# Formation and stability of the prismatic stacking faultin wurtzite (Al,Ga,In) nitrides 

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#### Abstract

The formation of the $\{1 \overline{2} 10\}$ stacking fault, which has two atomic configurations in wurtzite $(\mathrm{Ga}, \mathrm{Al}, \mathrm{In}) \mathrm{N}$, has been investigated by high resolution electron microscopy and energetic calculations. It originates from steps at the SiC surface and it can form on a flat (0001) sapphire surface. A modified Stillinger-Weber potential was used in order to investigate the relative stability of the two atomic configurations. They have comparable energy in AlN, whereas the $1 / 2<10 \overline{1} 1>\{1 \overline{2} 10\}$ configuration is more stable in GaN and InN. In GaN layers, only the $1 / 2<10 \overline{1}_{1}>\left\{1 \overline{2}_{10}\right\}$ configuration was observed. The $1 / 6<20 \overline{2} 3>$ configuration was found in small areas inside the AIN buffer layer where it folded rapidly to the basal plane, and when back into the prismatic plane, it took the $1 / 2<10 \overline{1} 1>\{1 \overline{2} 10\}$ atomic configuration.


## INTRODUCTION

Extensive research effort is being undertaken on wide band gap of GaN based semiconductors for their very promising device possibilities. Efficient laser diodes have been fabricated for emission in the blue range[1] in layers grown on sapphire by Metal Organic Vapor Epitaxy (MOVPE). The active GaN layers contain large densities of crystallographic defects[2,3], among which, one finds $\{1 \overline{2} 10\}$ planar defects which have recently been called double positioning boundaries (DPBs)[4,5], stacking mismatch boundaries (SMBs)[6] or inversion domain boundaries (IDBs)[7]. These faults have recently been investigated using High Resolution Electron Microscopy (HREM) and Convergent Beam Electron Diffraction (CBED), and it was shown that they are stacking faults on top of both sapphire and $\operatorname{SiC}[8-10]$. In fact these planar defects have already been studied in the sixties and two displacement vectors have been measured by conventional microscopy[11,12]. In wurtzite ZnS , Blank et al[12] were the first to study the planar defects which folded from basal to prismatic $\{1 \overline{2} 10\}$ planes, and to interpret them as stacking faults whereas other authors considered them to be thin lamella of the sphalerite phase in CdS[13]. In this work, we have investigated these faults in (Al,Ga)N epitaxial layers by HREM and
modified the Stillinger-Weber[14] (SW) potential in order to analyze their stability in AlN, GaN, InN. The theoretical results were found to correlate with the HREM observations for AlN and GaN.

## RESULTS

## The stacking fault atomic structure

Two atomic models exist in the literature for the $\{11 \overline{2} 0\}$ prismatic fault in wurtzite materials as originally characterized by conventional electron microscopy in the 60s by Drum[11] and Blank[12], respectively. Their projections are shown in figure 1 along [0001].


Figure 1. Atomic configurations of the $\{1 \overline{2} 0\}$ stacking fault seen along [0001], a) The $1 / 2$ [1011] displacement vector, b) The $1 / 6$ [ $20 \overline{2} 3$ ] stacking fault

## Formation mechanisms

## A. Formation on (0001) $\mathbf{6 H}-\mathrm{SiC}$ surface

The [0001] SiC surface exhibits steps of various heights. If one ignores the mismatch along the c axis which is small, the GaN and SiC can be geometrically consid


Figure 2. Generation of a prismatic stacking fault on a I1 type of step on the (0001) surface of $6 \mathrm{H}-\mathrm{SiC}$

A 6 H -portion under a step can be decomposed into a faulted 2 H stacking, and depending on the type of step, the decomposition may result in a displacement vector between the two crystallites which grow on the adjacent terraces (fig.2). In fact between the two polytypes, the only displacement vectors $d$ which can result from the decomposition are those of the hcp lattice ( the intrinsic $\left.\mathrm{I}_{1}, \mathrm{R}_{\mathrm{I} 1}=1 / 6\langle 20 \overline{2} 3\rangle, \mathrm{I}_{2}, \mathrm{R}_{\mathrm{I} 2}=1 / 3<10 \overline{1} 0\right\rangle$ and the extrinsic $E, R_{E}=1 / 2<0001>$ ). Among them, $I_{1}$ and $E$ have $1 / 2 c$ component along the c axis and may lead to the formation of an extended defect in the epitaxial layer (fig.2). The displacement vector identical to $I_{2}$ is confined in the interface and may contribute to release the misfit strain. When all the step heights are taken account, it was found that the largest fraction of the faults that will be formed are $\mathrm{I}_{1}$ as shown in table 1

| Interface | Defect Character | Interface Configuration: <br> Wurtzite <br> Defect ratio: (\%) |
| :--- | :--- | :--- |
| 3 H / 6H | I1 | 45 |
|  | I2 | 22 |
|  | - | - |

Table 1. Type of defects forming at an interface step between $2 \mathrm{H}-\mathrm{GaN}$ and $6 \mathrm{H}-\mathrm{SiC}$

## B. Growth on (0001) sapphire

The continuation of the two hcp anionic lattices may be described by three types of polyhedra at the interface. They are built with oxygen $(\mathrm{O})$ and nitrogen $(\mathrm{N})$ at their vertices, the metal $(M)$ at the centre: one tetrahedron $(3 O, M, N)$ that leads to upward polarity, one tetrahedron $(\mathrm{O}, \mathrm{M}, 3 \mathrm{~N})$ and one octahedron $(3 \mathrm{O}, \mathrm{M}, 3 \mathrm{~N})$ that lead to downward polarity. All these factors are taken into account in order to analyze how the resulting translation can be accommodated in the GaN layers by the formation of planar defects in the epitaxial layer: stacking faults (SF) or inversion domains boundaries (IDB). For the wurtzite structure, three models of IDBs have been proposed[15-18].

## B.1. Growth on a single terrace

On an oxygen terminated surface, there are four ways to build a hcp stacking of nitrogen atoms, they are related to each other by one of the three stacking fault vectors, $\mathrm{R}_{\mathrm{SF}}$, of the wurtzite structure $\left(\mathrm{R}_{\mathrm{I} 1}, \mathrm{R}_{\mathrm{I} 2}\right.$ and $\left.\mathrm{R}_{\mathrm{E}}\right)$. Since two families of tetrahedral sites are available for the $\mathrm{Ga}^{3+}$ cation, this leads to eight GaN stackings linked by the operator $\mathrm{W}_{\mathrm{CE}}=\mathrm{R}_{\mathrm{SF}}$ or $\mathrm{W}_{\mathrm{CE}}=\mathrm{R}_{\mathrm{SF}}+\mathrm{m}$ with opposite polarities(fig.3). In the case of Al-terminated surface, the number of stackings is reduced to three polyhedra due to the aluminium
position in the $\mathrm{Al}_{2} \mathrm{O}_{3}$ structure. The systematic analysis of the polyhedra combinations allows to determine the relative proportions of the planar defects induced by the operator $\mathrm{W}_{\text {CE }}$. For instance, if the interface polyhedra are exclusively downward tetrahedra, the $\mathrm{R}_{\mathrm{SF}}$ will be only $\mathrm{R}_{\mathrm{Il}}$, and combinations of downward tetrahedra and octahedra lead to the formation of $\mathrm{R}_{\mathrm{II}}$ and $\mathrm{R}_{12}$ faults in equal proportions which may explain the formation of stacking faults inside the epitaxial layers[19-21].

## B.2. Growth on adjacent terraces

A step, between two terraces on which two GaN islands grow, introduces a translation $\mathrm{T}_{\mathrm{S}}$ between them. Its component along c axis can be reduced in $\mathrm{R}_{\mathrm{E}}=1 / 2$ $<0001>$ and a residual translation $T_{R}$. The number of $R_{E}$ is calculated to minimize the absolute value of this residual translation. For instance, the step between two A terraces with a height of $\mathrm{c} / 3$ in $\mathrm{Al}_{2} \mathrm{O}_{3}(0.433 \mathrm{~nm})$ is equivalent in GaN to $0.835 \mathrm{c}_{\mathrm{GaN}}$, or : $T_{S}=2 R_{E}+T_{R}=T_{R}$ with $T_{R}=-0.165 \mathrm{c}_{\mathrm{GaN}} \approx \mathrm{c}_{\mathrm{GaN}} / 6$. By considering all the steps between $A$ or $B$ terraces (A or B layers of the hcp stacking), the $T_{S}$ translation can be written as : $T_{S}=a R_{E}+T_{R}$ with $a=0$ or 1 and $T_{R}$ may take four values with the approximation $2 \mathrm{c}_{\mathrm{Al}_{2} \mathrm{O}_{3}} \sim 5 \mathrm{c}_{\mathrm{GaN}}$ (table.2): So, the operator relating adjacent terraces must involve this additional parameter, $\mathrm{T}_{\mathrm{R}}$ :
$\mathrm{W}_{\mathrm{CE}}=\mathrm{R}+\mathrm{m}+\mathrm{T}_{\mathrm{R}}$ where $\mathrm{R}=\mathrm{R}_{\mathrm{SF}}+\mathrm{aR}_{\mathrm{E}}$.

| Steps | $\mathrm{h}_{\mathrm{c}_{\mathrm{Al}}^{2} \mathrm{O}_{3} \text { unit }}$ | $\mathrm{T}_{\mathrm{R}} \mathrm{c}_{\mathrm{GaN}}$ unit | $\mathrm{T}_{\mathrm{R}} \mathrm{nm}$ |
| :--- | :--- | :--- | :--- |
| A-A or B-B | nc (n: integer) | 0 | 0 |
| A-B | $1 / 6,5 / 6,7 / 6,11 / 6$ | $\sim 1 / 12$ | $\sim 0.0432$ |
| A-A or B-B | $1 / 3,2 / 3$ | $\sim 1 / 6$ | $\sim 0.0863$ |
| A-B | $1 / 2,3 / 2$ | $\sim 1 / 4$ | $\sim 0.1295$ |

Table 2. Residual translation in GaN as a function of the step height in $\mathrm{Al}_{2} \mathrm{O}_{3}$


Figure 3. Four of the 8 possible stacking of wurtzite $(\mathrm{Ga}, \mathrm{Al}) \mathrm{N}$ on the (0001) sapphire surface, the polyhedra configurations at the interface are shown

As this residual translation is never equal to $\mathrm{c} / 2$, it cannot be simply accommodated by the formation of prismatic stacking faults. The operator describing IDBs can be written in order to point out the c/8 translation found inside some of the models in addition to the mirror operation (1). When compared to the residual translation $T_{R}$, the introduction of the IDB containing the $\mathrm{c} / 8$ translation may help in minimizing the shift along c at most of the steps; it is reduced to $1 / 24 \mathrm{c}_{\mathrm{GaN}}[20]$. Therefore, in the case of steps, the residual translation cannot be minimized by introducing a stacking fault. During epitaxial growth of GaN layers on (0001) sapphire, the occurrence of basal and prismatic stacking faults is not a straightforward result of the steps at the substrate surface. They form on coalescence of islands whose growth has been initiated with different polyhedra[20].

## Relative stability

The original SW potential is short and it cannot be used in order to predict the values of the non ideal c/a ratio and the vector $u$ which characterizes the displacement along the c axis between the two hcp sublattices in the wurtzite structure. It is unable to reach the third nearest neighbour atom which is responsible of the deviation of c/a ratio from the ideal value. We have added a Gaussian term which was fitted in order to allow the interaction potential to reach the third nearest neighbour. It is given by:

$$
\begin{equation*}
v_{\mathrm{g}}=\varepsilon C \exp \left\{-\left(\left(\mathrm{d}_{\mathrm{ij}}-\mathrm{r}_{1}\right) / \delta \mathrm{r}_{1}\right)^{2}\right\} \tag{2}
\end{equation*}
$$

where $\mathrm{d}_{\mathrm{ij}}$ is the bond length between atoms i and j , $\mathrm{r}_{1}$ the center of the Gaussian is situated between the second and third neighbours distances and $\Delta r_{1}$ is the width of the Gaussian function. According to the magnitude of $r_{1}$ and the sign of $C$, it is possible to adjust the c/a ratio with respect to the ideal value. The potential obtained in the previous section is applied to investigate the atomic structure of the $\{11 \overline{2} 0\}$ stacking fault. The above atomic models were taken into account with the starting configurations corresponding to the $1 / 6<2 \overline{2} 03\rangle$ and $1 / 2<1 \overline{1} 01\rangle$ stacking fault displacement vectors as discussed in the previous paragraphs. We applied the method of lattice relaxation to a set of 1984 atoms containing the defect for the two atomic models. As seen in table 3, the formation energy of each configuration depends on the compound for AIN, GaN and InN. In AlN, the two atomic configurations of the $\{11 \overline{2} 0\}$ stacking fault have a comparable value of formation energy. This is in complete agreement with our HREM observations in GaN layers and in the AlN buffers ${ }^{22}$

| model | Amelinckx $(1 / 6<2 \overline{2} 03>)$ | Drum $(1 / 2<\overline{1} 101>)$ |
| :--- | :--- | :--- |
| AlN | 100 | 100 |
| GaN | $78(123)$ | $22(72)$ |
| InN | 65 | 21 |

Table 3. Formation energy in meV/ $\mathrm{A}^{2}$ for the relaxed atomic configurations of the $\{11 \overline{2} 0\}$ prismatic stacking fault, in parenthesis are the values of reference 23

## CONCLUSION

The two configurations of the stacking fault have already been investigated by conventional electron microscopy, one in AlN and the other in ZnS respectively. They both were found to fold easily from the basal to the prismatic plane of these wurtzite materials. In the basal plane both have the $1 / 6<20 \overline{2} 3>$ displacement vector of the I1 stacking fault. In the $\{11 \overline{2} 0\}$ plane, they differ by $1 / 6<10 \overline{1} 0\rangle$, which is worth less than $4 \%$ in energetic balance between the two vectors (using the $\mathrm{b}^{2}$ criterion) in the three nitrides compounds.

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