A method to retrieve the spectral complex refractive index and single scattering optical properties of dust deposited in mountain snow

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ABSTRACT. Dust deposition to snow can have regionally important climatic and hydrologic impacts resulting from direct reduction of surface albedo and indirectly from the initiation of snow albedo feedbacks. Modeling the radiative impacts of dust deposited in snow requires knowledge of the optical properties of both components. Here we present an inversion technique to retrieve the effective optical properties of dust deposited in mountain snow cover from measurements of hemispherical dust reflectance and particle size distributions using radiative transfer modeling. First, modeled reflectance is produced from single scattering properties modeled with Mie theory for a specified grain size distribution over a range of values for the imaginary part of the complex refractive index \(k = 0.00001-0.1\). Then, a multi-step look-up table process is employed to retrieve \(k\) and single scattering optical properties by matching measured to modeled reflectance across the shortwave and near infrared. The real part of the complex refractive index, \(n\), for dust aerosols ranges between 1.5 and 1.6 and a sensitivity analysis shows the method is relatively insensitive to the choice of \(n\) within this range. 1.525 was used here. Using the values retrieved by this method to update dust optical properties in a snow + aerosol radiative transfer model reduces errors in springtime albedo modeling by 50–70%.

KEYWORDS: energy balance, ice/atmosphere interactions, snow/ice surface processes, snow

1. INTRODUCTION

Mineral dust particles emitted from arid and disturbed landscapes are the most common atmospheric aerosol by mass (Andreae, 1995). The global radiative impact of these dust aerosols can be positive or negative depending on how they influence cloud formation and their optical contrast with the substrate (Tegen and others, 1996; Myhre and Stordal, 2001). Given the importance of aerosol optical properties on determining the magnitude of aerosol radiative forcing, there have been multiple direct analyses and indirect inversion techniques developed to determine the optical properties of aerosol dust and dust from geographic source regions (Gams and others, 1974; De Luisi and others, 1976; Patterson and others, 1977; Sokolik and others, 1993). The bulk of this effort has focused on Saharan dust, which dominates dust aerosol mass loading (Patterson and others, 1977; Linke and others, 2006; Kandler and others, 2007; McConnell and others, 2008; Wagner and others, 2012).

Dust aerosols also influence radiative forcing when deposited on snow (Painter and others, 2012; Skiles and others, 2012). Clean snow is highly reflective in the visible wavelengths and even moderately absorbing dust aerosols decrease visible albedo. This is a regionally important process that has received less attention than global atmospheric dust radiative forcing. The impacts of dust in snow have been most well studied in the mountain snow cover of the Colorado Rocky Mountains, the headwaters of the Colorado River, on which dust is deposited during the springtime when dust emission rates peak upwind in the semi-arid Colorado Plateau (Painter and others, 2012; Flagg and others, 2014). Deposition of mineral dust has increased five-fold in portions of the Upper Colorado River Basin (UCRB) since settlement and disturbance of the Western US (Neff and others, 2008), and studies indicate that extreme dust years may become more frequent in the future as climate warms and vegetation dynamics shift (Monson and others, 2011; Li and others, 2013).

Dust has also been shown to impact the snow albedo of glaciers in the Himalaya (Kaspari and others, 2009; Gautam and others, 2013; Kaspari and others, 2014) and Switzerland (Oerlemans and others, 2009), annual snow cover of the Sierra Nevada (Sterle and others, 2013) and snow in the Canadian Arctic (Woo and Dubreuil, 1985; Zdanowicz and others, 1998). Additional observational studies of dust in snow have occurred in the European Alps (De Angelis and Gaudichet, 1991; Franzén and others, 1994; Schwikowski and others, 1995; Grousset and others, 2003), central/east Asia (Wake and Mayewski, 1994; Xin and others, 2014) and the Antarctic Peninsula (McConnell and others, 2007). It has been suggested that dust on snow may be responsible for northern China remaining ice free during the last glacial maximum (Krinner and others, 2006). It has also been theorized that dust on snow accelerated snowmelt early in the history of Mars, leading to the formation of valley networks from meltwater (Clow, 1987).

Although radiative forcing by dust in snow has been well recognized for decades, its precise value has largely
remained unquantified. Many snow radiative forcing models justify neglecting dust because black carbon (BC), a widespread light absorbing aerosol produced by incomplete combustion, can be orders of magnitude more absorptive by mass than dust and the effects of dust loading in snow should be similar to those of optically equivalent concentrations of BC (Warren, 1984; Warren and Wiscombe, 1980). Alternatively, some models assume that all the dust is characteristically Saharan (Flanner and others, 2007). These assumptions are not well justified. Given the established presence and impact of dust on snow globally it is necessary to determine the regionally varying optical properties of dust deposited in snow. Furthermore, the optical properties of dust in snow cannot be properly inferred from source region dust, because exact source area is unknowable and particle size distributions (PSDs) and overall composition are altered during atmospheric travel (Miller and others, 2004).

The radiative properties of dust aerosols, which are size- and wavelength-dependent, are described by the spectral complex index of refraction:

$$m_λ = n_λ + ik_λ$$  \hspace{1cm} (1)

where $n_λ$ is the real part, also known as the simple index of refraction, $i$ is the imaginary number and $k_λ$ is the imaginary part. Values of $n$ have been fairly well established for airborne mineral aerosols, generally ranging from 1.5 to 1.6 for dust aerosols and between 1.4 and 1.6 for pure mineral phases (Grins and others, 1974; Patterson and others, 1977; Sokolik and others, 1993; Zhao and others, 1997; Barthelmy, 2012; Meng and others, 2010; Wagner and others, 2012).

The imaginary part, $k_λ$, describes absorption loss as the wave propagates through the medium. Despite a number of methods to determine it, it is less well established for dust aerosols. Methods can be generalized into two categories: direct and inversion. Direct methods use laboratory measurements to measure diffuse reflectance or transmitted light to retrieve $k$ values from radiation theories, like the two flux Munk theory (Patterson and others, 1977). Inversion methods for determining $k$ values utilize measurements from one or more optical instruments, like nephelometers, photometers and spectroradiometers, to determine scattering and reflectance. These instruments can be in the laboratory (Wagner and others, 2012), in the field (Grins and others, 1974), or on airborne remote-sensing platforms (Redemann and others, 2000; McConnell and others, 2008; Osborne and others, 2008). Measurements are then used to retrieve $k$ values by relating them to modeled scattering/reflectance. Inversion methods require that certain assumptions about the nature of the dust be made, for instance PSD and sphericity.

Here, an inversion method is presented to determine the spectral complex index of refraction for dust deposited in snow, motivated by the fact that generic/non-specific dust representations cannot accurately constrain radiative transfer modeling of snow albedo in the UCRB (or necessarily any other snow-covered region), either in magnitude or reflectance shape. Measured dust PSDs are used to model single scattering optical properties from Mie theory for varying values of $k$, and a specified value of $n$. Multiple scattering and reflectance is then modeled from single scattering optical properties, and the complex index of refraction is retrieved by matching measured hemispherical dust reflectance to modeled reflectance in the visible (VIS) and near infrared (NIR). The single scattering optical properties, associated with retrieved $k_λ$ values, are incorporated in a snow/aerosol radiative transfer model to verify the validity of results by comparing modeled albedo of snow containing dust to snow albedo measured in the field.

2. METHODS

2.1. Study area and field sampling

We used dust collected from snow at Swamp Angel Study Plot (SASP), a subalpine study plot located in Senator Beck Basin Study Area (SBBSA), a 290 ha study basin located in the San Juan Mountains of southwestern, CO (Fig. 1). The San Juan Mountains are the first major mountain range approached by dust aerosol plumes emitted from the southern Colorado Plateau, and SBBSA was established in 2003 to monitor the hydrologic impacts of dust in snow in the Colorado River Basin (CRB). For more information see Landry and others (2014) and Painter and others (2012).

Snow measurements at SASP have included weekly collections of snow samples for determination of dust loading at the surface and stratigraphy in the top 30 cm of the snow column at 3 cm intervals (the approximate maximum depth at which radiative forcing is influenced by light absorbing impurities). The dust in snow data record has been used to assess the interannual variability of dust deposition and dust composition (Lawrence and others, 2010; Skiles and others, 2012), but previous measurements were not carried out in a way to facilitate radiative transfer modeling. To address this void, a high-resolution record of snow properties and gravimetric dust and BC concentrations were collected on a near daily basis at SASP over the last 2 months of snow cover in 2013. A detailed description of this dataset is presented in Skiles and Painter (2016).

Briefly, measured snow properties included spectral snow albedo, grain size and snow density, in addition to impurity concentrations. Spectral albedo was measured above the surface of gravimetric snow sampling with an Analytical Spectral Devices FieldSpec3 field spectroradiometer. The optical grain size was retrieved via contact spectroscopy (Painter and others, 2007) in 2 cm increments across the full vertical snow profile. Snow density in each of the 10 gravimetric samples in the top 30 cm was calculated from sample mass and volume. Below the top 30 cm, snow density was measured with a 1 L density cutter and field scale at 10 cm intervals.

2.2. Laboratory measurements

Laboratory analysis for snow impurity content is described in more detail in Skiles and Painter (2016). Briefly, snow samples were kept frozen until time of analysis at which point they were melted, weighed, filtered and dried for dust mass and concentration. Dust PSD between 0.05 and 2000 μm was quantified utilizing laser light diffraction (Malvern Instruments; Mastersizer 2000E) from a subset of snow samples introduced directly using a wet dispersion system. The need to meet obscuration limits of the system limited analysis here to visibly dusty samples, but the extreme dust loading in spring 2013 enabled us to analyze
six samples, representing both single event and merged dust layers.

Dust does settle out during the process of melting the snow sample and to disperse the dust in the melted snow water again samples were agitated (both manually and through sonification) prior to analysis. We note here that sonification could break apart aggregates that may have been present in the snow. There is also potentially a discontinuity between PSDs determined from dispersed samples relative to aggregate (filtered and dried) samples. This is relevant for this analysis because we use dispersed dust PSDs for modeling but the reflectance of dried (aggregate) samples for retrieval, as discussed further below. To assess the variation in PSD between dispersed and filtered/dried dust samples, we also measured the PSD of dried dust from two samples post-filtering.

Hemispherical reflectance of optically thick dry filtered dust was measured with an Analytical Spectral Devices (ASD) FieldSpec3 spectroradiometer coupled to an ASD RTS-3ZC integrating sphere. The spectrometer measures from 0.35 to 2.50 µm, with contiguous bands that are 0.003 µm (at 0.7 µm) to 0.01 µm (at 1.4 and 2.1 µm) at full width half maximum. The spectra are resampled and splined to 1 nm resolution. The sample is illuminated by a collimated tungsten light source at a radiance close to that of sun at the Earth’s surface. We were able to measure reflectance of seven optically thick samples from 2013, representing both single event and merged dust layers. The spectrometers shortwave infrared (SWIR) detector was noisy and the reflectance between 1.7 and 2.5 µm needed to be smoothed, which introduces some uncertainty in the reflectance values in the SWIR.

The optical property retrieval technique presented here does not account for individual constituents of the impurity mixture. Impurities are here referred to as dust because they dominate the impurity mass, but likely also include some organics (bacteria, plant matter) and BC. The presence of BC could influence the selection of the real part of the refractive index, which has higher suggested values ($n = 1.75–1.95$ (Bond and Bergstrom, 2006)) than dust aerosol, Skiles and Painter (2016) showed that over the 2013 spring melt season BC concentrations ranged from 2 to 26 ppb. These concentrations accounted for, on average, <0.01% of the total impurity mass.

### 2.3. Dust radiative transfer modeling

The modeling and analysis scheme described here is represented in **Figure 2**. Mie theory was used to model single scattering and absorption for a measured PSD and specified value of $n$ with a range of $k_{\lambda}$ values, for wavelengths between 0.35 and 2.5 µm at 10 nm resolution, to match the spectral resolution of the SNOW, ICE and Aerosol Radiation model (SNICAR) (Flanner and Zender, 2005, 2006), the snow and aerosol radiation transfer model used to validate results. The PSD is described by the volume

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**Figure 1.** Overview of the four corners region of the western US showing location of Senator Beck Basin Study Area in the San Juan Mountains of southwestern Colorado.
weighted mean radius, $r$ and standard deviation of $\log(r)$ from the PSD measurements of dust samples.

The use of Mie theory requires the assumption of spherical dust particles, a reasonable, but imperfect assumption. Although dust aerosols are irregularly shaped and non-spherical, it has been shown that differences in optical properties between spherical and non-spherical particles, like the shape of the phase function (angular distribution of reflected light), become less important when integrated over hemispheres. Mishchenko and others (1995) showed that the spherical assumption can lead to large errors when retrieving properties where scattering geometry matters, like optical thickness for dust aerosols in the atmosphere, but spherical/non-spherical errors ‘averaged out’ when integrating over reflectance and illumination angles. Therefore, the accuracy of applying Mie theory is adequate when modeling radiative flux and albedo. Still, we recognize the spherical assumption as an uncertainty in this analysis, and plan to investigate the utility of non-spherical radiative transfer modeling in the future. Further discussion of the limitations of treating dust aerosols as spheres, can be found in Meng and others (2010) and Yi and others (2011) and citations therein.

Previous studies have reported that the retrieval of $k_\lambda$ is not sensitive to the value of the real part of the refractive index between $n = 1.5$ and $n = 1.6$ (Grams and others, 1974; Kandler and others, 2007; McConnell and others, 2008; Yi and others, 2011). To assess this, we conducted a sensitivity analysis by producing separate look up tables (LUTs) for $n = 1.5, 1.525, 1.55, 1.75$ and $1.6$. Retrievals of $k_\lambda$ from each LUT allowed us to independently determine that this method is also relatively insensitive to the $n$ value in this range (Fig. 3). Here we selected $n = 1.525$ across the entire wavelength range to match the value of Grams and others (1974), which was measured for dust from the southwestern US using the oil immersion technique.

The values for the imaginary part of the refractive index, $k_\lambda = 0.00001$–$0.1$, at $0.0001$ resolution, were selected to bracket the range of reported values for dust aerosols and mineral components in the literature. The single scattering optical properties were used to model multiple scattering and reflectance using the plane parallel discrete ordinate radiative transfer algorithm DISORT (Stamnes and others, 1988) to create a reflectance LUT catalogued by wavelength and $k$ value (Fig. 4). Measured reflectance was then processed through the LUT to retrieve $k_\lambda$. The associated spectral single scattering optical properties (albedo, asymmetry parameter and mass extinction coefficient) were then compiled as separate optical property LUTs to update SNICAR, discussed further below. Similar methodology has been used to infer the imaginary part of refractive index of sea-ice sediment by Light and others (1998) and for hydrated salt crystals in sea ice by Carns and others (2016).
2.4. Snow radiative transfer modeling

SNICAR computes multiple scattering and reflectance from snow + aerosol mixtures across 470 bands (0.3–5.0 µm) at 10 nm resolution with a single layer version of the two stream, multilayer radiative approximation of Toon and others (1989). The inputs for SNICAR include solar zenith angle, snow optical grain size, snow density and concentrations of impurities. The single scattering optical properties for impurities and ice are extracted from LUTs. For ice, LUTs are included for a large range of grain sizes (between 10 µm to 5 mm at 1 µm resolution) and have been updated to reflect the revised ice optical property compilation of Warren and Brandt (2008).

Currently, the dust optical properties in SNICAR are designed to represent general global dust aerosols, which are characteristically Saharan. The single scattering optical properties for four partitions of a lognormal size distribution (D1: 0.1–1 µm; D2: 1.0–2.5 µm; D3: 2.5–5.0 µm; and D4: 5.0–10.0 µm) are characterized by combinations of indices of refraction for a mixture of quartz, limestone, montmorillonite, illite and hematite using the Maxwell-Garnett approximation (SNICAR-Online (Flanner and others, 2007)). We compare SNICAR albedo, modeled with both the general dust characterization (‘dustgeneral’) and with the updated optical properties for dust on snow (‘dustsnow’) presented here, and assess modeled albedo scenarios by comparing them with both spectral albedo, measured at the snow sampling site and broadband albedo, measured at the instrumentation tower nearby the sampling site.

Spectral albedo was modeled with SNICAR for each day measurements, were made in the field between 11 March and 18 May 2013. Snow property inputs were specified for the full depth of the snowpack, represented as 11 layers; the top 10 layers are 3 cm deep, and correspond to snow sampling described above and in Skiles and Painter (2016), the 11th layer represents the ‘bulk’, or remainder, of the snowpack (Fig. 5). Density, optical grain size (resampled from 2 to 3 cm resolution) and dust concentrations are specified in each of these layers. Across the lowest layer the mean density, mean grain size and bulk dust concentration were specified. Model solar zenith angles were concurrent with measured values. For dustgeneral runs, dust particles were binned based on measured PSDs (3% D1, 6% D2, 9% D3, 82% D4). Note that the filtered dust pictured in Figure 5 is an example of an optically thick dust sample.

To assess modeled albedo, we compare modeled with measured spectrally weighted albedos, which were calculated over the broadband (BB; 0.35–1.5 µm), visible (VIS; 0.35–0.75 µm) and NIR wavelengths (0.75–1.5 µm) by dividing the product of the summation of irradiance and albedo by the summation of irradiance, i.e. for broadband albedo between 0.35 and 1.5 µm:

\[
\alpha = \frac{\sum_{\lambda = 0.35\mu m}^{1.5\mu m} I \times \alpha_{dust}\Delta\lambda}{\sum_{\lambda = 0.35\mu m}^{1.5\mu m} I\Delta\lambda}
\]

where \(I\) is spectral irradiance at a given solar zenith angle, \(\alpha_{dust}\) is the modeled albedo with dust at the same solar zenith angle and \(\lambda\) is the wavelength (µm). We use the difference between measured reflected flux and modeled reflected flux (\(\alpha_{dust} \times I\)) to quantify the skillfulness of albedo modeled with dustgeneral and dustsnow to represent observed conditions.

To minimize uncertainty due to measurement conditions we selected only the days that had consistent (fully clear or fully cloudy) sky conditions during albedo collection (14 of 36 d). Although this is a smaller subset of the full record, these days were representative of the range of observed snow conditions, from cold to melting snow, and from relatively low to extremely high-dust content. As noted for integrating sphere measurements, there was high noise in the SWIR for spectral albedo measurements, which is why we chose to carry out the comparison between 0.35 and 1.5 µm. This is acceptable in this application because the majority of snow reflectance, and solar irradiance, occurs in this range.

During albedo measurements uplooking measurements were not collected in irradiance mode, therefore we

![Fig. 3.](https://doi.org/10.1017/jog.2016.126) We found that varying the real part, \(n\), did not strongly impact the retrieval of the imaginary part, \(k\). Here we show an example retrieval where the shaded area represents the range of \(k\) values for specified values for \(n\) between 1.5 and 1.6.

![Fig. 4.](https://doi.org/10.1017/jog.2016.126) Visual representation of DISORT look up table (LUT) used to retrieve the imaginary part of the complex index of refraction. The actual LUT is more densely populated; the resolution is limited here so that reflectance curves remain discernible.
model clear sky spectral irradiance with Santa Barbara DISORT Atmospheric Radiative Transfer model (SBDART) (Ricchiazzi and others, 1998). The presence of clouds can shift the spectral distribution of irradiance, while this was not accounted for here, daily variation in irradiance was accounted for by scaling modeled irradiance such that its spectral integration matched measured broadband irradiance at the instrumentation tower.

Snow albedo varies with wavelength and is controlled in the NIR wavelengths by snow grain size and in the visible wavelengths by impurity content thus a spectrally explicit treatment is required. In addition, spectral albedo is best used in this analysis given that model inputs (including grain size and impurity content) and albedo measurements were spatially and temporally coincident. However, due to sky condition limitations, the spectral albedo dataset was smaller than the number of days when measurements were collected. Here, we also use broadband albedo from tower pyranometers to compare modeled with measured albedo across the full measurement time series (modeled spectrally weighted albedos, Eqn (2), were calculated between 0.35 and 2.5 µm for this comparison). Measured broadband albedo is calculated from uplooking and downlooking pyranometers after correcting snow reflectance for slope and aspect gradients (Painter and others, 2012). For consistency, comparison is made at the same daily time step across the time series, 11:00 AM local time, which corresponds to the time when snow measurements were typically being made.

Fig. 5. A representation of SNICAR inputs and output for 11 May 2013. Snow properties and dust concentrations are specified in 11 layers: 10 3-cm surface layers and a single layer for the remainder of the snowpack.
3. RESULTS AND DISCUSSION

3.1. Laboratory measurements

3.1.1. Particle size distributions

The dust PSDs were relatively consistent from sample to sample (Fig. 6). Variations mainly depended on the number of dust deposition events represented in the sample, where samples that contained dust from single events exhibited a slightly more narrow distribution range than snow samples that contained merged dust events. This may be due to the fact that the source region and deposition conditions are fairly consistent from event to event. More likely it was due to the fact that 90% of the dust was deposited by one event (dust event No. 6; ‘D6’), which then dominated the PSD. The PSD used for the Mie modeling, a volume-weighted mean radius of 6 µm and standard deviation of log(r) of 0.28, was a mean of all PSDs including single and merged events.

We note that the PSDs presented here are shifted toward smaller sizes relative to PSDs previously published for dust deposited in snow between 2005 and 2008 at SBBSA (see Fig. 2 in Lawrence and others (2010)). We attribute this to differences in samples preparation; in Lawrence and others (2010) samples were freeze-dried, acid digested, sieved and then measured by size fraction, and it was recognized that they slightly underestimate the mass fraction of <250 µm size particles with this approach. That being said, both methodologies return size ranges that are classified as predominantly clay and silt, and have similar mean particle sizes (phi units; ~6).

The inversion for kr is sensitive to the selected PSD and measuring PSDs directly from melted samples, as we did here, is suggested. In part because dust in snow primarily is in contact with liquid water during its solar-interactive lifetime, and as might be expected we found that if the PSD was measured after the sample had been filtered, dried and physically separated (but no further treatments were applied like sieving), then the distribution shifted toward larger particles sizes (mean radius = 10 µm). When the ‘dry’ PSDs were used to produce the LUT the retrieved kr values were representative of weakly absorbing mineral phases like quartz, and were too low to describe absorption by dust in snow in this region.

3.1.2. Dust reflectance

Over the solar spectrum, the absorptivity of the dust filtered from the snow was greatest across the visible wavelengths and decreased into the NIR. At 0.35 µm albedo was ~0.1 and increased steadily over the visible wavelengths to ~0.3 at 0.75 µm, ~0.4 at ~1.35 µm, and then to ~0.5 at 2.5 µm (Fig. 7). The 2.2 µm absorption feature indicates the presence of clays. The general shape and magnitude of dust reflectance was consistent between samples, and there were no discernible patterns differentiating reflectance of individual and merged samples (Fig. 7). This is not unexpected given that the majority of dust was deposited by a single event, as mentioned in Section 3.1.1, which would then dominate the optical properties of merged samples. Although we report the retrieved kr values for the average reflectance, they were determined for all reflectance curves and the difference between the retrievals was negligible.

3.1.3. Dust optical properties

The retrieved imaginary part of the complex refractive index for dust in snow ranged from 0.0015 at 0.35 µm to 0.0005 at 1.5 µm (Fig. 8). The uncertainty in retrieval, assessed by comparing the difference in retrieved values between the individual and average reflectance curves, was ±9 × 10⁻⁵. The most rapid decrease in kr corresponded to the increase in reflectance across the visible wavelengths between 0.35 and 0.6 µm, where kr decreases from 0.0015 to 0.0006. Some complex indices of refraction retrieved by this method across the visible wavelengths were 1.525–0.0015i, 1.525–0.0010i and 1.525–0.0006i at 0.35, 0.5 and 0.75 µm, respectively (see Table 1 for more values).

Other kr values published for dust aerosols are widely ranging and are typically only determined at a few wavelengths, but generally, what we would expect is that dust mainly originating from the southern Colorado Plateau would be more absorptive in the visible wavelength relative to most but not all Saharan dust, which is generally less iron rich. We selected a few values from the literature for comparison. Carlson and Benjamin (1980) summarized a range of previously published values in the visible, NIR and infrared for Saharan dust, in the visible wavelengths studies found that the dust was most absorptive ~0.3 µm (0.018–0.039) with decreasing absorptivity toward 0.7 µm (0.002–0.012). These values are higher than more recent
measurements, McConnell and others (2010) collected airborne Saharan dust over West Africa and found the imaginary part of the complex refractive index at 0.55 µm to range between 0.0001 and 0.0046. Muller and others (2008) report higher values of 0.0051, 0.0016 and 0.0045 at 0.45, 0.55 and 0.65 µm, respectively, for near-surface airborne dust in Morocco. Very few studies have taken place in the western US, the imaginary part of the complex refractive index suggested by Grams and others (1974), 0.005 at 0.5µm determined from near-surface airborne dust in Texas, was the geometric mean value from a set of retrievals that ranged from 0.0009 to 0.01. We would like to note again that the optical properties of dust in snow should not be inferred from the assumed source region, but there have been no other studies of which we are aware that have collected dust deposited in snow for optical property analysis.

The single scattering albedo, the probability that a photon will survive an extinction event (where 1 is fully scattering and 0 is fully absorbing), for dust_{snow} ranged from 0.76 at 0.35 µm to 0.97 at 2.5 µm (Fig. 9). Corresponding to the measurements, McConnell and others (2010) collected airborne Saharan dust over West Africa and found the imaginary part of the complex refractive index at 0.55 µm to range between 0.0001 and 0.0046. Muller and others (2008) report higher values of 0.0051, 0.0016 and 0.0045 at 0.45, 0.55 and 0.65 µm, respectively, for near-surface airborne dust in Morocco. Very few studies have taken place in the western US, the imaginary part of the complex refractive index suggested by Grams and others (1974), 0.005 at 0.5µm determined from near-surface airborne dust in Texas, was the geometric mean value from a set of retrievals that ranged from 0.0009 to 0.01. We would like to note again that the optical properties of dust in snow should not be inferred from the assumed source region, but there have been no other studies of which we are aware that have collected dust deposited in snow for optical property analysis.

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<table>
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<tr>
<th>Wavelength (µm)</th>
<th>Complex Refractive Index, k</th>
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<td>0.35</td>
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<td>1.525–0.0013/</td>
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Fig. 9. The single scattering albedo, asymmetry parameter and mass absorption coefficient for dust_{snow} and four size bins of dust_{general}.

Fig. 10. Surface dust concentrations, shown with snowfall events, between 21 March and 18 May 2013.
decrease in absorption and $k_\lambda$ values across the visible wavelengths, the largest rate of change in SSA occurred between 0.35 and 0.7 µm, where it increased from 0.76 to 0.9. The asymmetry parameter $g$, the mean cosine of direction of scattering (where 1 is forward scattering and −1 is backward scattering), for dust\textsubscript{snow} decreased slightly from 0.82 at 0.35 µm to 0.7 at 2.5 µm. This indicates that across the solar wavelength range there is a decrease in the forward scattering, and penetration of photons into the snowpack, by dust. An assumed particle density of 2.6 g cm\textsuperscript{-3} (Tegen and Fung, 1995; Hess and others, 1998; Kandler and others, 2007) was used to determine the mass specific extinction coefficient for dust\textsubscript{snow}, which was highest at 0.35 µm, decreased to 0.7 µm, and then remained fairly constant into the NIR (Fig. 9).

The optical properties retrieved for dust\textsubscript{snow} are plotted with the optical properties for the four size bins of dust\textsubscript{general} in Figure 9. The optical properties for dust\textsubscript{snow} are most similar to properties for the largest dust\textsubscript{general} size bin (D4: 5–10 µm), which is expected given the volume weighted mean radius for dust\textsubscript{snow} falls within this range. Notably, the main difference between scenarios is the higher absorption coefficient of dust\textsubscript{snow} in the visible wavelengths relative to the dust\textsubscript{general} D4 size bin.

Fig. 11. Measured and modeled spectral albedo, difference from measured albedo, reflected flux, and difference from measured reflected flux for a relatively clean day (24 April), a day with high dust content near but not at the surface (28 April), and a day with high dust content at the surface (2 May).
Sokolik and Toon (1999) presented a good summary of the limitations of retrieving dust optical properties from bulk samples, like the method presented here. Essentially, they argue that it is difficult to justify the representativeness of bulk samples when dust aerosols are highly variable in time and space and also question the appropriateness of attributing a single refractive index to mixtures of various particle sizes and chemical composition.

We acknowledge the validity of these arguments for dust aerosols in transport but argue that using the reflectivity of bulk samples is an appropriate method to retrieve optical properties for dust in snow, for multiple reasons. First, space-time variability is constrained by deposition region and seasonality of dust impacts, and we have found DOS reflectance and grain-size distributions exhibit limited intra- and interannual variability. Second, this method utilizes hemispherical reflectance and is therefore not sensitive to issues associated with illumination angle. Third, approaching dust in snow with a forward, composition mixing approach neglects some absorbing components like organics (bacteria, plant matter) since these are typically removed by digestion/sieving prior to compositional analysis. Ultimately, we argue this method is useful because it improves radiative transfer modeling of snow-containing dust, as discussed below, and provides a method for the establishment of a geographic library of optical properties of dust found in snow around the globe.

### 3.2. Evaluation of dust optical properties

#### 3.2.1. Spectral albedo

Snow conditions on days in which spectral albedo measurements were made can be generally classified into three types that occurred during three distinct time periods: five relatively clean snow days when dust near the surface was <0.1 pptw (28 March–24 April); four transitional days over which dust layers began to converge and emerge at the surface (26–29 April); and five days with high-dust content (4.0 pptw or more) at the surface (2–4 May, 17–18 May) (Fig. 10). We selected a day during each of these periods to show: (1) albedo modeled with both dust$_{\text{general}}$ and dust$_{\text{snow}}$, (2) the difference between modeled and measured albedo, (3) reflected flux and (4) the difference between modeled and measured reflected flux (Fig. 11). In Figure 12, spectrally integrated BB, VIS and NIR albedo are plotted for all 14 d, and the summary of results is presented in Table 2.

Due to the presence of dust in all the snow samples, albedo modeled with dust$_{\text{snow}}$ was always lower than dust$_{\text{general}}$ because dust$_{\text{snow}}$ is more absorptive across the VIS wavelengths. Snow reflectance modeled with dust$_{\text{snow}}$ also better captured measured snow reflectance magnitude and shape, particularly on days when there was high-dust content at or near the surface. This higher absorption resulted in an improvement in albedo modeling of 50% on average across the full range of snow reflectance, reducing the
difference in reflected flux ($\Delta$ flux) from 43.9 to 20.7 Wm$^{-2}$. The most marked improvement occurred across the VIS during the 5 d when dust was at the surface, when dust$_{snow}$ reduced errors by almost 80% relative to dust$_{general}$ (Fig. 11). Therefore, utilizing dust$_{snow}$ optical properties allowed SNICAR to more accurately model the reduction in snow albedo due to dust in this region, particularly in the presence of heavy dust loading.

The largest variation between measured and modeled albedo for both dust optical representations occurred in the NIR wavelengths in the presence of heavy dust loading, where SNICAR overestimated NIR albedo by $\sim$15% for dust$_{snow}$ and $\sim$20% for dust$_{general}$, with respective $\Delta$ flux of 13.3 and 17.8 Wm$^{-2}$. Given that (1) we force the model with measured effective grain size, and (2) solar irradiance across this wavelength range is lower, we would have expected these errors to be smaller and we discuss this in more detail below. Despite the presence of these errors, dust$_{snow}$ still improved the modeled NIR albedo, reducing the average errors from 12 to 9%.

3.2.2. *Discussion of NIR errors*

Albedo in the NIR should be a better match in all cases given that it is determined by the optical grain-size input, which is estimated from measured reflectance. The method, contact spectroscopy, uses the integral of the continuum normalized ice absorption feature centered at 1.03 $\mu$m to invert for grain size using the same theory and ice optical properties contained in SNICAR. We recognize that extreme dust deposition, like that which occurred in 2013, could impact the grain size retrieval by making the absorption feature more shallow, therefore returning a smaller grain size. Increasing the snow grain size, though, does not resolve the NIR discrepancy observed here, because a larger grain size reduces the albedo at all wavelengths (this was observed in test runs, also see (Warren and Wiscombe, 1980)). Therefore, we attribute this issue to representation of dust absorption within SNICAR, as opposed to an error that could be attributed to inputs.

The mismatch between measured and modeled NIR albedo issue may arise from how dust particles and snow grains are modeled as a mixture: SNICAR treats dust as an external mixture, while at SBSA wet and dry deposition of dust is observed, resulting in dust that is both internally and externally mixed with snow grains. An external treatment results in heterogeneous dispersions of dust among snow grains that interact with solar radiation differently from homogeneous external mixtures. This micro-scale variation in absorption manifests as spatially variable surfaces, for example, high-surface roughness and vertical and planar patches of concentrated dust interspersed with clean snow (Fig. 13). Even with high-dust content, surfaces like these would have reflectance that is characteristic of both dust and ice.

The way SNICAR models NIR albedo in the presence of heavy dust loading is similar to the spectral albedo

<table>
<thead>
<tr>
<th>Date</th>
<th>DOY</th>
<th>Irradiance Wm$^{-2}$</th>
<th>Reflected flux Wm$^{-2}$</th>
<th>Measured Albedo</th>
<th>Dust$_{snow}$ Albedo</th>
<th>$\Delta$ Flux Wm$^{-2}$</th>
<th>Dust$_{general}$ Albedo</th>
<th>$\Delta$ Flux Wm$^{-2}$</th>
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Table 2. Summary of measured broadband, visible, and near infrared irradiance, reflectance and albedo, in comparison with modeled albedo and difference in reflected flux from that which was measured, for the two different dust optical properties representations.
measurements presented in Singh and others (2010), where varying amounts of dust were manually applied at the snow surface. In this instance, snow would almost be exclusively externally mixed. In spectroscopy measurements a plateau of NIR albedo and increased SWIR albedo with increasing amounts of dust was observed. Essentially, the reflectance became more dust like and less ice like in the NIR/SWIR. As shown here, this is not representative of heavy dust absorption deposited by atmospheric deposition, where NIR albedo does not plateau and albedo still reduces close to 0 in the SWIR. Previous radiative transfer models of snow containing impurities have treated them as both exclusively external (Warren and Wiscombe, 1980) and exclusively internal (Chýlek and others, 1983). We suggest that representing dust as both internally and externally mixed would allow modeled absorption in the NIR to better match observations.

3.2.3. Broadband albedo time series
Using dust$_{\text{snow}}$ optical properties also improved albedo modeling relative to the measured broadband albedo time series from the tower (Fig. 14).

Prior to 28 April, when surface concentrations were relatively low (0.01–0.35 pptw), dust$_{\text{snow}}$ moderately improved albedo modeling and reduced $\Delta$ flux from 43 to 33 W m$^{-2}$. Between 29 April and 5 May when dust layers emerged and converged at the snow surface with melt (0.5–5.7 pptw), using dust$_{\text{snow}}$ improved albedo modeling by 50%, reducing $\Delta$ flux from 122 to 67 W m$^{-2}$. When combined dust layers were exposed at the surface (after 5 May, >5.0 pptw), using dust$_{\text{snow}}$ improved albedo modeling by ~70%, reducing $\Delta$ flux from 91 to 30 W m$^{-2}$.

The snow albedo measured at the tower may not always be representative of snow in the nearby study plot, and it should be noted that snow melted out underneath the tower a day and a half earlier than in the measurement plot. This is likely a product of the snow being shallower under the tower due to the difference in underlying surface height of the ground (which varies across the study plot). It could also be a product of spatial variability in albedo, which was not characterized. Still, it is worthwhile to assess the variation between SNICAR modeled albedo and tower measurements over the full time series. Relative to tower albedo, dust$_{\text{snow}}$ improved broadband albedo modeling by 50% over the spring and 70% in the presence of heavy dust loading.

4. CONCLUSION
Here, we presented an inversion technique to determine the complex index of refraction and single scattering optical
properties of dust deposited in mountain snow cover using measured PSDs and hemispherical reflectance. We validated our retrievals by comparing albedo modeled by a snow + aerosol radiative transfer model with measured albedo, and found utilizing the derived optical properties of reduced errors in broadband albedo modeling by 50% relative to optical properties for a ‘global mean’ dust characterization.

The study of light absorbing impurities in snow has focused on BC in permanent snow and ice in the high northern latitudes where even minor reductions in albedo can have important climatic impacts (Hansen and Nazarenko, 2004; IPCC, 2007, 2013). Despite the importance of annual snowmelt runoff in the mid-latitudes, and the increased risk for dust emission and deposition with climate and land use change, the impacts of mineral dust on snow cover are not as well understood and the optical properties of dust are poorly constrained observationally. A few recent studies have found that dust dominates radiative forcing in mid-latitude mountain snow cover, even in the presence of BC (Sterle and others, 2013; Kaspari and others, 2014). The method presented here, which requires no more than an optically thick dust sample, could be employed to determine the region specific dust optical properties in mountain snow cover in remote regions like the Middle East, Central Asia and the Himalaya to improve radiative transfer and hydrologic modeling efforts.

In some areas organics, like algae and tree debris, also play a role in albedo decline (Winkler and others, 2010; Benning and others, 2014). This method, while it does not directly discriminate between dust and other impurity inclusions, assumes that dust dominates the impurity mass. This has been well established in this region, but in locations where organics are the dominant impurity, this method would not be appropriate given the variability in size, shape and optical properties of organic material.

Although the ultimate goal of this method was to improve the accuracy of radiative transfer modeling of snow containing dust, it may be useful in other applications, given that multiple groups worldwide have identified optical property characterization as the main missing component for understanding the climatic role of dust aerosols globally. Additionally, the development of this method facilitates an additional inversion technique to retrieve dust concentrations from a snow and snow containing dust reflectance library when the only snow albedo measurements are available, which has important implications for in situ and remote sensing retrievals in remote snow-covered environments.

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