Solar System Wave Function 1 2 Abolfazl Soltani 3 Department of Physics, University of Birjand, Birjand, Iran 4 Email: soltani.a.phyics@gmail.com **Abstract** 5 6 Pluto, Ceres and all planets of Solar system except Neptune, with a high approximation, follow a 7 rule called Titius-Bode rule or Bode rule, which can by no means be considered as a stochastic event. This rule shows that the distance of planets from the sun in Solar system is regulated. Here, 8 I prove that the existence of a standing and cosine wave packet, with the wavelength $\lambda = 0.6 \ AU$ 9 (AU represents the distance of Earth from the Sun) and the phase constant $\emptyset = \frac{\pi}{6}$, in solar system 10 is the reason for Bode rule. And moreover, I prove that this huge wave packet belongs to the sun. 11 Bode rule does not predict the distance of Neptune from the Sun but, this article is able to give us 12 the distance of Neptune. Based on this article, Quantum mechanics and Astronomy will enter into 13 a new stage. 14 15 **Keywords**: Solar system, Titius-Bode rule, Quantum mechanics 16 Introduction The planets of solar system move around the sun in elliptical orbits such that the sun is in one of 17 the focal points of these ellipses. These ellipses are very close to the circle, and in fact the orbits 18 19 of the planets of solar system are concentric circles. Pluto, Ceres and all planets of Solar system except Neptune, with a high approximation follow a rule known as Bode rule or Titius-Bode rule. 20 According to this rule, the distance of each planet from the Sun is equal 21 22 to $a = 0.4 AU + 0.3 AU \times 2^n$, where 0.4 AU is the distance of Mercury from the Sun (or more precisely the length of the semi-major axis of Mercury's orbit) and n = 0,1,2,3,... [1]. Table. 1 23 shows the high accuracy of the Bode rule. If this rule was only true for three or four planets, then 24 25 we could call it a coincidence, but when it is true for seven planets, plus Ceres and Pluto, there is 26 definitely a reason for it. It was historically based on this rule that Ceres was discovered in 1801[1]. In this article, I will find the reason for the existence of the Bode rule. In fact, I will prove that the 27 28 presence of a cosine and standing wave packet in solar system is the reason for existence of Bode rule; And moreover, I will prove that this wave packet belongs to the sun. 29 30 31 32 33 34

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Planet	T–B rule	Semi-major	Deviation from
	distance (AU)	axis (AU)	prediction
Mercury	0.4	0.39	-2.5%
Venus	0.7	0.72	+2.8%
Earth	1.0	1.00	0.00%
Mars	1.6	1.52	-4.77%
Ceres	2.8	2.77	-1.16%
Jupiter	5.2	5.20	+0.00%
Saturn	10.0	9.58	-4.45%
Uranus	19.6	19.20	-1.95%
Pluto	38.8	39.48	+1.05%

Table. 1. Planets distances from the Sun and the prediction of Bode rule. Bode rule cannot predict the distance of Neptune from the Sun.

Wave Function and Bode Rule

Consider a standing and cosine wave function with a wavelength $\lambda = 0.6 AU$; if we assume that the first node of this wave is at a distance of 0.1 AU from the Sun the next nodes are at the distances of 0.4 AU, 0.7 AU, 1 AU, 1.3 AU, 1.6 AU, 2.8 AU, . . . from the Sun. Each node is 0.3 AU ahead of the previous node. If we consider the planets of solar system in the position of the nodes of this wave, in such a case, there is no planet on the first node (0.1 AU) and Mercury is on the second node, Venus is on the third node, Earth is on the fourth node, Mars is on the sixth node, and the position of fifth node (1.3 AU) is empty. The seventh, eighth, and ninth nodes are empty, and Ceres is on the tenth node. Jupiter is placed on the eighteenth node and Saturn is on the thirtythird node, and Uranus, Neptune, and Pluto are on the nodes farther from the Sun. As you can see, a wave function, with the wavelength $\lambda = 0.6 AU$, easily predicts the position of the planets and it seems that a huge and standing wave plays a role in determining the position of the planets in solar system. Therefore, we can consider the reason for the Bode rule to be the existence of a large cosine wave in solar system that oscillates along the axis perpendicular to the plane of solar system. I call this wave "Solar system wave function". In this article, I will obtain the equation of this wave function. But what does this wave belong to? I answer this question in this article. The presence of a huge cosine wave in solar system seems strange at first glance, but quantum mechanics eradicates our surprise. Based on quantum mechanics, a wave packet can be assigned to each object which called the 'associated matter wave 'of that object, and this associated wave is the solution of the Schrodinger equation. In this article, I prove that the above standing and cosine wave function (Solar system wave function) is in the form of a solution of the Schrodinger equation and therefore, based on quantum mechanics, this wave must belong to an object; I demonstrate that this object is the sun. It is sun that has created a standing wave around itself and provided a definite orbit for the planets¹.

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¹ I know that Quantum mechanics, the Schrodinger equation, and the de Broglie wavelength relation can only be used for subatomic scale and objects. But, in this article, I prove that quantum mechanics is also valid in astronomical scale and I will obtain the shape of Schrodinger equation and de Broglie wavelength relation in astronomical scale.

Wave Equation of Solar System

As mentioned, a cosine and standing wave function, with the wavelength $\lambda = 0.6$ AU ($k = \frac{2\pi}{\lambda} = \frac{10\pi}{3}$), can predict the position of the planets in solar system. First I want to derive the phase constant (\emptyset) of this wave function. Any wave in which the variables x and t are entered as a combination of $kx \pm wt$ is a traveling wave [2]. For example, the equation $\sin(kx - wt + \emptyset)$ shows a traveling wave. The zeros of this sinusoidal function, which are correspond to the nodes of this wave, are found at positions x_n as follows:

$$\sin(kx_n - wt + \emptyset) = \sin(n\pi) = 0 \Longrightarrow 2\pi \left(\frac{x_n}{\lambda} - ft + \frac{\emptyset}{2\pi}\right) = n\pi \Longrightarrow x_n = \frac{\lambda}{2}(n + 2ft - \frac{\emptyset}{\pi})$$

Where f is frequency. As you can see, by variation t, the location of nodes (x_n) is changed. 71 Therefore, a standing wave is in the form of $cos(wt) cos(kx + \emptyset)$ or $sin(wt) cos(kx + \emptyset)$ or 72 $sin(wt) sin(kx + \emptyset)$ or $cos(wt) sin(kx + \emptyset)$. As mentioned, a cosine standing wave can 73 74 predict the positions of planets. Therefore, the form of the standing wave of solar system must be 75 either $sin(wt) cos(kx + \emptyset)$ or $cos(wt) cos(kx + \emptyset)$ (In the following, we choose one of these two forms). For the nodes of these two standing waves we have $cos(kx + \emptyset) = 0$. As mentioned 76 previously, Mercury is on the second node of Solar system wave function (the second node 77 corresponds to the phase $\frac{3\pi}{2}$). We have: 78

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$$x_{Mercury} = 0.4 AU \Rightarrow \psi(x_{Mercury}) = 0 \Rightarrow cos(kx + \emptyset) = 0 \Rightarrow kx + \emptyset = \frac{3\pi}{2} \xrightarrow{k = \frac{10\pi}{3}} \emptyset = \frac{\pi}{6}$$

Having k and \emptyset , we can easily find the position of the other planets using the equation $kx + \emptyset = \frac{\pi}{2}, \frac{3\pi}{2}, \frac{5\pi}{2}, \dots, \frac{(2m-1)\pi}{2}$ (Where m is the node number). For example

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$$kx_{Venus} + \emptyset = \frac{5\pi}{2} \Rightarrow \frac{10\pi}{3}x_{Venus} + \frac{\pi}{6} = \frac{5\pi}{2} \Rightarrow x_{Venus} = 0.7 AU$$

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$$kx_{Earth} + \emptyset = \frac{7\pi}{2} \implies \frac{10\pi}{3} x_{Earth} + \frac{\pi}{6} = \frac{7\pi}{2} \implies x_{Earth} = 1 AU$$

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$$kx_{Mars} + \emptyset = \frac{11\pi}{2} \implies \frac{10\pi}{3} x_{Mars} + \frac{\pi}{6} = \frac{11\pi}{2} \implies x_{Mars} = 1.6$$

The distances of the other planets can also be calculated in the same way, which is quite consistent with experience. According to the above equation $(kx + \emptyset = \frac{(2m-1)\pi}{2})$, Neptune is on the ninety-eighth node, which corresponds to the phase $\frac{195\pi}{2}$. Contrary to the Bode rule, which is not able to predict the distance of Neptune, our wave theory predicts the position of Neptune. Therefore, a cosine and standing wave function with $\emptyset = \frac{\pi}{6}$ and $k = \frac{10\pi}{3}$ can be attributed to solar system. But what is the general equation of this wave function? As mentioned, The equation of solar system must contain a component with the equation $cos(\frac{10\pi}{3}x + \frac{\pi}{6})$ and on the other hand, this wave must

be standing so that the position of the nodes (planets) does not change. Therefore, the form of solar system wave function must be either $cos(\delta wt) cos(\frac{10\pi}{3}x + \frac{\pi}{6})$ or $sin(\delta wt) cos(\frac{10\pi}{3}x + \frac{\pi}{6})$. There is no difference between $cos(\delta wt)$ and $sin(\delta wt)$. we choose the equation $cos(\delta wt) cos(\frac{10\pi}{3}x + \frac{\pi}{6})$ and then we will show that our choice is correct(δ is a constant number that we will derive its value). Since solar system has a certain size and is not infinitely wide, its wave equation must be localized (a wave packet). If we consider an expression in the form $e^{-\gamma x^2}$ (which is a Gaussian function and plays the role of a wave envelope) in the final equation, in such a case, the final equation is a localized wave or a wave packet, (the value of γ , which is a positive number, will be obtained in the following) thus, the primary form of the wave function of solar system is as follows (equation 1) and the planets are on the nodes of this wave function (Fig. 1):

$$\begin{cases} \psi(x,t) = C\cos(\delta wt)\cos(\frac{10\pi}{3}x + \frac{\pi}{6}) e^{-\gamma x^2} & x \ge 0\\ \psi(x,t) = C\cos(\delta wt)\cos(\frac{10\pi}{3}x - \frac{\pi}{6}) e^{-\gamma x^2} & x \le 0 \end{cases}$$
 (1)

In equation 1, γ , C and δ are constant values and we obtain their values in this article.

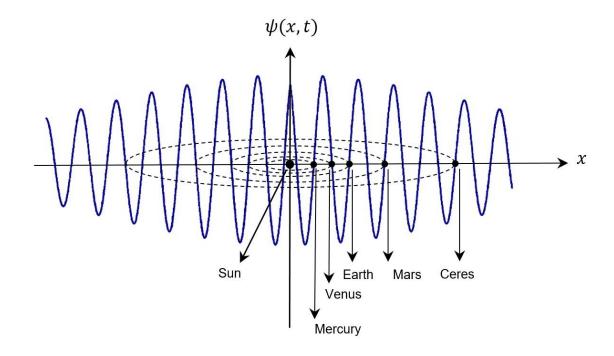


Fig. 1. Solar system standing wave packet with $\lambda = 0.6$ AU and $\emptyset = \frac{\pi}{6}$. Diagram of $\psi(x, t)$ at the moment t = 0. The value of $\psi(0,0)$ is equal to $\sqrt{3}C/2$. This diagram is drawn by a certain value of C, δ and γ in equation 1, which we will obtain their value at the end of the article. As you can see, the planets are on the nodes of the wave function. Jupiter, Saturn, Uranus, Neptune, and Pluto are on the nodes farther from the Sun.

In Fig. 1, the wave oscillates along the ψ axis over time. But the nodes and the anti-nodes do not move relative to each other along the x-axis. This does not mean that the wave packet is stationary

- in the space; it is just like passengers sitting on a train who do not move relative to each other but
- the train is moving relative to the rails. In the same way, solar system wave packet (equation 1) is
- a standing wave that rotates, along with solar system, around the center of the galaxy. As you see,
- equation (1) can easily predict the position of planets. This equation is the "wave equation of solar
- system". In the continuation of the article, we will prove that this equation is in the form of the
- Real part of a solution of Schrodinger equation² and that's why we can assign it to an object like
- 118 the sun.

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Associated Wave Packet of Sun

- 120 Consider a set of infinite numbers of flat matter waves $e^{i(kx-wt+\emptyset)}$, which move in the positive
- direction of the x-axis³, and suppose that the angular frequency of these waves is equal to w_0 and
- the wave number of these waves is around the median of k_0 and between $k_0 + \frac{\Delta k}{2}$ and
- $k_0 \frac{\Delta k}{2}$. In such a case, the resultant of these waves, using the superposition principle, is a
- wave packet with equation 2 [3][4].

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$$\psi_{total}(x,t) = \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{\infty} g(k)e^{i(kx - w_0 t + \emptyset)} dk$$
 (2)

Where k means k_x . In equation 2, g(k) is a Gaussian and symmetric function.

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$$g(k) = \left(\frac{2\alpha}{\pi}\right)^{1/4} e^{-\alpha(k-k_0)^2}$$
 (3)

- In equation 3, α is a constant with a positive value and shows the width of the bell-shaped function
- 129 g(k). $(\frac{2\alpha}{\pi})^{1/4}$ is a normalization coefficient which is obtained by normalize of g(k). Since
- equation 2 is derived from the superposition principle, it is the solution of the Schrodinger equation
- 131 [4].
- To obtain $\psi_{total}(x,t)$ from equation 2, we calculate the superposition of all of the waves in one
- moment, which we consider to be the origin of time (t = 0), and then we can obtain the net wave
- at any other time. We have:

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$$\psi(x,0) = \frac{1}{\sqrt{2\pi}} \int g(k)e^{i(kx+\emptyset)}dk \tag{4}$$

- The above equation is the momentary image of the net wave. Multiply equation 4 by $e^{ik_0x-ik_0x}$.
- 137 We have:

² As you know, the solutions of the Schrodinger equation have two parts: Real and Imaginary.

³ $e^{i(kx-wt+\emptyset)}$ is a solution of Schrodinger equation for a free particle: $i\hbar \frac{\partial}{\partial t} \psi(x,t) = -\frac{\hbar^2}{2m} \Delta \psi(x,t)$ [4].

⁴ In the Electromagnetic (EM) waves we cannot consider one w_0 for two or many waves in which their k is different from each other, because for all of the EM waves we have: w=ck where c is the speed of light. But for matter waves the issue is different. In the matter waves we have $w=\frac{\hbar k^2}{2m}$ [4]. As you can see w is the function of k and m. Therefore, it is possible to choose one value of w_0 for the waves in which their k is different from each other.

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$$\psi(x,0) = \frac{1}{\sqrt{2\pi}} e^{i(k_0 x + \emptyset)} \int g(k) e^{i(k - k_0)x} dk$$
 (5)

Considering $\vec{k} = k - k_0$, we have:

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$$\psi(x,0) = (\frac{\alpha}{2\pi^3})^{1/4} e^{i(k_0 x + \emptyset)} \int e^{-\alpha k^2} e^{ikx} dk$$
 (6)

- Using the variable transformation $k \frac{ix}{2a} = q$ (this variable transformation can be explained based
- on the theory of complex variables [3]) and the Gaussian integral $\int_{-\infty}^{\infty} dq \ e^{-\alpha q^2} = \sqrt{\frac{\pi}{\alpha}}$, equation
- 6 can be calculated. After placement and simplification, we reach the following final solution [3]:

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$$\psi(x,0) = \left(\frac{\alpha}{2\pi^3}\right)^{1/4} \sqrt{\frac{\pi}{\alpha}} e^{i(k_0 x + \emptyset)} e^{-\frac{x^2}{4\alpha}} = \left(\frac{1}{2\pi\alpha}\right)^{1/4} e^{i(k_0 x + \emptyset)} e^{-\frac{x^2}{4\alpha}}$$
 (7)

145 Lets check the normalization

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$$\int_{-\infty}^{\infty} |\psi(x)|^2 dx = \sqrt{\frac{1}{2\pi\alpha}} \int_{-\infty}^{\infty} e^{-\frac{x^2}{2\alpha}} dx = \sqrt{\frac{1}{2\pi\alpha}} \sqrt{2\alpha\pi} = 1$$

- Given a normalized g(k), we get the normalized $\psi(x)$.
- Now, how is the time variation of equation 7? Let's go back to equation 2:

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$$\psi(x,t) = \frac{1}{\sqrt{2\pi}} \int g(k)e^{i(kx-w_0t+\emptyset)}dk = \left(\frac{\alpha}{2\pi^3}\right)^{1/4} \int e^{-\alpha(k-k_0)^2}e^{i(kx-w_0t+\emptyset)}dk$$

150 We put $e^{ik_0x-ik_0x}$ in the equation:

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$$\psi(x,t) = (\frac{\alpha}{2\pi^3})^{1/4} e^{i(k_0 x + \emptyset) - iw_0 t} \int e^{-\alpha k^2} e^{ikx} dk$$

- This integral is similar to integral 6, which led to $\psi(x,0)$ (Equation 7). Therefore, the output wave
- equation of a set of the infinite number of waves $e^{i(kx-w_0t+\emptyset)}$, which are moving in the positive
- direction of the x-axis, is equal to :

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$$\psi(x,t) = \psi_1(x,t) = \left(\frac{1}{2\pi\alpha}\right)^{1/4} e^{i(k_0x - w_0t + \emptyset)} e^{-\frac{x^2}{4\alpha}}$$
 (8)

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$$e^{i\theta} = \cos\theta + i\sin\theta \implies Re \,\psi_1(x,t) = \left(\frac{1}{2\pi\alpha}\right)^{1/4} \cos(k_0 x - w_0 t + \emptyset) \,e^{-\frac{x^2}{4\alpha}} \tag{9}$$

- Due to the presence of the factor $k_0x w_0t$, Equation 9 represents a traveling wave packet that
- propagates in the positive direction of the x-axis [2]. This means that the location of the nodes is
- 159 not known.
- Similarly, we use the recent trend to obtain the superposition of flat waves traveling in the negative
- direction of the x-axis, i.e. $e^{i(kx+w_0t+\emptyset)}$. If we do this, we get to Equation 10:

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$$\psi_2(x,t) = \left(\frac{1}{2\pi\alpha}\right)^{1/4} e^{i(k_0 x + w_0 t + \emptyset)} e^{-\frac{x^2}{4\alpha}}$$
 (10)

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$$Re \,\psi_2(x,t) = \left(\frac{1}{2\pi\alpha}\right)^{1/4} \cos(k_0 x + w_0 t + \emptyset) \,e^{-\frac{x^2}{4\alpha}} \tag{11}$$

- 164 This equation shows a traveling wave packet that propagates in the negative direction of
- 165 the x-axis.
- Now we sum up the two equations 11 and 9 together to get the final wave.

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$$Re \,\psi_{total}(x,t) = Re \,\psi_1 + Re \,\psi_2$$

168 Thus:

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$$Re \,\psi_{total}(x,t) = \left(\frac{1}{2\pi\alpha}\right)^{1/4} e^{-\frac{x^2}{4\alpha}} \left[\cos(k_0 x - w_0 t + \emptyset) + \cos(k_0 x + w_0 t + \emptyset)\right] \tag{12}$$

- Using the equation $\cos\alpha + \cos\beta = 2\cos\frac{1}{2}(\alpha + \beta)\cos\frac{1}{2}(\alpha \beta)$ and $\cos(\theta) = \cos(-\theta)$ we
- obtain the equation of a standing wave packet.

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$$\begin{cases} \alpha = k_0 x - w_0 t + \emptyset \\ \beta = k_0 x + w_0 t + \emptyset \end{cases} \Rightarrow Re \, \psi_{total}(x, t) = 2(\frac{1}{2\pi\alpha})^{1/4} \cos(k_0 x + \emptyset) \cos(w_0 t) e^{-\frac{x^2}{4\alpha}} \tag{13}$$

- 173 There is not the structure of $kx \pm wt$ in Equation 13 so the ψ_{total} is a standing wave. As you
- observe, Equation 13, which is the real part of a solution of the Schrodinger equation, is exactly
- the same as equation 1 for $x \ge 0$, which is solar system wave function. It means that equation 1 is
- the real part of a solution of the Schrodinger equation. It means that the Schrodinger equation and
- quantum mechanics are valid in astronomical scale. This is a great achievement in physics. by
- comparing equation 13 and equation 1, we have

$$\delta = 1 \quad , \quad \gamma = \frac{1}{4\alpha} \quad and \quad C = 2(\frac{1}{2\pi\alpha})^{1/4}$$

- 180 If we put these values in Equation 1, then we get the final equation of solar system wave function
- 181 for $x \ge 0$:

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$$Re \,\psi_t(x,t) = 2\left(\frac{1}{2\pi\alpha}\right)^{1/4} \cos(w_0 t) \cos\left(\frac{10\pi}{3}x + \frac{\pi}{6}\right) \, e^{-\frac{x^2}{4\alpha}} \qquad x \ge 0 \tag{14}$$

- 183 Equation 14 is obtained by calculating the superposition of a set of infinite number of waves
- 184 $e^{i(kx-w_0t+\emptyset)}$ and $e^{i(kx+w_0t+\emptyset)}$ that move in opposite directions to each other (pay attention to the
- + sign behind \emptyset). Now if we sum a set of infinite number of flat wave functions with the equations
- 186 $e^{i(kx-w_0t-\emptyset)}$ and $e^{i(kx+w_0t-\emptyset)}$ (pay attention to the sign behind \emptyset) together, by following the
- path we have taken from equation 2 to equation 14, we reach the following relation;

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$$Re \, \psi_t(x,t) = 2(\frac{1}{2\pi\alpha})^{1/4} \cos(w_0 t) \cos(\frac{10\pi}{3} x - \frac{\pi}{6}) e^{-\frac{x^2}{4\alpha}}$$

189 Which is the same as equation 1 for $x \le 0$. Therefore, the final form of solar system wave function 190 (Equation 1) is as follows:

$$\begin{cases}
Re \,\psi(x,t) = 2\left(\frac{1}{2\pi\alpha}\right)^{1/4}\cos(w_0t)\cos\left(\frac{10\pi}{3}x + \frac{\pi}{6}\right) e^{-\frac{x^2}{4\alpha}} & x \ge 0 \\
Re \,\psi(x,t) = 2\left(\frac{1}{2\pi\alpha}\right)^{1/4}\cos(w_0t)\cos\left(\frac{10\pi}{3}x - \frac{\pi}{6}\right) e^{-\frac{x^2}{4\alpha}} & x \le 0
\end{cases} \tag{15}$$

- In this equation, the larger the α , the more the width of wave packet is, along the x-axis. We drew Fig. 1 by $\alpha = 10$.
- Here we demonstrated that solar system wave equation (equation 1) is the real part of a solution of the Schrodinger equation. So, based on quantum mechanics, we can assign it to an object in
- 196 Solar system. The closest star to solar system is at a distance of 4.8 light-years, which is so far.
- And the biggest and heavyset object in solar system is Sun. Therefore, the wave function of solar
- system can only belong to the sun. This wave was created during the formation of solar system.
- 199 With the formation of the young sun, from the molecular cloud and early nebula [5], the wave
- function of solar system was created. And certain orbits were created by this wave for the planets.
- In some orbits, planets have formed and in others no planets have formed.
- In this article, we proved that the Schrodinger equation is valid in astronomical scale; on the other
- hand, as you know, the Schrodinger relation is based on de Broglie equation $(\lambda = \frac{h}{mv})$. Therefore,
- 204 the de Broglie equation is valid in astronomical scale⁵. But, according to the very large mass of
- Sun, using the de Broglie relation the wavelength of 0.6 AU will not obtain. So, instead of Planck
- 206 constant we must choose another value for celestial objects, which is larger than h. We call
- 207 this new value the Planck constant in Astronomy ($h_{Astronomy}$) abbreviated as h_A and we
- have: $\lambda_A = \frac{h_A}{P}$. In such a case, the Schrodinger equation in the astronomical scale can be written
- as follows:

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$$i\hbar_A \frac{\partial}{\partial t} \psi(x, t) = -\frac{\hbar_A^2}{2m} \Delta \psi(x, t)$$
 (16)

- If we follow the path of proving the Schrodinger wave equation and put the value h_A instead of h,
- we reach equation 16. The Davisson–Germer experiment [8] is considered as the confirmation of
- 213 de Broglie equation and the Schrodinger equation at the atomic scale, and the regularity of the
- 214 distances of the planets from sun can be considered as the confirmation of equation 16 and the
- formula $\lambda_A = \frac{h_A}{P}$. Moreover, for the celestial wave packet we have $w = \frac{h_A k^2}{2m}$.

⁵ There is no problem about this issue. Because the de Broglie relation is a guess [6][7] and therefore considering a similar relation in astronomical scale is without problem. The Davisson–Germer experiment [8] is the confirmation of de Broglie equation in subatomic scale and the regularity of the distances of the planets from sun (Titius-Bode rule) is the confirmation of de Broglie equation in astronomical scale.

Conclusion

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- In this article, by investigating the distances of the planets of solar system from Sun, we 218 219 concluded that a huge, cosine, and standing wave packet surrounds our solar system. Using 220 Mathematics calculations, it was proved that this wave packet belongs to the sun. It is the sun that 221 has created a standing wave around itself and provided a definite orbit for the planets. This wave was created during the formation of solar system. With the formation of the young sun, from the 222 molecular cloud and early nebula, the wave function of solar system was created. And certain 223 224 orbits were created by this wave for the planets. In some orbits, planets have formed and in others no planets have formed. Finally, I obtained the Schrodinger equation in astronomy, which 225 describes the behavior of huge astronomical wave packets. My wave theory predicts the distances 226 227 of all of the planets (including Neptune), plus Ceres and Pluto, but as we have seen, the Bode rule does not predict the distance of Neptune. Describing the distances of the planets by a quantum 228 229 wave packet can be considered as another confirmation of the validity of Quantum theory. It seems that, we cannot present any justification for Bode rule except wave theory. 230
- In addition to the astronomical scale, in the atomic scale, according to this article, it is very likely that electrons are located on the nodes of the associated wave packet of the atom nucleus.
- This issue can be discussed and investigated in future studies.

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