### **PROCEEDINGS**

OF

## THE ROYAL SOCIETY OF EDINBURGH

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Bounds for the point spectrum for a Sturm-Liouville equation

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Padé approximant bounds on the positive solutions of some nonlinear elliptic equations

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Monotone techniques and semilinear elliptic boundary value problems

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Eigenfunction expansions and spectral matrices of singular differential operators

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