FINDING COMMON FIXED POINTS OF NONEXPANSIVE MAPPINGS BY ITERATION: CORRIGENDUM

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In [3] the following theorem was stated.

THEOREM 1. Let X be a uniformly convex Banach space, C a closed convex subset of X, T_1, T_2, \ldots, T_k a family of nonexpansive selfmaps of C with nonempty common fixed point set. Then $\{x_n\}$, defined by

$$x_0 \in C, \ x_{n+1} = (1-\alpha)x_n + \alpha T_k x_n, \ n \ge 0, \ 0 < \alpha < 1,$$

where

$$U_1 := (1 - \alpha)I + \alpha T_1 U_0, \ U_0 = I$$
$$U_2 := (1 - \alpha)I + \alpha T_2 U_1,$$
$$\dots$$
$$U_k := (1 - \alpha)I + \alpha T_k U_{k-1}$$

converges weakly to a common fixed point of the family.

However, the theorem was actually proved only for semicontractive maps, because a portion of the proof relied on [1, Theorem 3] (stated as [3, Lemma 2]). Using an improvement of that result, [2, Theorem 8.4], enables one to prove the Theorem of [3] as stated. For completeness we state this result of Browder.

LEMMA 1. Let X be a uniformly convex Banach space, G a bounded closed convex subset of X, U a nonexpansive map of $G \rightarrow X$. Then

(a) If $\{u_j\}$ is a weakly convergent sequence in G with weak limit u_0 and if $(I - U)u_j$ converges strongly to an element w in X, then

$$(I-U)u_0=w.$$

(b) (I - U)(G) is a closed subset of X.

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