K above and 1 K below the threshold temperature. Within this temperature range, the snow and rain percentages of total precipitation are obtained from linear interpolation. Redistribution of the original snowfall by wind transport or avalanches is not considered.

3.7. Initial snow cover

The initial snow water equivalent on the glacier was determined from the winter balance survey and ablation stake readings. The winter balance is determined as part of the annual mass-balance programme (Holmlund and Jansson, 1999) by manual probing in a 100×100 m grid across the glacier and several density pits. The amount of melt between the survey and the starting day of simulation was determined by means of approximately 50 ablation stakes and was then subtracted from the winter balance. The snow water equivalent was interpolated to each glacier gridcell using ordinary kriging interpolation (Hock and Jensen, 1999). Initial snow cover on the surrounding valley slopes is difficult to quantify because measurements are inhibited by the steepness of the terrain. In 1994, the surrounding slopes and the glacier forefield were mostly snow-free at the beginning of the simulation, so any snow cover outside the glacier was neglected. In 1993 the areal snow distribution in the forefield was estimated from snow surveys. On the valley slopes snow was distributed to the slope gridcells as a function of elevation, slope and curvature of the terrain following a procedure discussed in Blöschl and others (1991).

4. RESULTS AND DISCUSSION

The energy balance was calculated for each gridcell of the catchment for the periods 7 June–17 September 1993 and 5 July–6 September 1994. Simulated results were compared to cumulative ablation at the ablation stakes on the glacier and to observed patterns of snow-line retreat. In order to allow for additional verification by means of observed discharge records, the melt model was coupled to a discharge routine described in detail by Hock and Noetzli (1997). The model routes areal melt and precipitation through the glacier by means of three parallel linear reservoirs corresponding to the different storage properties of firn, snow and ice using storage constants of 350, 30 and 16 hours, respectively.

4.1. Discharge

Discharge data were available for the periods 9 July– 17 August 1993 and 11 July–6 September 1994. The discharge pattern in 1993 was dominated by rain-induced discharge peaks, whereas melt-induced discharge cycles prevailed during the 1994 melt season. Despite the different weather character, simulated and observed discharge hydrographs for the two years are in very good agreement (Figs 5 and 6). The model performs well with respect to both the diurnal and the seasonal discharge fluctuations. Expressing the agreement in terms of the R^2 efficiency criterion by Nash and Sutcliffe (1970), values of 0.84 and 0.86 are obtained for the periods considered in 1993 and 1994, respectively.

4.2. Cumulative ablation

Simulated ablation was cumulated for the locations of the ablation stakes over the periods 7 June–17 September 1993 and 5 July–25 August 1994, and compared to measured values (Fig. 7). The results for 1994 show a tendency for melt to be overestimated by the model. In 1993 the model tends to slightly under-predict high ablation amounts and overestimates low ablation.

4.3. Snow-line retreat

Accurate predictions of snow-line retreat are a decisive factor in melt modelling, because the snow-line separates two areas of appreciably different albedo. The observed and modelled patterns of snow-line retreat for the 1994 melt season are illustrated in Figure 8. Results indicate good agreement between observations and simulations, although in the first part of the melt season the model tends to underestimate the areas where the ice is exposed, whereas later in the season this tendency is reversed. The mismatch at the glacier margins later in the season may be associated with the uncertainties involved in determining the initial snow water equivalent. Snow probings showed a tendency for snow depths to increase abruptly at the margins of the glacier tongue. This increase, however, cannot be represented by the applied interpolation scheme, as data were not available in these areas, so the initial snow cover was probably underestimated.

4.4. Energy-balance components

The quality of the radiation model was evaluated by comparing modelled and measured global and net radiation



Fig. 5. Simulated melt averaged over the glacier, $M \pmod{h^{-1}}$, hourly data of air temperature T (°C) and precipitation $P \pmod{h^{-1}}$ at station B, and simulated and measured hourly discharge $Q \pmod{s^{-1}}$ (black lines) of Storglaciären, 7 June–27 August 1993; and cumulated discharge Q_{cum} (m³) (grey lines) over the period of discharge observations, 9 July–17 August.

at stations A and C. Results show fairly good agreement between measurements and simulations (Fig. 9). Discrepancies in global radiation are mainly associated with errors in the modelling of the timing of topographic shading. If the climate station is in sunlight (shade), but the model assumes shading (sunlight), global radiation will be underestimated (overestimated). The absence of systematic deviations in the net radiation plots promotes confidence in the accuracy of the new albedo parameterization, although albedo underestimation at one time might be compensated by overestimation at another time. On average, modelled net shortwave radiation fluxes agree well with those measured at the weather stations.

On average, net radiation only contributed roughly 40% and 60% of the melt energy in 1993 and 1994, respectively, the remaining energy mainly being supplied by the sensible-heat flux (Table 1). As expected, direct radiation exhibited the largest spatial variability, reflecting the effects of topographic shading, slope and aspect (Fig. 10). The spatial variability of diffuse radiation was small, with highest values occurring on steep slopes. The differences between melt and ablation were small (Table 1), indicating that the mass changes by (re)sublimation were negligible compared to melt. On average, in 1993 the glacier experienced condensation, while in 1994 the latent-heat flux was negligible. In contrast to 1993, in 1994 evaporation prevailed in the higher parts of the glacier, whereas condensation was



Fig. 6. Simulated melt averaged over the glacier, $M \pmod{h^{-1}}$, hourly data of air temperature T (°C) and precipitation $P \pmod{h^{-1}}$ at station B, and simulated and measured hourly discharge $Q \pmod{s^{-1}}$ of Storglaciären, 5 July–6 September 1994; and cumulated discharge Q_{cum} (m³) (grey lines) from 11 July, when the measured discharge record started.



Fig. 7. Measured vs simulated cumulative ablation (m w.e.) at the ablation stakes on Storglaciären for the periods 7 June–17 September 1993 and 5 July–25 August 1994.

dominant at lower elevations. The large relative contribution of the latent-heat flux in 1993 appears high compared to the results obtained from most single location studies on valley glaciers in the Alps (e.g. Hock, 2005). However, in particular in more maritime areas, considerable condensation has been found on average (e.g. on Worthington Glacier, Alaska, USA (47 W m⁻²; Streten and Wendler, 1967), Ivory Glacier, New Zealand (23 W m⁻²; Hay and Fitzharris, 1988), and Peyto Glacier, Canada (15 W m⁻²; Föhn, 1973)). The difference in the relative contributions on Storglaciären between the two years is attributed to the difference in prevailing weather character. In contrast to 1994, the melt season in 1993 was subject to frequent rain and fog. In addition, the simulations extend over different time periods, and the relative importance of the energybalance components may change considerably during the melt season (e.g. Orvig, 1954; Holmgren, 1971; Wendler and Weller, 1974).

4.5. Parameter sensitivity

The sensitivity of results to the choice of various parameters and parameterization schemes was analyzed in order to assess the robustness of the model.

4.5.1. Turbulent heat fluxes

As the sensible-heat flux contributed a considerable amount to the energy available for melt on Storglaciären, the sensitivity of the results to assumptions about roughness lengths was investigated. Figure 11 shows simulated discharge for 1994 for a lowering of z_{0w} from the optimized value of 10 mm to 0.1 mm as reported for ice on Storglaciären by Grainger and Lister (1966). The average sensible-heat flux is reduced from 36 to $15 \text{ W} \text{ m}^{-2}$ and discharge is considerably underestimated, yielding $R^2 = 0.5$. Furthermore Figure 11 displays a model run neglecting a correction for atmospheric stability ($\Psi = 0$). Although, strictly speaking, a stability correction should be included since stable stratification is common over melting snow and ice, several studies have concluded that the turbulent fluxes tend to be underestimated when correction formulas in terms of the bulk Richardson number or the Monin-Obukhov length are applied over sloping glacier surfaces, in particular under strong stability (e.g. Harding and others, 1989; Konzelmann and Braithwaite, 1995; Van den Broeke, 1996; Forrer and Rotach, 1997; Martin and Lejeune, 1998). Hence, various studies have neglected stability correction schemes in their energy-balance calculations (e.g. Hock and Holmgren, 1996; Oerlemans, 2000;



Fig. 8. Observed and simulated patterns of snow-line retreat on Storglaciären for the 1994 melt season. The black areas are those where the ice or firn is exposed.

Konya and others, 2004). Our results based on neglect of stability correction yield an improved simulation of glacier runoff ($R^2 = 0.92$) mainly during the period of prolonged high air temperatures when runoff tended to be underestimated in the run including the stability correction. This finding may provide additional evidence that existing stability correction schemes underestimate the turbulent fluxes in the glacier environment. An assumption that the roughness length of ice exceeds that of snow did not lead to improved results, probably because the surface roughness of snow will rapidly increase as melt proceeds. Computing the roughness lengths z_{0T} and z_{0e} using the surface renewal model of Andreas (1987), as, for example, done by Munro (1990) and Van den Broeke (1996), considerably underestimated discharge, especially during the warm, calm period in mid-July 1994. Generally speaking, results indicate that in regions where the turbulent fluxes play a significant role in the energy balance, the roughness lengths are sensitive parameters, emphasizing the importance of accurate estimates of the roughness lengths for melt modelling.



Fig. 9. Measured vs simulated hourly global radiation and net radiation at stations A and C (Fig. 1) for the data in 1994.

4.5.2. Ice albedo

In various studies, albedo has been recognized as a key factor for the energy balance of a glacier (e.g. Van de Wal and others, 1992). In our model, temporal variations in the albedo of ice-exposed gridcells are neglected, and spatial variations are only considered by an elevation dependency. Two sensitivity runs were performed, increasing and decreasing ice albedo by 0.05, thus assigning it 0.305 and 0.405. The results indicate little impact within the range considered, yielding almost identical hydrographs. Concerning the spatially averaged shortwave radiation balance, the overall effect is dampened, as larger parts of the glacier are snow-covered and not affected by variations in ice albedo. The sensitivity to albedo variations is also dampened by the large relative contribution of the turbulent fluxes to melt energy.

4.5.3. Separation of direct and diffuse radiation

The function splitting global radiation into the direct and diffuse components obtained from all available data (Equation (3)) differed significantly from that derived only for the May data (Fig. 3c). Therefore, the latter function was applied in a sensitivity run for comparison. Discharge simulations were almost identical, yielding the R^2 value as before. Spatially averaged melt energy remained the same, although the fractions of direct and diffuse radiation were altered by roughly 10%.

5. CONCLUDING REMARKS

A distributed surface energy-balance model has been developed, combining existing and new approaches to the spatial modelling of ice- and snowmelt in rugged terrain on an hourly time-scale. The model is forced by near-surface data of air temperature, humidity, wind speed and global radiation collected at one meteorological station considered representative of the area calculated. In addition, data on reflected shortwave radiation and net radiation were used to derive longwave incoming radiation, which could alternatively be obtained from measurements or from a parameterization based on cloud data. The model was applied



Fig. 10. Direct, diffuse, global and net radiation ($W m^{-2}$) and cumulative simulated melt (cm) of Storglaciären averaged over the period 7 June–17 September 1993.

to Storglaciären to simulate hourly melt for each grid element of a DEM for two melt seasons. Modelled melt rates varied substantially across the glacier, mainly due to the effects of surrounding topography on direct solar radiation. The contribution of the turbulent fluxes to the energy available for melt was found to be remarkably high, with roughly 60% and 40% in 1993 and 1994, respectively, resembling the energy partitioning generally found in maritime climates.

In general, simulations of melt rates, patterns of snow-line retreat and proglacial discharge corresponded well with observations. In particular, the model performed remarkably well with respect to the simulation of the melt-induced diurnal discharge fluctuations typical of glacial regimes. Such diurnal variability is generally not captured by models based on simpler temperature-index methods (Hock, 2003). The energy-balance model may be used to provide the meltwater input for runoff modelling in any snow- or icecovered terrain, particularly when the daily discharge cycles are to be simulated, or for any other purposes requiring the prediction of melt rates with high spatial or temporal resolution.

Sensitivity studies indicated the robustness of the model. However, results were sensitive to the choice of roughness lengths within the range of values reported for ice and snow surfaces in the literature, emphasizing the importance of accurate estimates of the roughness parameters in case the turbulent heat fluxes are substantial contributors to melt. Roughness lengths are difficult to obtain and their temporal and spatial variability poses an additional problem, thus rendering the roughness lengths a tuning parameter. Further research should be directed towards the parameterization of roughness lengths over snow and ice surfaces and their spatial and temporal variability, as well as to more realistic extrapolation of wind speed across glaciers. In addition, the new snow albedo scheme needs further scrutiny using other datasets.

The model has successfully been tested in other climate settings (e.g. in Antarctica (Braun and Hock, 2004) and on a tropical glacier (Sicart, 2002)). Our model intends to provide a tool for sensitivity tests and to quantify the response of glacier melt and discharge to predicted climate changes. Although temperature-index models have been used for such purposes (e.g. Braithwaite and Zhang, 2000) and are more practical due to lower data requirements, the stability of calibration factors under a different climate remains uncertain, so more physically based methods are preferable if the necessary data are available.

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Period		I	D	S	L↓	L↑	$Q_{\rm N}$	$Q_{\rm H}$	$Q_{\rm L}$	Q_{R}	$Q_{ m G}$	Q_{M}	М	A
7 June-17 Sept. 1993	Mean	66	81	37	277	-297	18	20	8	2	-1	-48	1.27	1.28
	Min.	11	79	18	274	-295	1	9	0	1	0	-24	0.64	0.65
	Max.	92	90	69	287	-299	46	26	13	2	-2	-79	2.10	2.11
5 July–6 Sept. 1994	Mean	89	80	77	271	-299	49	36	0	1	-1	-86	1.42	1.43
	Min.	9	79	28	267	-297	5	22	-11	1	0	-31	0.51	0.53
	Max.	129	86	115	286	-301	85	48	6	1	-2	-134	2.22	2.23

Table 1. Energy-balance components (W m^{-2}) averaged over the glacier and the entire period of computation in 1993 and 1994

Notes: I is direct solar radiation, *D* diffuse solar radiation, *S* shortwave radiation balance, $L\downarrow$ and $L\uparrow$ incoming and outgoing longwave radiation, respectively, Q_N net radiation, Q_H the sensible-heat flux, Q_L the latent-heat flux, Q_R the heat flux supplied by rain, Q_G the ice heat flux, Q_M the energy available for melt, *M* melt (m w.e.) and *A* ablation (m w.e.). The spatial variability is given in terms of minimum and maximum time averages found across the glacier.



Fig. 11. Hourly measured and simulated discharge Q (m³ s⁻¹) of Storglaciären, 11 July–6 September, 1994, for two model sensitivity runs: reducing z_{0w} from 10 mm to 0.1 mm; and neglecting a correction for atmospheric stability and applying optimized $z_{0w} = 8 \text{ mm}$ and $z_{0T} = z_{0e} = 0.008 \text{ mm}$.

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REFERENCES

- Ambach, W. 1986. Nomographs for the determination of meltwater from snow and ice surfaces. *Berichte des naturwissenschaftlichmedizinischen Vereins in Innsbruck*, 73, 7–15.
- Andreas, E.L. 1987. A theory for the scalar roughness and the scalar transfer coefficients over snow and sea ice. *Boundary-Layer Meteorol.*, 38(1–2), 159–184.
- Arendt, A. 1999. Approaches to modelling the surface albedo of a high Arctic glacier. *Geogr. Ann.*, **81A**(4), 477–487.
- Arnold, N.S., I.C. Willis, M.J. Sharp, K.S. Richards and W.J. Lawson. 1996. A distributed surface energy-balance model for a small valley glacier. I. Development and testing for Haut Glacier d'Arolla, Valais, Switzerland. J. Glaciol., 42(140), 77–89.
- Beljaars, A. and A. Holtslag. 1991. Flux parameterization over land surface for atmospheric models. J. Appl. Meteorol., 30(3), 327–341.
- Blöschl, G., R. Kirnbauer and D. Gutknecht. 1991. Distributed snowmelt simulations in an Alpine catchment. I. Model evaluation on the basis of snow cover patterns. *Water Resour. Res.*, 27(12), 3171–3179.
- Braithwaite, R.J. 1995. Aerodynamic stability and turbulent sensible-heat flux over a melting ice surface, the Greenland ice sheet. J. Glaciol., 41(139), 562–571.
- Braithwaite, R.J. and Y. Zhang. 2000. Sensitivity of mass balance of five Swiss glaciers to temperature changes assessed by tuning a degree-day model. *J. Glaciol.*, **46**(152), 7–14.
- Braithwaite, R.J., T. Konzelmann, C. Marty and O.B. Olesen. 1998. Reconnaissance study of glacier energy balance in North Greenland, 1993–94. J. Glaciol., 44(147), 239–247.
- Braun, M. and R. Hock. 2004. Spatially distributed surface energy balance and ablation modelling on the ice cap of King George Island (Antarctica). *Global Planet. Change*, **42**(1), 45–58.
- Brock, B.W., I.C. Willis and M.J. Sharp. 2000a. Measurement and parameterization of albedo variations at Haut Glacier d'Arolla, Switzerland. J. Glaciol., 46(155), 675–688.
- Brock, B.W., I.C. Willis, M.J. Sharp and N.S. Arnold. 2000b. Modelling seasonal and spatial variations in the surface energy

balance of Haut Glacier d'Arolla, Switzerland. *Ann. Glaciol.*, **31**, 53–62.

- Collares-Pereira, M. and A. Rabl. 1979. The average distribution of solar radiation correlations between diffuse and hemispherical and between daily and hourly insolation values. *Solar Energy*, **22**(2), 155–164.
- Cutler, P.M. and D.S. Munro. 1996. Visible and near-infrared reflectivity during the ablation period on Peyto Glacier, Alberta, Canada. *J. Glaciol.*, **42**(141), 333–340.
- Dozier, J. 1980. A clear-sky spectral solar radiation model for snowcovered mountainous terrain. *Water Resour. Res.*, **16**(4), 709–718.
- Escher-Vetter, H. 1985. Energy balance calculations for the ablation period 1982 at Vernagtferner, Oetztal Alps. *Ann. Glaciol.*, **6**, 158–160.
- Escher-Vetter, H. 2000. Modelling meltwater production with a distributed energy balance method and runoff using a linear reservoir approach: results from Vernagtferner, Oetztal Alps, for the ablation seasons 1992 to 1995. *Z. Gletscherkd. Glazialgeol.*, **36**, 119–150.
- Fierz, C., C. Plüss and E. Martin. 1997. Modelling the snow cover in a complex Alpine topography. *Ann. Glaciol.*, **25**, 312–316.
- Föhn, P.M.B. 1973. Short-term snow melt and ablation derived from heat- and mass-balance measurements. J. Glaciol., 12(65), 275–289.
- Forrer, J. and M. Rotach. 1997. On the turbulence structure in the stable boundary layer over the Greenland ice sheet. *Boundary-Layer Meteorol.*, **85**(1), 111–136.
- Fröhlich, C. 1993. Changes of total solar irradiance. In McBean, G.A. and M. Hantel, eds. Interactions between global climate subsystems: the legacy of Hann. Washington, DC, American Geophysical Union, 123–129.
- Funk, M. 1985. Räumliche Verteilung der Massenbilanz auf dem Rhonegletscher und ihre Beziehung zu Klimaelementen. Zürcher Geogr. Schr. 24.
- Garnier, B. and A. Ohmura. 1968. A method of calculating the direct shortwave radiation income on slopes. J. Appl. Meteorol., 7(10), 796–800.
- Grainger, M.E. and H. Lister. 1966. Wind speed, stability and eddy viscosity over melting ice surfaces. *J. Glaciol.*, **6**(43), 101–127.
- Greuell, J.W. and T. Konzelmann. 1994. Numerical modeling of the energy balance and the englacial temperature of the Greenland ice sheet: calculations for the ETH-Camp location (West Greenland, 1155 m a.s.l.). *Global Planet. Change*, **9**(1–2), 91–114.
- Halldin, S. and A. Lindroth. 1992. Errors in net radiometry: comparison of six radiometer designs. *J. Atmos. Oceanic Technol.*, **9**(6), 762–783.
- Harding, R.J. and 7 others. 1989. Energy and mass balance studies in the firn area of the Hintereisferner. In Oerlemans, J., ed. Glacier fluctuations and climatic change. Dordrecht, etc., Kluwer Academic Publishers, 325–341.
- Hay, J.E. and B.B. Fitzharris. 1988. The synoptic climatology of ablation on a New Zealand glacier. J. Climatol., 8, 201–215.
- Hieltala, M. 1989. En utvärdering av areella nederbördsmetoder och mätarplaceringar i Tarfaladalen. (Master's thesis, Stockholm University.)
- Hock, R. 2003. Temperature index melt modelling in mountain areas. J. Hydrol., 282(1-4), 104-115.
- Hock, R. 2005. Glacier melt: a review on processes and their modelling. Prog. Phys. Geogr., 29(3), 1–30.
- Hock, R. and B. Holmgren. 1996. Some aspects of energy balance and ablation of Storglaciären, northern Sweden. *Geogr. Ann.*, 78A(2–3), 121–131.
- Hock, R. and H. Jensen. 1999. Application of kriging interpolation for glacier mass balance computations. *Geogr. Ann.*, **81A**(4), 611–619.
- Hock, R. and C. Noetzli. 1997. Areal melt and discharge modelling of Storglaciären, Sweden. *Ann. Glaciol.*, **24**, 211–216.

- Holmgren, B. 1971. Climate and energy exchange on a sub-polar ice cap in summer. Arctic Institute of North America Devon Island Expedition 1961–1963. Parts A–E. Uppsala, Uppsala Universitet. Meteorologiska Institutionen. (Meddelande 107–112.)
- Holmlund, P. and P. Jansson. 1999. The Tarfala mass balance programme. *Geogr. Ann.*, **81A**(4), 621–631.
- Holmlund, P. and V. Schytt. 1987. *Glaciärerna i Tarfala*. (Scale 1:20 000.) Stockholm, University of Stockholm. Department of Physical Geography.
- Jonsell, U., R. Hock and B. Holmgren. 2003. Spatial and temporal variations in albedo on Storglaciären, Sweden. J. Glaciol., 49(164), 59–68.
- Kirnbauer, R., G. Blöschl and D. Gutknecht. 1994. Entering the era of distributed snow models. Nord. Hydrol., 25(1-2), 1-24.
- Klok, E.J.L. and J. Oerlemans. 2002. Model study of the spatial distribution of the energy and mass balance of Morteratschgletscher, Switzerland. *J. Glaciol.*, **48**(163), 505–518.
- Kondrat'ev, K.Ya. 1969. *Radiation of the atmosphere.* New York, Academic Press.
- Konya, K., T. Matsumoto and R. Naruse. 2004. Surface heat balance and spatial distributed ablation modelling on Koryto Glacier, Kamchatka Peninsula, Russia. *Geogr. Ann.*, 86A(4), 337–348.
- Konzelmann, T. and R.J. Braithwaite. 1995. Variations of ablation, albedo and energy balance at the margin of the Greenland ice sheet, Kronprins Christian Land, eastern north Greenland. J. Glaciol., 41(137), 174–182.
- Konzelmann, T. and A. Ohmura. 1995. Radiative fluxes and their impact on the energy balance of the Greenland ice sheet. *J. Glaciol.*, **41**(139), 490–502.
- Liu, B.H.Y. and R.C. Jordan. 1960. The interrelationship and characteristic of direct, diffuse and total solar radiation. *Solar Energy*, **4**(3), 1–19.
- Martin, E. and Y. Lejeune. 1998. Turbulent fluxes above the snow surface. *Ann. Glaciol.*, **26**, 179–183.
- Moore, R.D. 1983. On the use of bulk aerodynamic formulae over melting snow. *Nord. Hydrol.*, **14**(4), 193–206.
- Morris, E.M. 1982. Sensitivity of the European hydrological system snow models. International Association of Hydrological Sciences Publication 138 (Symposium at Exeter 1982 – Hydrological Aspects of Alpine and High Mountain Areas), 221–231.
- Müller, G. and A. Ohmura. 1993. Radiation annual report ETH, No.2, 1990 and 1991. Zürcher Geogr. Schr. 52.
- Munro, D.S. 1990. Comparison of melt energy computations and ablatometer measurements on melting ice and snow. Arct. Alp. Res., 22(2), 153–162.
- Nash, J.E. and J.V. Sutcliffe. 1970. River flow forecasting through conceptual models. Part 1. A discussion of principles. J. Hydrol., 10(3), 282–290.
- Oerlemans, J. 2000. Analysis of a 3 year meteorological record from the ablation zone of Morteratschgletscher, Switzerland: energy and mass balance. J. Glaciol., **46**(155), 571–579.

- Ohmura, A., P. Kasser and M. Funk. 1992. Climate at the equilibrium line of glaciers. *J. Glaciol.*, **38**(130), 397–411.
- Ohta, T. 1994. A distributed snowmelt prediction model in mountain areas based on an energy balance method. *Ann. Glaciol.*, **19**, 107–113.
- Oke, T.R. 1987. *Boundary layer climates. Second edition.* London, Methuen; New York, Routledge Press.
- Orvig, S. 1954. Glacial-meteorological observations on icecaps in Baffin Island. *Geogr. Ann.*, **36**(3–4), 197–318.
- Paulson, C.A. 1970. The mathematical representation of wind speed and temperature profiles in the unstable atmospheric surface layer. J. Appl. Meteorol., 9, 857–861.
- Pettersson, R., P. Jansson and P. Holmlund. 2003. Cold surface layer thinning on Storglaciären, Sweden, observed by repeated ground penetrating radar surveys. J. Geophys. Res., 108(F1), 6004. (doi: 10.1029/2003JF000024.)
- Plüss, C. and R. Mazzoni. 1994. The role of turbulent heat fluxes in the energy balance of high Alpine snow cover. *Nord. Hydrol.*, **25**(1–2), 25–38.
- Plüss, C. and A. Ohmura. 1997. Longwave radiation on snowcovered mountainous surfaces. J. Appl. Meteorol., 36(6), 818–824.
- Rohrer, M. 1989. Determination of the transition air temperature from snow to rain and intensity of precipitation. *In* Sevruk, B., *ed. Instruments and observing methods.* Geneva, World Meteorological Organization, 475–482. (WMO/TD 328, Technical Report 48.)
- Sellers, W.D. 1965. *Physical climatology.* Chicago, University of Chicago Press.
- Sicart, J.-E. 2002. Contribution à l'étude des lux d'energie, du bilan de masse et du débit du fonte d'un glacier tropical: le Zongo, bolivie. (PhD thesis, Université de Paris.)
- Streten, N.A. and G. Wendler. 1967. Some observations of Alaskan glacier winds in midsummer. *Arctic*, **20**(2), 98–102.
- Ujihashi, Y., N. Takase, H. Ishida and E. Hibobe. 1994. Distributed snow cover model for a mountainous basin. *International Association of Hydrological Sciences Publication* 223 (Symposium at Yokohama 1993 – *Snow and Ice Covers: Interactions with the Atmosphere and Ecosystems*), 153–162.
- United States Army Corps of Engineers (USACE). 1956. *Snow hydrology: summary report of the snow investigations.* Portland, OR, US Army Corps of Engineers. North Pacific Division.
- Van den Broeke, M. 1996. Characteristics of the lower ablation zone of the West Greenland ice sheet for energy-balance modelling. *Ann. Glaciol.*, **23**, 160–166.
- Van de Wal, R.S.W., J. Oerlemans and J.C. van der Hage. 1992. A study of ablation variations on the tongue of Hintereisferner, Austrian Alps. J. Glaciol., 38(130), 319–324.
- Wendler, G. and G. Weller. 1974. A heat-balance study on McCall Glacier, Brooks Range, Alaska: a contribution to the International Hydrological Decade. J. Glaciol., 13(67), 13–26.

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