

# COMPLETE ALPHA-TENSOR FOR SOLAR DYNAMO

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**Abstract.** We applied the results of recent derivations of the  $\alpha$ -effect to the solar convection zone model by Stix (1989) to find the depth and latitude dependences of the  $\alpha$ -tensor. Pronounced inhomogeneity and anisotropy are revealed: the  $\alpha$ -coefficients for different directions are quite different and strongly latitude-dependent.

Knowledge of the complete tensoral representation of the  $\alpha$ -effect is important to develop stellar dynamos. The expressions for the coefficients  $\alpha_n$  of the  $\alpha$ -tensor,

$$\alpha_{ij} = \alpha_1(\mathbf{g} \cdot \boldsymbol{\Omega})\Omega^{-1}\delta_{ij} + \alpha_2(g_i\Omega_j + g_j\Omega_i)/\Omega + \alpha_4(\mathbf{g} \cdot \boldsymbol{\Omega})\Omega_i\Omega_j/\Omega^3, \quad (1)$$

have recently become available as fully-nonlinear functions of the angular velocity (Rüdiger and Kichatinov, 1993). In the Eq. (1),  $\mathbf{g}$  is the radial unit vector and  $\boldsymbol{\Omega}$  is the angular velocity. The tensor (1) has five non-zero components in the spherical coordinates system,  $r, \theta, \phi$ :

$$\alpha_{\phi\phi} = \alpha_1 \cos \theta, \quad \alpha_{rr} = (\alpha_1 + 2\alpha_2) \cos \theta + \alpha_4 \cos^3 \theta,$$

$$\alpha_{\theta\theta} = \alpha_1 \cos \theta + \alpha_4 \sin^2 \theta \cos \theta, \quad \alpha_{r\theta} = \alpha_{\theta r} = -\alpha_2 \sin \theta - \alpha_4 \cos^2 \theta \sin \theta.$$

All the coefficients  $\alpha_n$  are superpositions of the contributions made by the two basic inhomogeneities of density and the turbulence intensity:  $\alpha_n = \alpha^{dens} + \alpha^{int}$ . We used the solar convection zone model by Stix (1989) to evaluate the  $\alpha$ -tensor components. The results are shown in the figures 1 to 3.

Only  $\alpha_{\phi\phi}$ -component is important for the  $\alpha\Omega$ -dynamos. Fig.1 shows that the inhomogeneities of density and the turbulence intensity contribute this component with opposite signs. The  $\alpha_{\phi\phi}$  varies rather slowly with depth except for the near-bottom layer where strong intensity gradient makes the  $\alpha_{\phi\phi}$  to change its sign.

The often used isotropic representation,  $\alpha_{ij} = \alpha_0 \cos \theta \delta_{ij}$ , implies the same depth-dependences for all components of the  $\alpha$ -tensor and the independence of  $\alpha/\cos \theta$  of latitude. Our findings are in drastic contrast to the isotropic picture. The depth-dependences shown in the Figures 1 and 2 are quite different one from another and display pronounced variations from pole to equator. Next, Fig.3 shows that the  $\alpha$ -tensor possesses the off-diagonal component which is also a manifestation of anisotropy.

It is very tempting to look at the consequences of the strongly anisotropic  $\alpha$ -effect for solar dynamo. Some preliminary results are presented by Elstner and Rüdiger (1993).

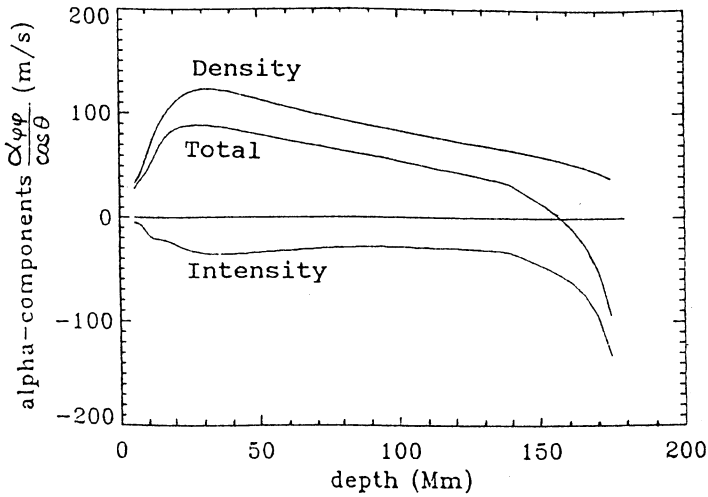


Fig. 1. The total value of  $\alpha_{\phi\phi}/\cos\theta$  and its constituents due to inhomogeneities of density and the turbulence intensity as functions of depth in the SCZ

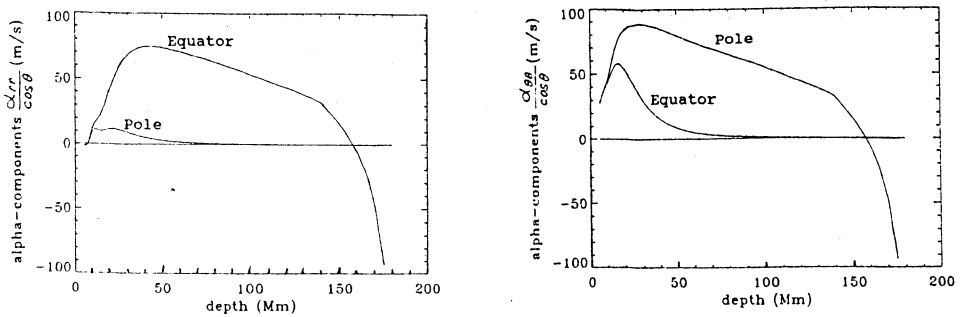


Fig. 2. The total values of  $\alpha_{rr}/\cos\theta$  (left) and  $\alpha_{\theta\theta}/\cos\theta$  (right) as functions of depth in the SCZ at the pole and the equator

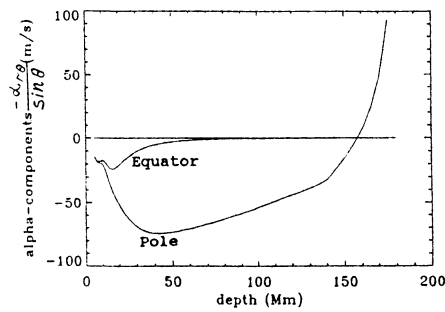


Fig. 3. The same as in Fig.2 but for the off-diagonal component,  $-\alpha_{r\theta}/\sin\theta$

References

Elstner, D. and Rüdiger, G.: 1993, *This volume*  
 Rüdiger, G. and Kichatinov, L.L.: 1993 *Astron. Astrophys.* (in press)  
 Stix, M.: 1989, *The Sun: An Introduction*, Springer, Berlin Heidelberg