Modelling vaccination programmes against measles in Taiwan

S. C. CHEN1, C. F. CHANG1, L. J. JOU1,2 AND C. M. LIAO1*

1 Ecotoxicological Modelling Centre, Department of Bioenvironmental Systems Engineering, National Taiwan University, Taipei, Taiwan, ROC
2 Department of Biomechatronic Engineering, National Ilan University, Ilan, Taiwan, ROC

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SUMMARY

Vaccination has proved a powerful defence against measles. We reappraise measles seroepidemiological data in Taiwan from 1974 to 2004 having robust age-stratified serological information on exposure and immunity to quantitatively characterize measles vaccination programmes. We dynamically model measles seroepidemiology to estimate age-dependent intensity of infection associated with the effects of different contact patterns on pre- and post-vaccination. The WAIFM (who acquires infection from whom) contact matrix is employed to describe the transmission between and within each age group. A deterministic SEIR (susceptible–exposed–infected–recovery) model is used to capture subpopulation dynamics. Our study shows that mass regional or nationwide vaccination programmes could greatly reduce the potential for a major measles epidemic and have strong direct effects on the potential impact of childhood vaccination. We parameterize a predictive model that should reduce the socio-economic costs of measles surveillance in Taiwan and thereby encourage its continuance, especially for preschool children.

INTRODUCTION

Measles virus is one of the most contagious diseases known to humans and is a major killer of children in the developing countries of Africa and South America. The high mortality rate associated with measles virus infection results from increased susceptibility to opportunistic infections [1]. Measles had been endemic with a 2-year epidemic cycle in Taiwan until the introduction of the universal measles immunization programme (two doses, one at age 9 months and the other at age 15 months) in 1978 [2–6]. However, there were still several epidemic outbreaks in 1985, 1988, and 1989 with 2219, 1386, and 1060 reported cases, respectively. The 1985 epidemic resulted in a total of 97 deaths (mortality rate equal to 1.7 deaths/100 000 population aged <15 years). In January 1989, an outbreak of measles occurred among elementary and junior high-schoolchildren at a rural village, Li-Tse, in northeastern Taiwan, demonstrating that the disease spread from younger (aged 5–9 years) to older schoolchildren (≥10 years) and pre-schoolchildren (≤4 years) in both the Taipei city and suburban areas of Taipei county [3, 7]. Therefore, measles surveillance has been established based on passive reporting since 1985. Moreover, the government established a national goal of measles elimination by 2000 [2, 4–6].

Several countries have established serological surveillance to provide supplementary data as the basis
for immunization and public health planning programmes. The European Sero-Epidemiology Network (ESSEN) collected data through large serological surveys of measles, mumps and rubella antibodies and has recently performed surveys in eight participating European countries [8]. Seroepidemiology can be defined as the systematic collection and testing of blood samples from a target population or a representative sample. Seroepidemiological data can measure the population susceptibility profile and identify current and past experiences with infectious diseases by means of antibody and antigen tests. Serological survey of measles has been investigated for different countries such as Italy [9], Zambia [10], and European countries [8, 11].

Mathematical models are useful in investigating the potential impact of changes in vaccination programmes, e.g. the introduction of mass vaccination campaigns or changes in the age of vaccination and changes in effective vaccination coverage in those serological surveys that facilitate several important epidemiological parameters. We use prevaccination seroepidemiology to estimate the age-specific force of infection (FOI), which is defined as the per capita rate of acquisition of infection converted from seronegativity to seropositivity [12]. Finally, the age-specific transmission rate could be described by the basic reproduction ratio, $R_0$, quantifying the transmissibility of any infectious disease, which is defined as the expected number of successful secondary infections cases generated by a typical primary infected case in an entirely susceptible population [12–14]. This quantifies the transmissibility of the potential of the infection in a given population. Contact process may be seen as the infectious disease transmission route from the infectious to susceptible where the transmissibility varied with heterogeneous contact patterns based on different age of individuals or settings [15, 16]. In light of the contact matrix models, the WAIFW (who acquires infection from whom) matrix was commonly used to control the transmission within and between each age group in the spread of airborne infections [17–20].

Here we use a relatively parsimonious individual-based mechanistic model that allows us to accurately capture the overall effects of pre- and post-vaccination epidemiology of measles on the subpopulation dynamics. To achieve this objective, we employed the standard deterministic compartmental model known as the susceptible–exposed–infected –recovery (SEIR) model to provide a mechanistic bridge between theoretical models and empirical data [12]. The SEIR model is a cornerstone of epidemiology, as it provides a simple mechanistic model for microparasite dynamics and can represent the transmission dynamics for populations [21–24].

The aims of this study are twofold: (1) to compare the pre- and post-vaccination epidemiology of measles in a national context by using mathematical modelling concepts; (2) to provide useful parameter values for further refining childhood vaccination modelling and perspectives toward measles elimination.

**MATERIALS AND METHODS**

**Quantitative seroepidemiological data**

Seroepidemiological data is the powerful information that provides us with the immune proportion of the host before the disease outbreak. We can combine the vaccine effectiveness with the results of the seropositive level from post-vaccination to estimate the level of herd immunity of the interesting population. In this study, we adopted the limited data of the seropositive level in Taiwan from 1974 to 2004 to estimate the age-specific FOIs and $R_0$ by linking the age group-specific transmission contact patterns for pre- and post-vaccination epidemiology of measles. Based on the surveys sites of measles vaccination, the nationwide data adopted from Huang et al. [2], Lee et al. [6] and Chiu et al. [25] were used in the age-specific modelling scheme, whereas the regional settings of Taiwan data adopted from Lee et al. [5] were used in the population-specific modelling scheme. We assumed that these samples are representative of the random sampling population. We estimated that the average vaccination coverage ranged from 2% to 8% in 1974–1977. However, the values were higher from 21% to 55% in 1978–1990 as the universal measles immunization programme was instituted in 1978, whereas the values ranged from 71% to 88% in 1991–2004.

The serum sample was tested by the usual quantitative enzyme immunoassay (EIA) kit and Enzyme-linked immunosorbent assay (ELISA) kit (Table 1). The first published EIA and ELISA systems differed in assay design, yet both techniques are based on the principle of immunoassay with an enzyme. We thus ignored the difference between test kits in our study. Furthermore, we treated the seroepidemiological data from Lee et al. [6] as prevaccination data while other
data were treated as post-vaccination data in estimating $R_b$. Figure 1(a, b) shows the epidemics of the confirmed cases of measles outbreaks from 1985 to 1992 associated with data from 1993 to 2004 (adopted from Center of Disease Control Taiwan, ROC), indicating that measles outbreaks occurred in 1985, 1988–1989, and 1992 (Fig. 1a). The recent number of confirmed cases of measles was <40 (Fig. 1b).

The profile of measles immunoglobulin G (IgG) seroprevalence indicates the age-specific measles IgG seroprevalence for 1974–1977, 1991–1992, and 2004 (Fig. 1c) and the age-/population-specific measles IgG seroprevalence for 1995–1997 (Fig. 1d). The IgG seroprevalences are increasing approximately with age, indicating that the existing antibody was contributed by the vaccinated and infected persons before serum testing. We used a dynamic model of seroepidemiology to describe the profile of age-specific seroprevalence of measles [26],

$$S^+(a) = 1 - \exp \left\{ \frac{k_1}{k_2} \left[ k_2(a - L_C) + 1 \right] \right\} \times \exp(-k_2(a - L_C)) - 1 \right\} , \quad (1)$$

where $S^+(a)$ is the proportion of seropositive individuals to measles at a specific age group $a$, $k_1$ and $k_2$ are fitting parameters that can be estimated by fitting eqn (1) to seroprevalence data (Fig. 1c, d), and $L_C$ is the average duration of maternal immunity for measles that is $\approx 3$ months [12].

### Age-specific FOI for pre- and post-vaccination

The FOI, that depends on the number of infectious individuals and mixing patterns within a population in a given time period (e.g. 1 year), reflects the proportion of susceptible persons in the model population who acquired new infections during that time period. The FOI can be directly estimated from the serological data of pre- and post-vaccination [12],

$$1 - S^+_b(a) = \frac{X}{N} = x = \exp \left( - \int_0^a \lambda_b(a) da \right) , \quad (2)$$

$$1 - S^+_b(a) = \frac{X'}{N} = x' = \exp \left( - \int_0^a \lambda_b(a) da \right) , \quad (3)$$

here $S^+_b(a)$ and $S^+_b(a)$ are the age group-specific proportion of seropositive individuals of the pre- and post-vaccination, respectively, $1 - S^+_b(a)$ is equal to the susceptible number $X$ divided by the population number $N$, representing the susceptible proportion of the population $N$, and $\lambda_b(a)$ and $\lambda_b(a)$ are the pre- and post-vaccination FOIs at a specific age group $a$, respectively. We assume that the recovered number of the population $N$ will not be a susceptible number again. We further assume that the post-vaccination data reflect a post-vaccination equilibrium situation and we state that a time span long enough to allow the onset of a post-vaccination equilibrium is passed. For post-vaccination modelling, we assume that the contribution of the proportion of seropositive is vaccinated on an individual basis only.

We further considered the following five age groups based on the social behaviours, corresponding to the major school grades in Taiwan: 0–1 (babies), 2–3 (toddlers), 4–6 (preschool), 7–14 (primary school), and 15–35 (adults). The five age groups were chosen to account for the fact of high prevalence in children throughout the world, which plays a very important role.

### Contact pattern model

The contact pattern is a complicated process which depends on contact frequency, number of contacts of infectious persons, virulence of the pathogen, and the
appropriate mode of the transmission route. The processes therefore provide the information necessary to focus on the available control measures and determine the effectiveness of elimination programmes. We use WAIFW to determine the transmission within and between each age group occurs at different rates due in part to a lack of transmission frequency information of susceptible and infectious [12].

We adopt three contact pattern matrices to describe the specific transmission to account for the human behaviour and population settings (Appendix 1). Matrix $\beta_{na}(a, a')$ structure [eqn (A1)] is chosen to reflect the transmission rate that depends only on the age of the susceptible [i.e. $\beta(a, a')=\beta(a)$] to compare its predictions with those of more plausible structures. Matrix $\beta_{na}(a, a')$ structure [eqn (A2)] corresponds to the transmission process for those in the first four age groups being primarily from contacts within their own age group against a general background common to all individuals, indicating the large amount within age group mixing. On the other hand, matrix $\beta_{na}(a, a')$ structure [eqn (A3)] shows that there is a unique coefficient ($\beta_2$) describing the transmission among susceptible and infectious in age group 2 associated with the other two coefficients ($\beta_1$ and $\beta_3$) for other contacts among children aged <6 years; whereas adolescents and adults are described as being likely to acquire infection from a wider range of age groups. We further treat $\beta(a, a')=\beta(a', a)$ for $\beta_{na}(a, a')$ and $\beta_{na}(a, a')$ to reflect a symmetry relation, indicating that the individuals in age group $a$ make contact with individuals in age group $a'$ at the same rate as which individuals in age group $a'$ make effective contact with individuals in age group $a$, where $a$ and $a'$ represent ages of susceptible and infectious individuals, respectively. High levels of mixing within

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**Fig. 1.** Quantitative epidemiology of measles outbreak: Number of cases for (a) 1985–1992 and (b) 1993–2004 and age-specific IgG seroprevalence for (c) 1974–1977, 1992–1995, and 2004, and (d) among different populations in mountain, rural, and urban regions.
Table 2. Estimated age-specific force of infection of measles from 1974 to 2004 in five age groups

<table>
<thead>
<tr>
<th>Time</th>
<th>Data type</th>
<th>Age group (years)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1974–1977</td>
<td>Nationwide</td>
<td>0.46 0.66 0.46 0.26 0.14</td>
</tr>
<tr>
<td>1992–1995</td>
<td>Nationwide</td>
<td>0.30 0.33 0.17 0.08 0.04</td>
</tr>
<tr>
<td>1995–1996</td>
<td>Mountain (Jen-Ai)</td>
<td>0.11 0.28 0.13 0.06 0.03</td>
</tr>
<tr>
<td>1997</td>
<td>Rural (Kin-San)</td>
<td>0.11 0.27 0.25 0.13 0.07</td>
</tr>
<tr>
<td>1997</td>
<td>Urban (Taipei City)</td>
<td>0.11 0.21 0.21 0.11 0.06</td>
</tr>
<tr>
<td>2004</td>
<td>Nationwide</td>
<td>0.047 0.049 0.059 0.061 0.034</td>
</tr>
</tbody>
</table>

age groups are a unique feature of the child age groups.

The five elements in the three contact pattern matrices can be estimated by a relationship that links age group-specific FOI and the WAIFW matrix [12],

\[(1-p) \lambda(a) = \sum_{a'=1}^{5} \tilde{\beta}(a, a') (\exp(-\psi(a') - 1)) - \exp(-\psi(a'))\],

where \(\lambda(a)\) is the FOI at a specific age group \(a\), \(p\) is the coverage rate of measles vaccination, \(\tilde{\beta}(a, a')\) denotes the WAIFW matrix, and \(\psi(a')\) is the age-independent constant defined as \(\psi(a') = \sum_{a'=1}^{5} \tilde{\lambda}(a') (\tilde{i}(a') - \tilde{i}(a' - 1))\) in that \(\tilde{i}(a)\) is the mean age of age group \(a\). The age-specific value of \(R_0(a)\) for an infection in age group \(a\) can be determined based on the known FOI and transmission rate as [12],

\[R_0(a) = \sum_{a'=1}^{5} \tilde{\beta}(a, a') \tilde{i}(a') - \tilde{i}(a' - 1)\].

In the heterogeneous population, \(R_0(a)\) is the summation of the average number of secondary cases arising in age group \(a' = 1 - 5\), from a case in age group \(a\) [13, 14]. We further estimate the mean \(R_0\) for a population by averaging the \(R_0(a)\) estimates to reflect the overall spread of the infection. Self-sustaining transmission occurs when \(R_0 > 1\), allowing amplification of case numbers from one round of infection to the next. The chain of human-to-human transmission will inevitably die out when \(R_0 < 1\).

Vaccination dynamics

For an analysis of latency, an exposed but latent class E (exposed) transforms the model from SIR to SEIR because latency always affects time-dependent phenomena, such as the speed of the epidemiological response to changes in immunization or the speed of an epidemic. Generally, measles has incubation, latent, and infectious periods of 8–13 days, 6–9 days, and 6–7 days, respectively [12]. We address the vaccination dynamics using a relatively parsimonious individual-based SEIR model with homogeneous mixing to capture the effect of pre- and post-vaccination on population dynamics (Appendix 2).

RESULTS

Age-specific FOIs

We characterize the age-specific IgG seroprevalence by fitting function \(S'(a)\) [eqn (1)] to published data (Fig. 1 c, d), resulting in the fitted parameters \(k_1\) and \(k_2\) that are estimated to be 1.3, 0.7 (1978–1977); 3.3, 0.7 (1992–1995); 26.5, 3 (1995–1996 Mountain); 7, 1.4 (1997 Rural); 5.8, 1.3 (1997 Urban); and 1.5, 0.7 (2004), respectively. We estimate the age-specific FOIs by eqns (2) and (3) to take into account the different contact patterns among the major school grades in Taiwan (Table 2). The FOI of age group 2 is higher than those of other age groups, indicating the FOI of age group 2 decreasing from 1974 to 2004, corresponding to the decreasing number of cases of measles epidemics in Taiwan (Table 2, Fig. 1 a, b).

Our results show that the peak values of FOIs are estimated to be 0.5, 0.37, and 0.07 year\(^{-1}\) for 1974–1977, 1992–1995, and 2004, respectively, indicating that the FOIs decreased after the measles vaccination programmes (Fig. 2 a). The vaccination policy was modified several times due to measles outbreaks in 1985, 1988–1989, and 1992 and this may explain the decreasing FOIs. The recommended ages for vaccination have been changed several times since 1978: two doses at ages 9 and 15 months in 1984, one dose at age 12 months in January 1988, and two doses...
at ages 9 and 15 months in May 1988 due to the eruption of measles outbreaks [6]. On the other hand, the age-/population-specific FOIs, taking into account the populations in mountain, urban, and rural regions in Taiwan, indicate that prevaccination FOIs are greater than post-vaccination FOIs. However, the patterns of population-specific post-vaccination FOIs are slightly different (Fig. 2b). Different regional settings reflect the complicated contact pattern or the transmission probability.

**Age-/population-specific $R_0$ estimates**

The choice of contact pattern matrix structures can strongly influence the age group-specific $R_0$ estimates (Fig. 3). The age group-specific $R_0$ estimates based on $\hat{\beta}_{ml}(a,a')$ and $\hat{\beta}_{m2}(a,a')$ have the similar profiles that are different from contact pattern $\hat{\beta}_{m1}(a,a')$ (Fig. 3a,b). The highest values of age-group-specific $R_0$ are estimated to be 13.2 and 16.1 for age groups 2 and 4 for $\hat{\beta}_{m1}(a,a')$ and $\hat{\beta}_{m2}(a,a')$, respectively, whereas it is 6.05 for age group 2 for $\hat{\beta}_{m3}(a,a')$ in 1974–1977 (Fig. 3a). The age group-specific $R_0$ estimates have very similar profiles for the three contact patterns in 2004 (Fig. 3c).

Figure 4 shows the age-/population-specific $R_0$ (Fig. 4a,c,e) and FOIs (Fig. 4b,d,f) for mountain, rural, and urban regions for specific contact pattern

![Fig. 2. Estimates of age-specific force of infection (FOI).](https://www.cambridge.org/core/core/10.1017/S0950268806007369)
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\[\tilde{\beta}_{ma}(a, a')\]

taking into account the age groups being primarily from contacts within their own age group. The age group-specific \(R_0\) estimates are still high at age group 2 for the three regional population settings (Fig. 4a, c, e) in that the population-specific average \(R_0\) estimates are 2.24, 2.51, and 1.83, whereas the average FOIs are 0.14, 0.16, and 0.12 year\(^{-1}\) for the urban, rural, and mountain regions, respectively.

Fig. 4. Age group-/population-specific basic reproduction ratio and force of infection estimates based on specific contact matrix \(\tilde{\beta}_{ma}(a, a')\). (a, b) Mountain (1995–1996), (c, d) rural (1997), and (e, f) urban (1997) regions.
Measles vaccination effectiveness on $R_0$

Figure 5 shows the effective reproduction ratio estimates of all age groups including the nationwide $R_0$ (1978, 1992, and 2004) and regional population-mates of all age groups including the nationwide measles vaccination campaigns. The measles vaccination criteria year was set in 1978 to separate pre- and post-vaccination campaigns. The measles vaccination effect on effective reproduction ratio was set in 1978 to separate pre- and post-measles vaccination campaigns. The measles vaccination criteria year that separates pre- and post-vaccination campaigns.

Pre- and post-vaccination dynamics

We formulate a mathematical model characterizing the nationwide SEIR population dynamics in terms of various FOIs and the realistic numbers of population in the specific years of 1974–1977, 1992–1995, and 2004 to describe the epidemic dynamics at age group 2 (2–3 years old) (Fig. 6). When an epidemic starts to spread, the number of susceptibles (S) decrease, whereas exposed (E), infected (I), and recovery (R) increase until each infected becomes immunized. The results show that the level of peak infected numbers of cases are decreasing from $4.96 \times 10^4$ (1974–1977), $1.87 \times 10^4$ (1992–1995) to $0.38 \times 10^4$ (2004), whereas the onset times of peak infected number are 9, 11, and 20 days for 1974–1977, 1992–1995, and 2004, respectively (Fig. 6c).

DISCUSSION

The design of effective elimination programmes for measles is often hampered by the lack of basic seroepidemiological information. In this study, we reappraised the published measles seroepidemiological data in Taiwan from 1974 to 2004, having robust age-stratified serological information on exposure and immunity following community-based studies. Combining this with a standard SEIR structure in that the transmission between and within each age group occurs at different rates and is controlled by the WAIFW matrix, we were able to parameterize a seroepidemiological model to further predict the impact of vaccination programmes on measles elimination. Our central findings concerning the effectiveness of measles immunization programmes and the potential impact of mass vaccination seem robust to key model assumptions and the limitations of the input data.

We presume measles transmission between and within each age group experiencing homogeneous mixing, although the model reasonably predicts measles dynamics of pre- and post-vaccination. Kanaan & Farrington [17] used a Bayesian approach to evaluate the 22 models of the contact-pattern matrices by reviewing published models to obtain prior model probabilities based on published frequency and expert opinions, recommending that the assortative mixing model is a best model type among those surveyed. Our results show the age-/population-specific $R_0$ at the mountain, rural, and urban regions for specific contact pattern $\beta_{n2}(a,a')$ (Fig. 4a, c, e), taking into account that the age groups are primarily from contacts within their own age group, indicating that the matrix $\beta_{n2}(a,a')$ is a more realistic and accurate matrix compared with the other two contact matrices. Edmunds et al. [8] suggested that it is acceptable to use the epidemiological parameters such as the age-specific FOIs and $R_0$ for different countries to modify the measles transmission, indicating that the epidemiological parameters seem similar for different population settings. Glass et al.
further revealed that heterogeneity in vaccination coverage can lead to a much increased rate of infection among unvaccinated individuals associated with a simultaneous drop in the average age at infection, suggesting the potential effect of heterogeneity in measles vaccination on population immunity. In future work, we may consult, among others, Babad et al. in England and Wales [28], Roberts & Tobias in New Zealand [29], and Manfredi et al. in Italy [30] for more useful applications of measles modelling in a nationwide-scale study and implicate the proposed model to the other common contagious diseases of childhood such as chickenpox.

Wallinga et al. [16] pointed out that quantitative study in social networks research of human contact patterns have recently begun to characterize relevant network structures, and mathematical modelling is shedding new light on how specific aspects of contact patterns can alter the spread of infectious diseases and the evolution of the infective agents. Moreover, Wallinga et al. [16] also provided three network characteristics that may have an important bearing on...
the spread of infectious diseases – the average number of contacts, the network’s transitivity and the characteristic path length. Matthews & Woolhouse [31] also suggested that the transmission model could compose of biological information, epidemiology information, real-time data, and demographic information to precisely describe the model. Consequently, a combination of theoretical and empirical research is needed to increase our understanding of the impact of human contact networks on the spread and evolution of infectious agents, and to assess the implications for the planning of public health policy.

Although a useful insight can certainly be gained from more complex models such as the time-series SEIR model used to analyse both endemic cycle and epidemic outbreaks in measles [32], the key benefits of models such as those presented here are the logical straightforwardness and relative simplicity of the results. We conclude that even simplified models are useful in assessing alternate strategies for control and guiding research in further refining childhood vaccination modelling for eradication of disease by mass regional or nationwide vaccination campaigns.

**APPENDIX 1. Contact pattern matrices**

The transmission between and within each age group occurs at different rates and is controlled by the following three WAIFW matrices:

\[ \tilde{\beta}_{m}(a, a') = \begin{pmatrix} \beta_1 & \beta_1 & \beta_1 & \beta_1 & \beta_1 \\ \beta_3 & \beta_3 & \beta_3 & \beta_3 & \beta_3 \\ \beta_4 & \beta_4 & \beta_4 & \beta_4 & \beta_4 \\ \beta_5 & \beta_5 & \beta_5 & \beta_5 & \beta_5 \end{pmatrix} , \]
\[ \beta_{ma}(a,a') = \begin{pmatrix} \beta_1 & \beta_2 & \beta_3 & \beta_4 & \beta_5 \\ \beta_2 & \beta_3 & \beta_4 & \beta_5 \\ \beta_3 & \beta_4 & \beta_5 \\ \beta_4 & \beta_5 \\ \beta_5 \end{pmatrix}, \]  
\tag{A 2}

\[ \tilde{\beta}_{ma}(a,a') = \begin{pmatrix} \beta_1 & \beta_2 & \beta_3 & \beta_4 & \beta_5 \\ \beta_1 & \beta_2 & \beta_3 & \beta_4 & \beta_5 \\ \beta_1 & \beta_2 & \beta_3 & \beta_4 & \beta_5 \\ \beta_1 & \beta_2 & \beta_3 & \beta_4 & \beta_5 \\ \beta_1 & \beta_2 & \beta_3 & \beta_4 & \beta_5 \end{pmatrix}, \]  
\tag{A 3}

where \( \beta(a,a') \) is the transmission rate describing the probability that an infective of age \( a' \) will be infected by a susceptible of age \( a \).

**APPENDIX 2. SEIR model**

The standard SEIR model categorizes individuals into five distinct age groups: 0–1 (babies), 2–3 (toddlers), 4–6 (preschool), 7–14 (primary school), and 15–35 (adults). Within each age class, the population is subdivided into susceptible (S), exposed (E), infected (I), and recovery (R) groups. Therefore, the dynamics of measles vaccination can be modelled straightforwardly using a simple parameterized set of differential equations as

\[ \frac{dS}{dt} = -\lambda S(t) - \mu S(t), \]  
\tag{A 4}

\[ \frac{dE}{dt} = \lambda S(t) - \alpha E(t) - \mu E(t), \]  
\tag{A 5}

\[ \frac{dI}{dt} = \alpha E(t) - \nu I(t) - \mu I(t), \]  
\tag{A 6}

\[ \frac{dR}{dt} = \nu I(t) - \mu R(t), \]  
\tag{A 7}

\[ N(t) = S(t) + E(t) + I(t) + R(t), \]  
\tag{A 8}

where \( N(t) \), \( S(t) \), \( E(t) \), \( I(t) \), and \( R(t) \) are the number of total population, susceptible, exposed, infected, and recovery at time \( t \), respectively, \( \lambda \) is the FOI per unit time (year\(^{-1}\)), \( \sigma \) is the rate at which an exposed individual becomes infectious per unit time that is equal to 0-143 day\(^{-1}\) (1/measles incubation period of 7 days), \( \nu \) is the rate at which an infectious individual recovers per unit time (day\(^{-1}\)), \( \mu \) is the birth rate and death rate that is equal to 0.013 year\(^{-1}\) (1/human average lifetime of 75 years), and \( N \) is the population number that can be adopted from the Department of Statistics, Minister of the Interior.

**DECLARATION OF INTEREST**

None.

**REFERENCES**